

Coherent X-ray Diffraction as a probe of Nanocrystalline Materials

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Spring-8 Seminar
13 October 2004

Outline

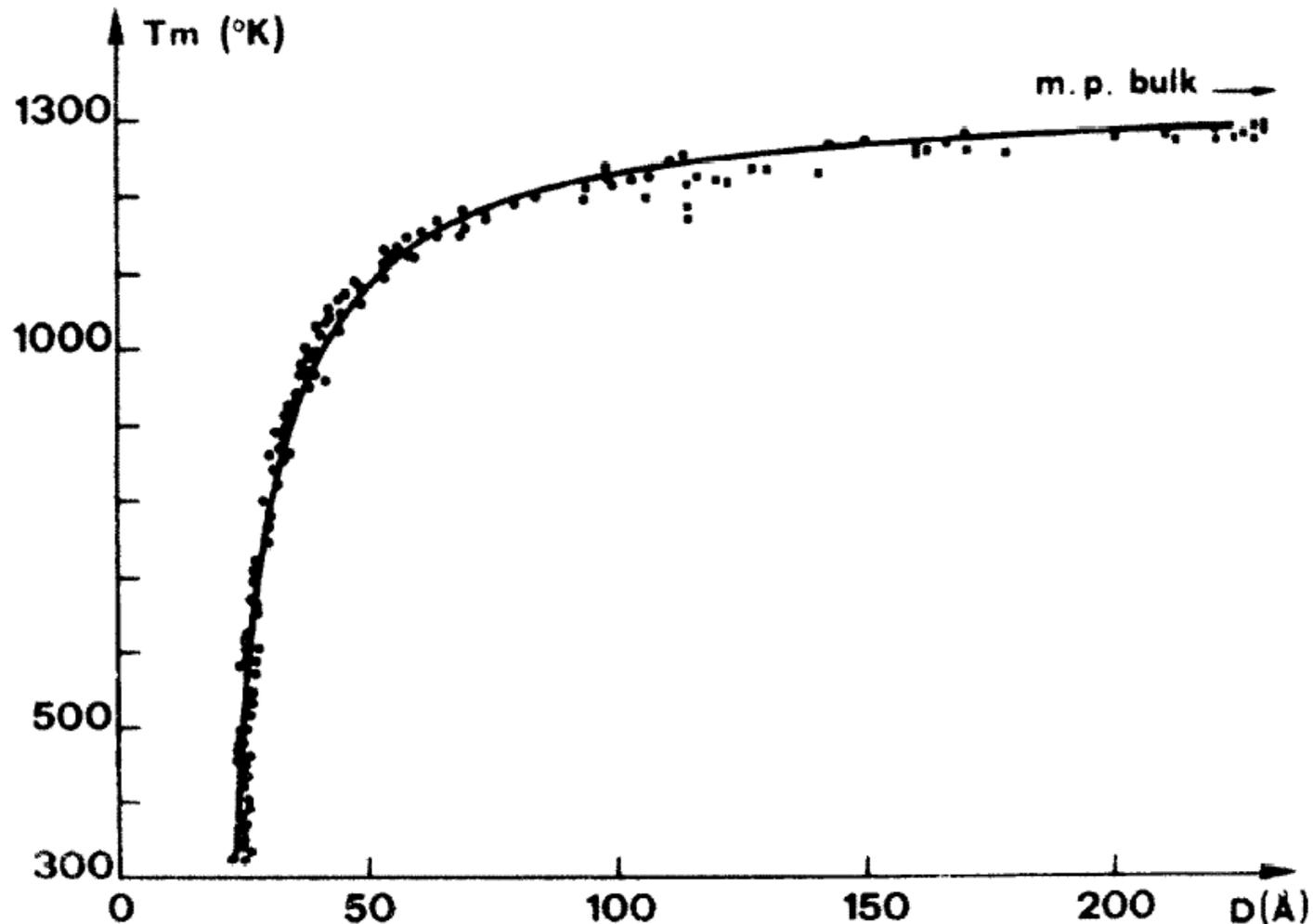
- Coherence in Diffraction
- The **Phase** Problem
- Nanocrystal Shapes
- Imaging of **Phase** Objects
- Quantum Dot structures
- How small can we go?

Goals of Coherent Diffraction

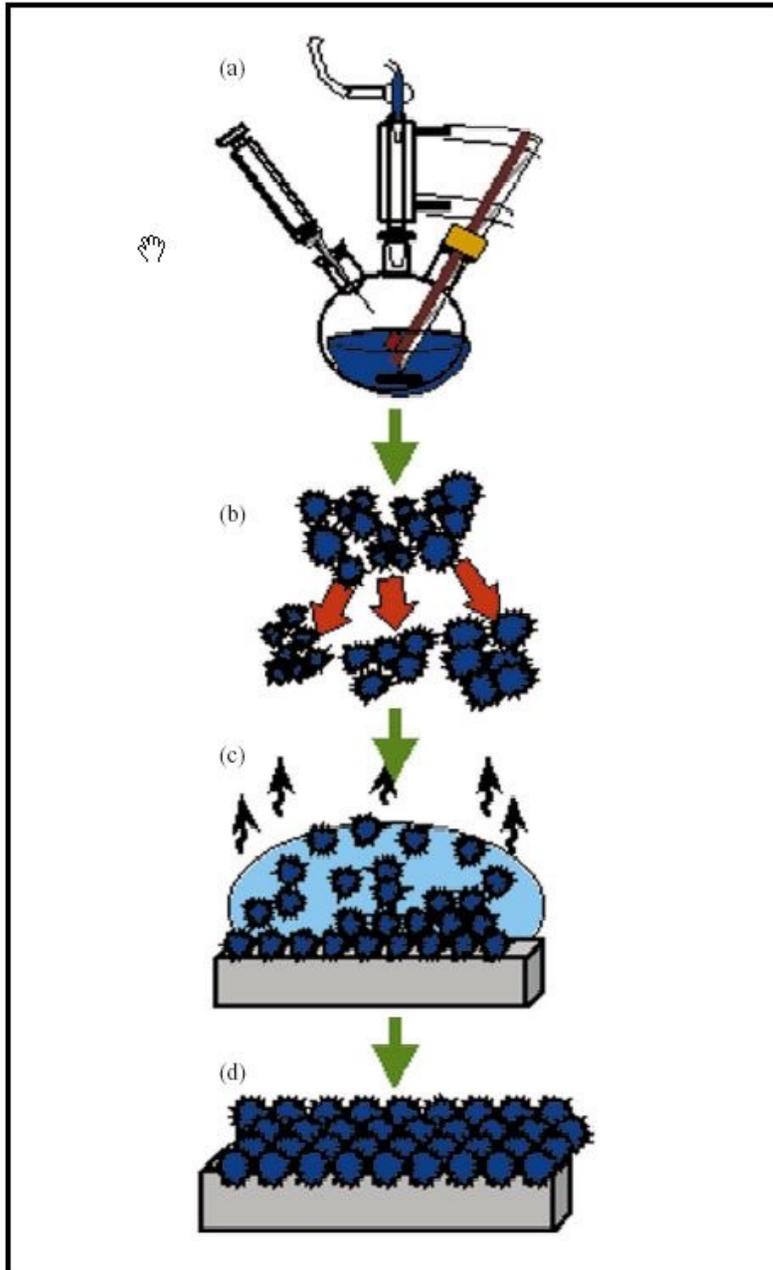
- Thermodynamic fluctuations
 - No ensemble average in CXD
- Probe of structure on **nm** scale
 - 1D, 2D and 3D
 - non-periodic object gives **continuous** $F(\mathbf{q})$
- **Oversampling** (in reciprocal space) permits solution of the **phase** problem

Size-dependent Melting of Au Particles

P. Buffat and J-P. Borel, Phys. Rev. A 2287-97 (1975)

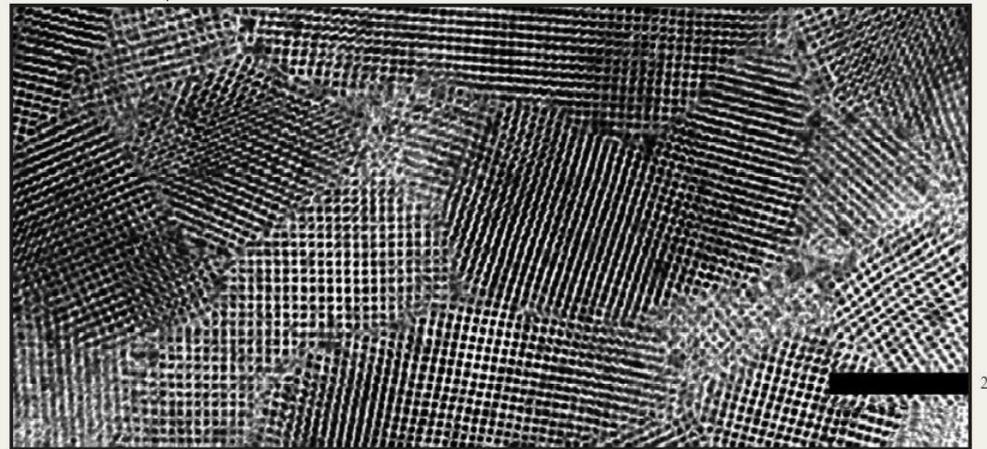


Chemical Synthesis of Nanocrystals

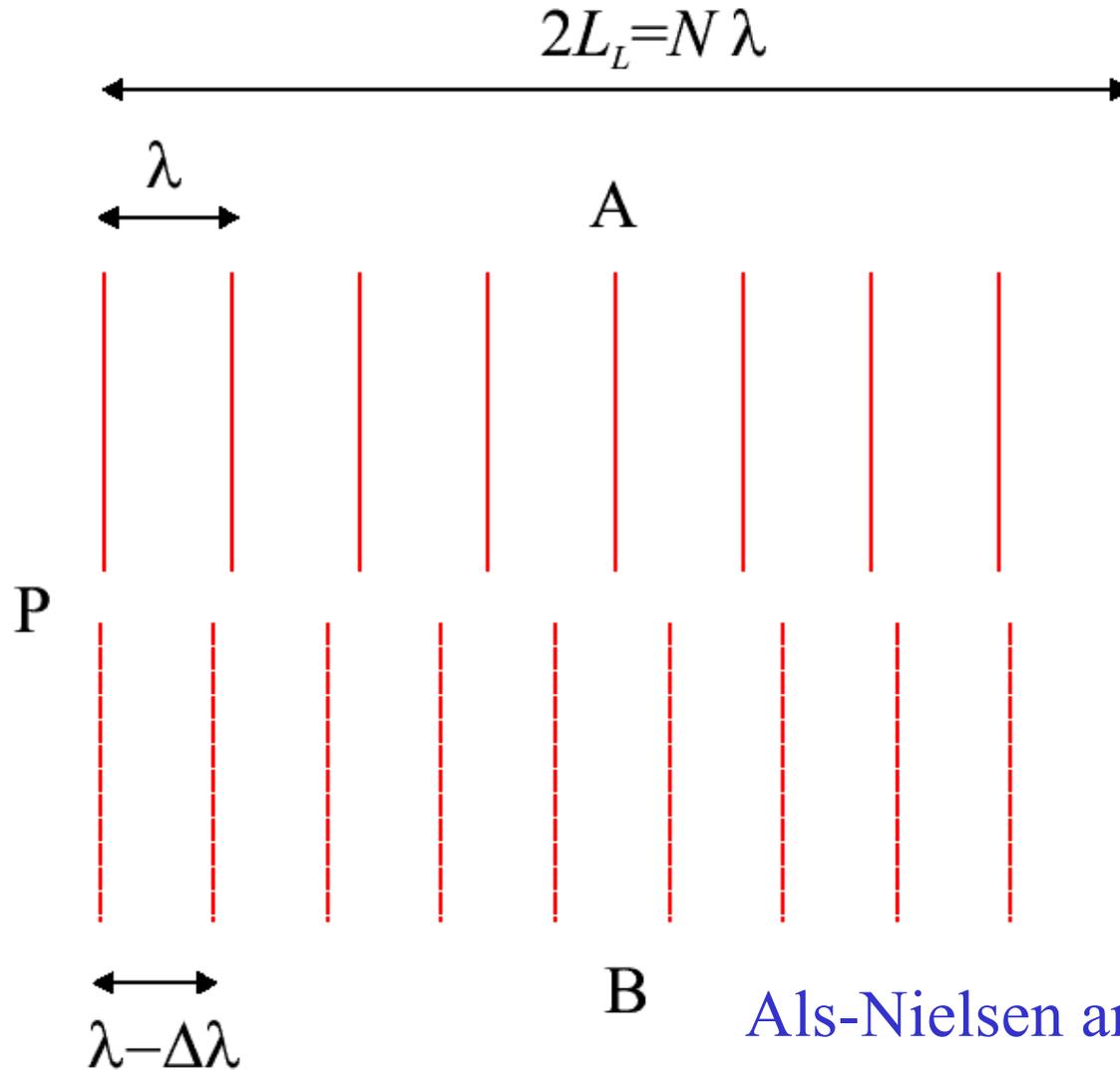


- Reactants introduced rapidly
- High temperature solvent
- Surfactant/organic capping agent
- Square superlattice (200nm scale)

C. B. Murray, IBM J. Res. & Dev. **45**
47 (2001)



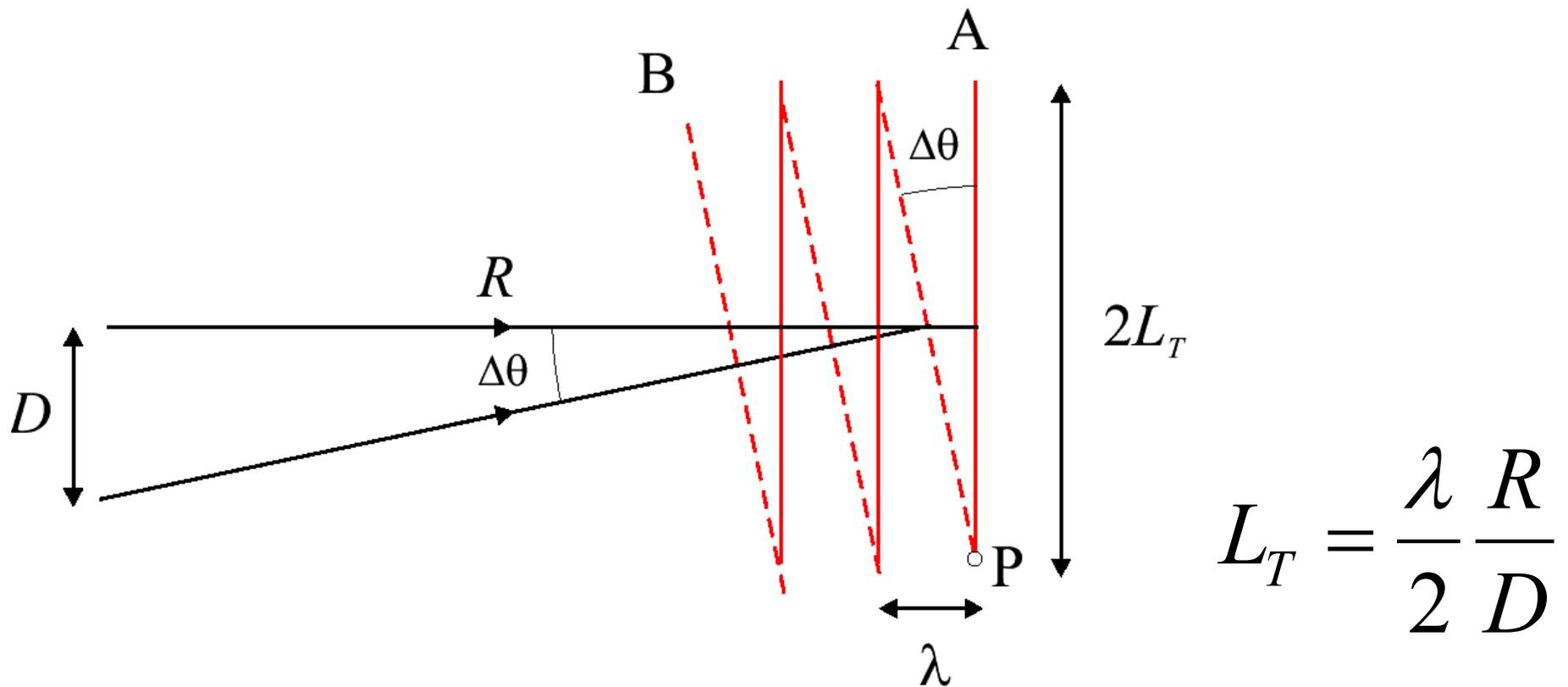
Longitudinal Coherence



$$L_L = \frac{1}{2} \frac{\lambda^2}{\Delta\lambda}$$

Als-Nielsen and McMorro (2001)

Lateral (Transverse) Coherence



$$L_T = \frac{\lambda R}{2 D}$$

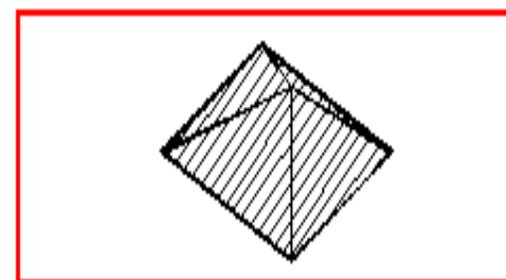
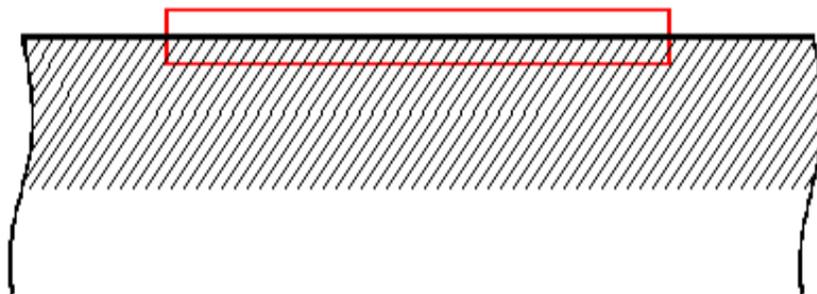
Als-Nielsen and McMorrow (2001)

Coherence at Spring8, APS or ESRF

Typical of 3rd Generation (undulator) Synchrotron Source

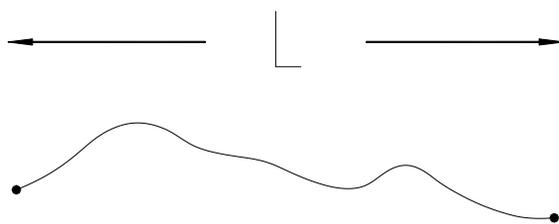
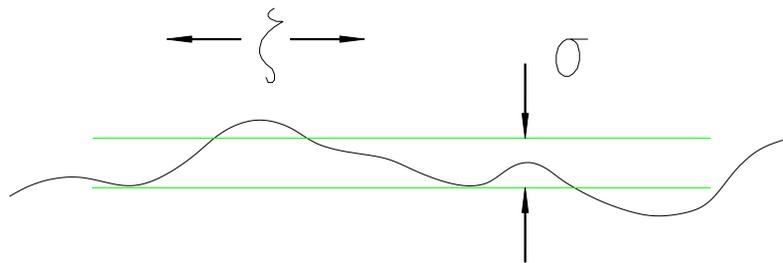
Coherence of	ξ_{VER}	ξ_{HORIZ}	ξ_{LONG}	Flux
Raw Undulator	35 μm	9 μm	0.004 μm	2×10^{12}
Si(111) Monochromator	35 μm	9 μm	1 μm	1×10^{10}
C(111) Monochromator	35 μm	9 μm	3 μm	3×10^9

Coherent region defined by slits

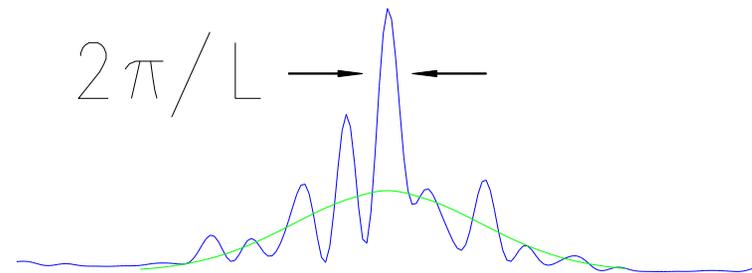
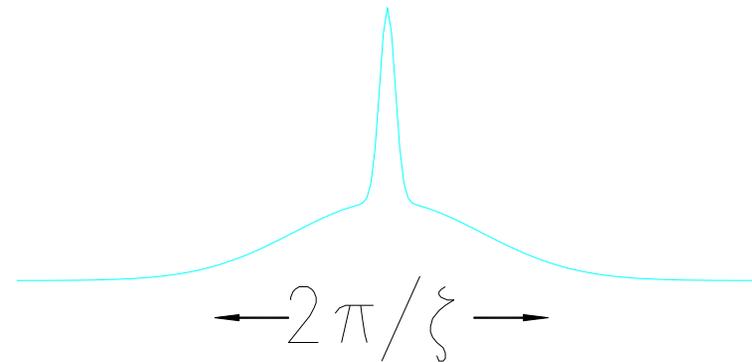


Diffuse Scattering acquires Structure using CXD

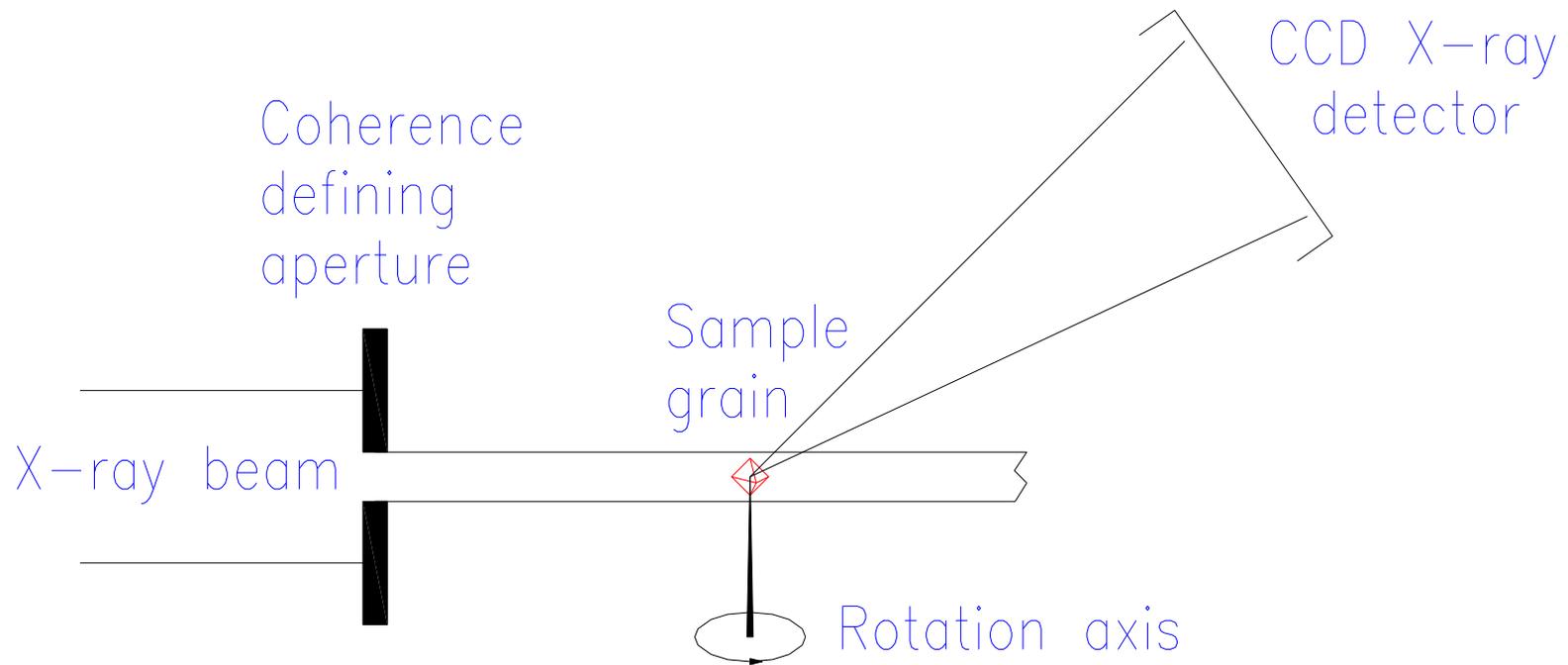
Real Space

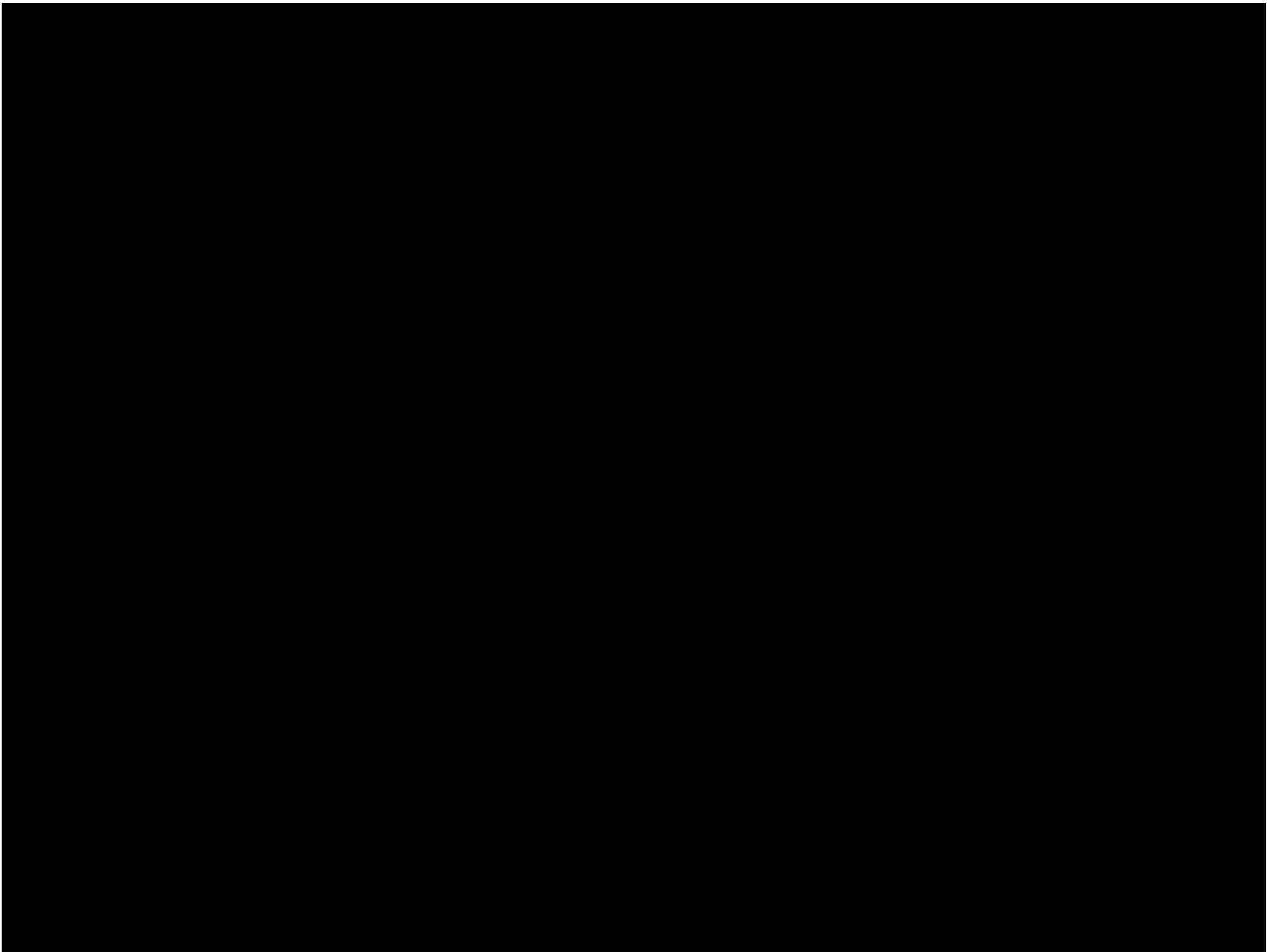


Reciprocal Space

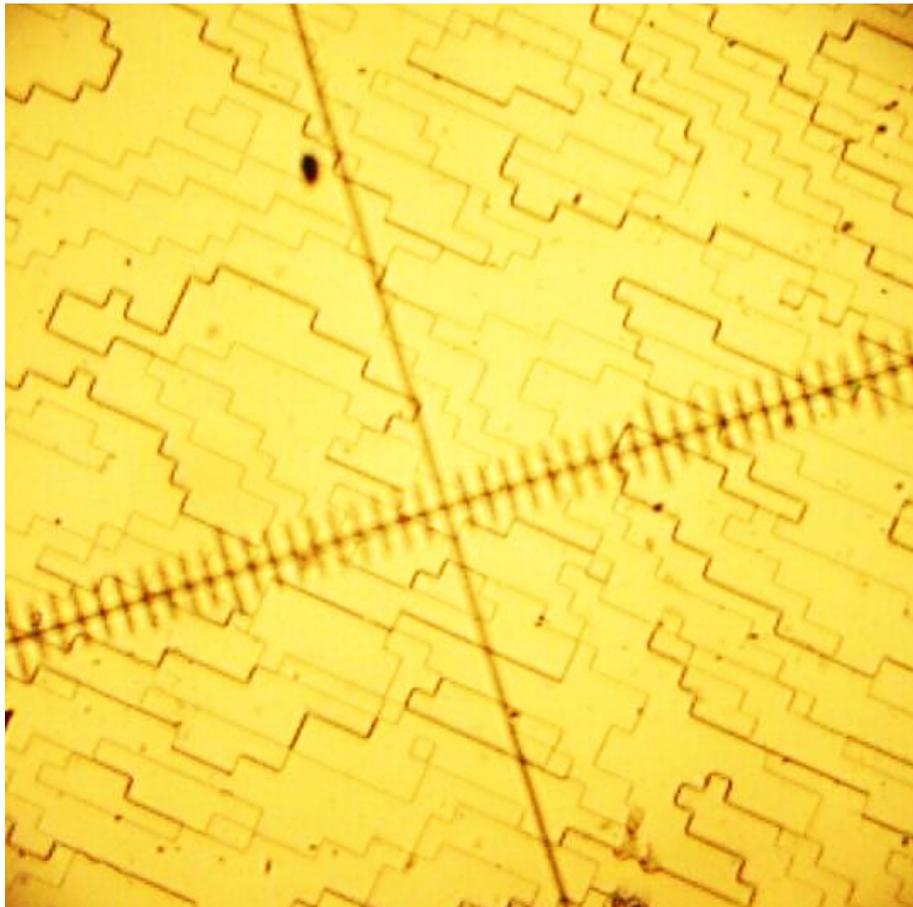


Lensless X-ray Microscope

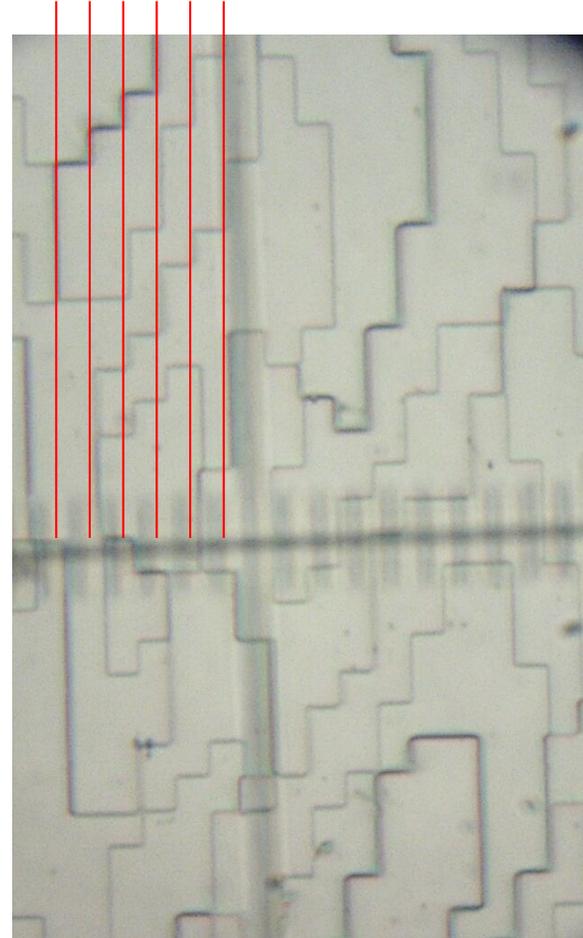




Microscope Images of Gratings



5 μ m grid lines

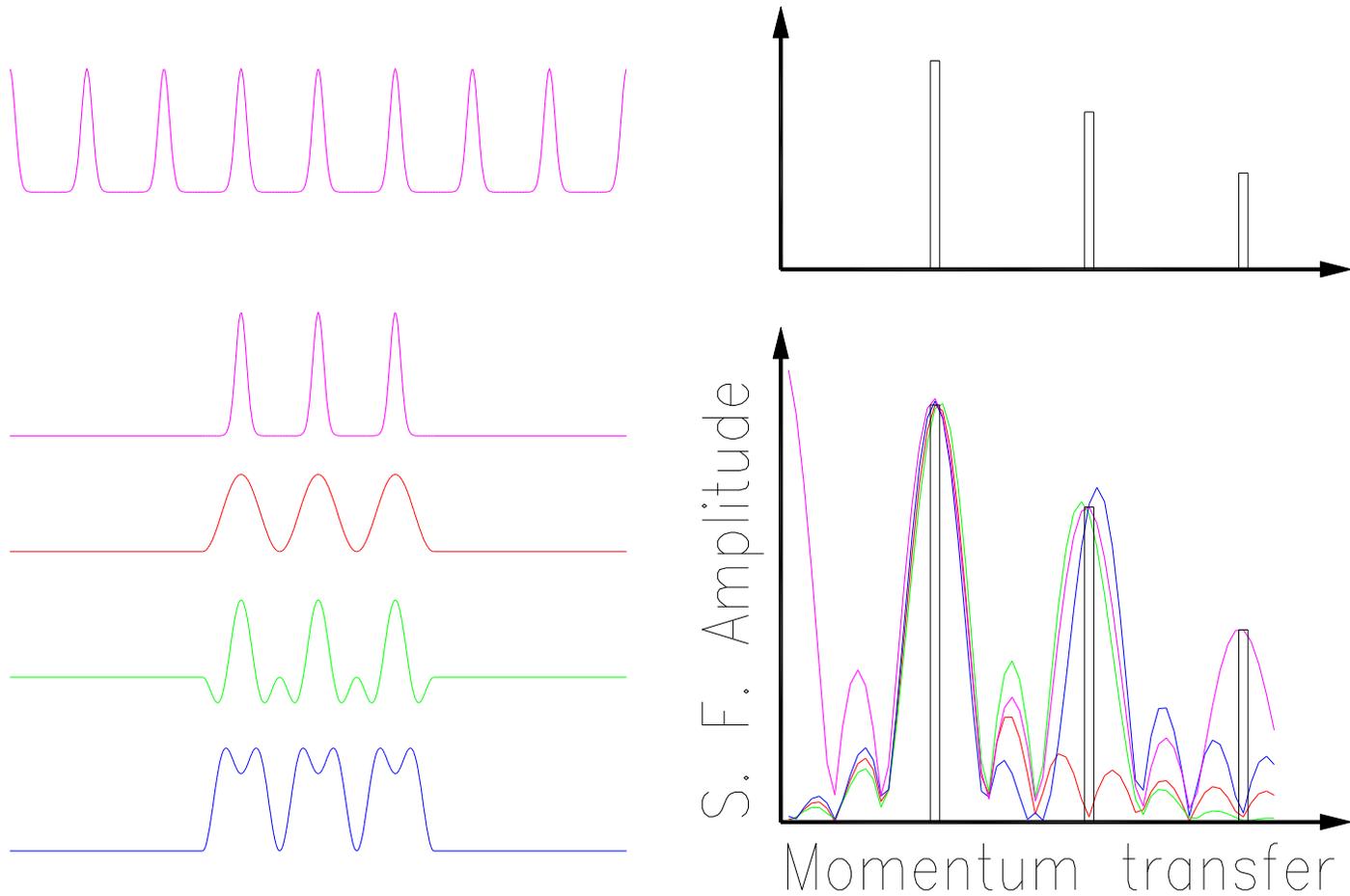


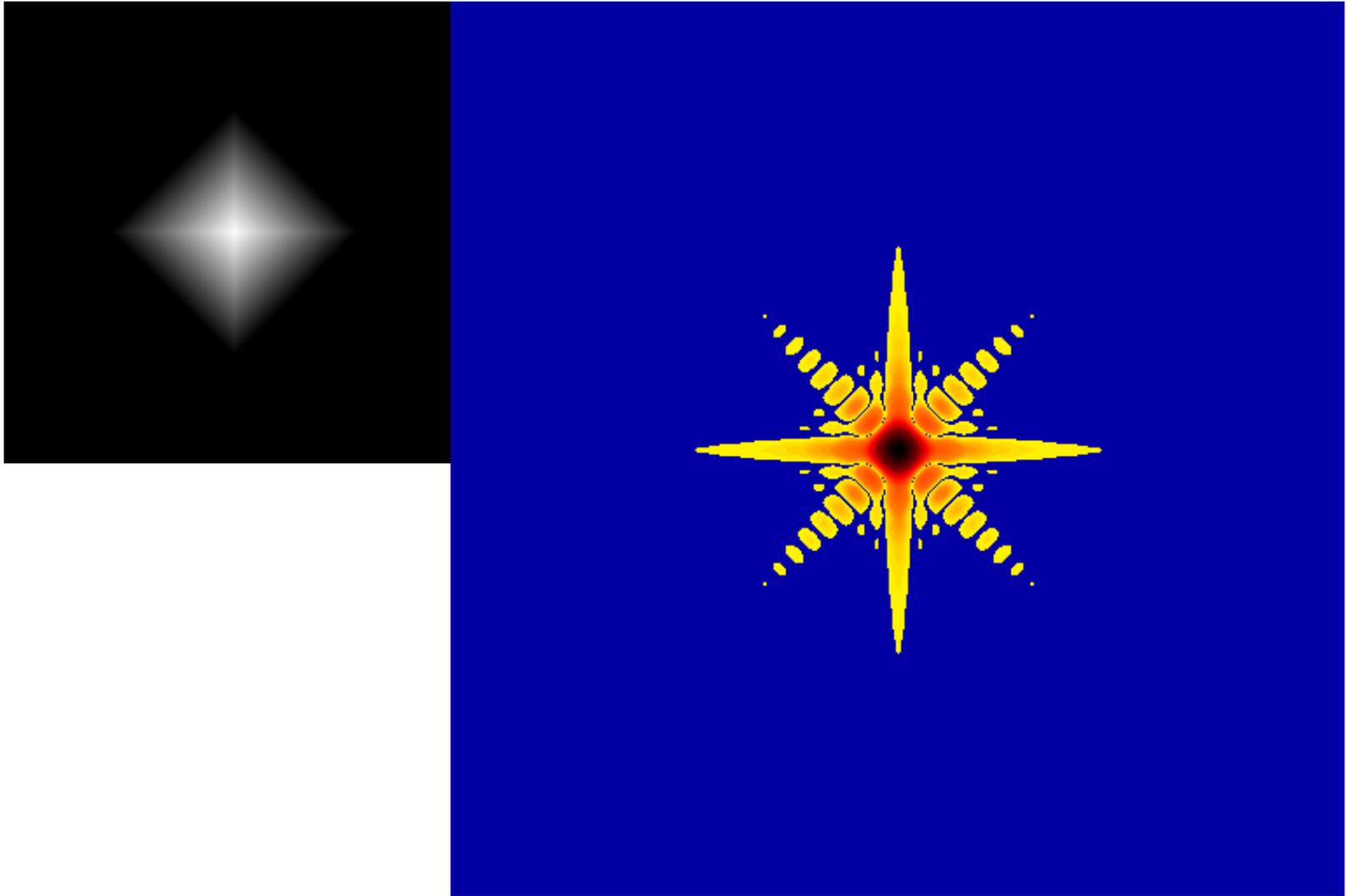
Real-space Constraints in Crystallography

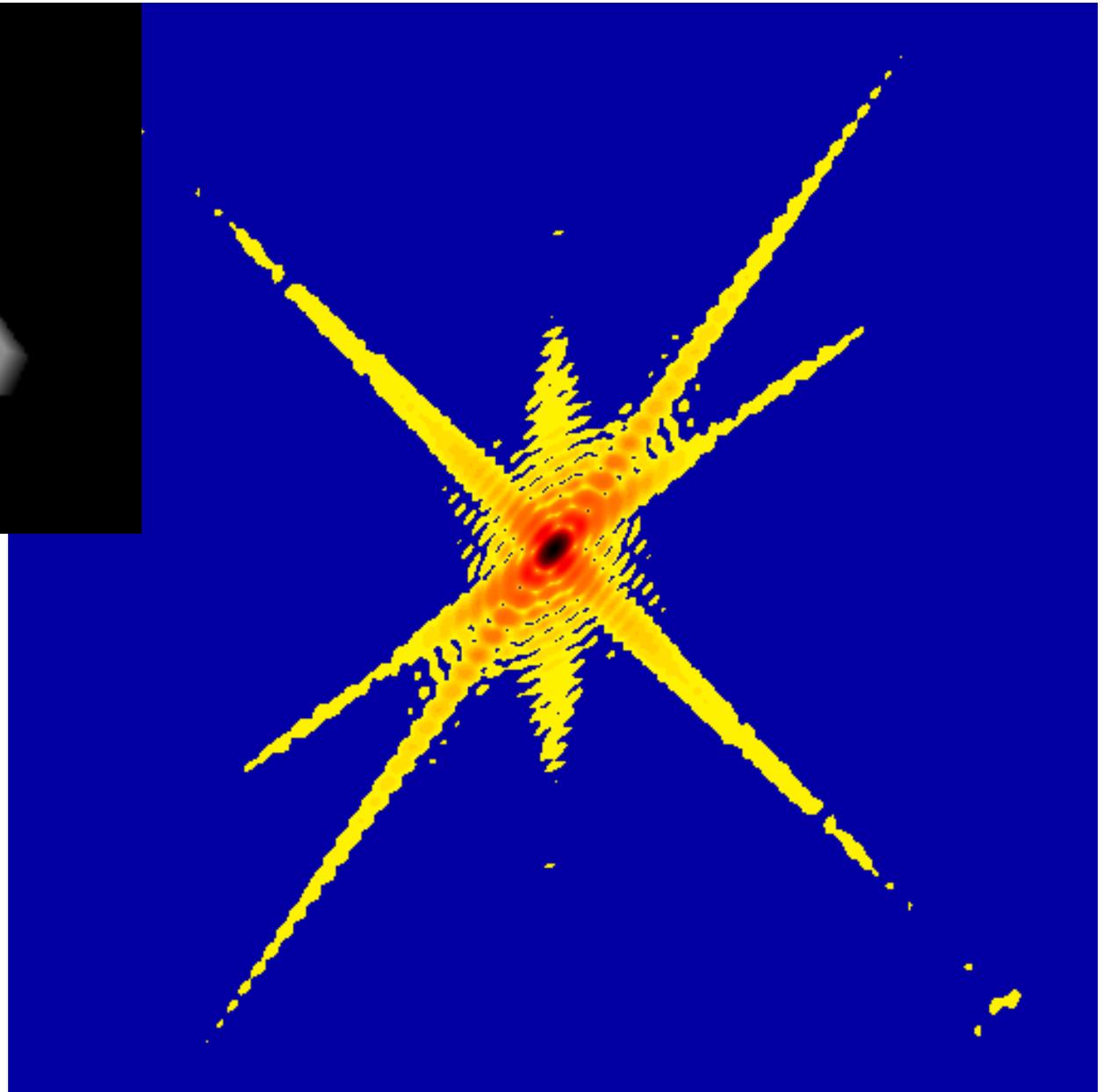
R. P. Millane, J. Opt. Soc Am. A **13** 725 (1996)

- ‘Positivity’ and ‘Atomicity’ constraints (Sayre)
- Finite **support**, molecular envelope
- Solvent flattening/Molecular replacement
- Non-crystallographic symmetry
- Non-uniqueness is ‘pathologically rare’ ($d > 1$)
- Uses memory to avoid stagnation (Fienup HIO)

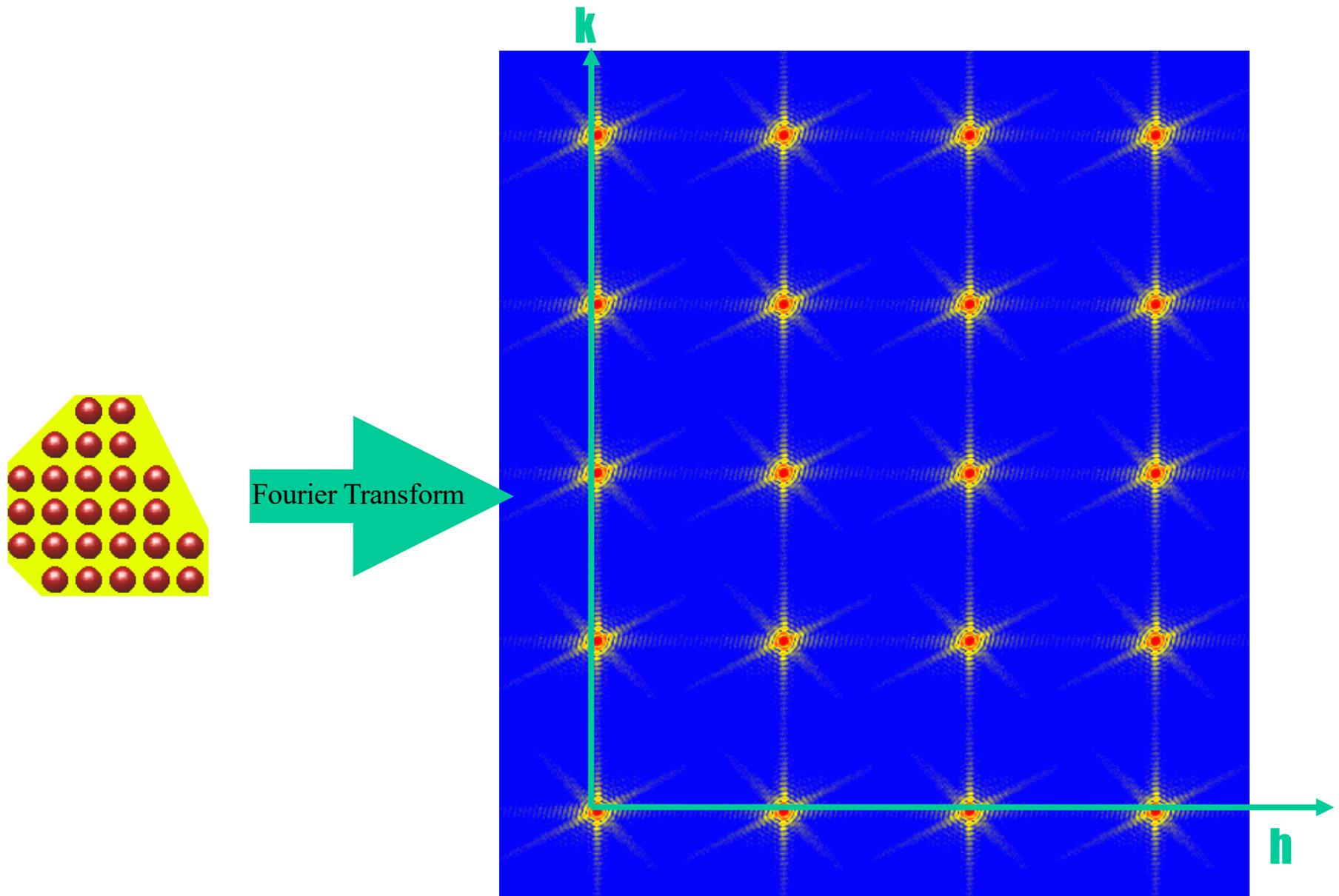
Phase Problem: Finite-size Effect





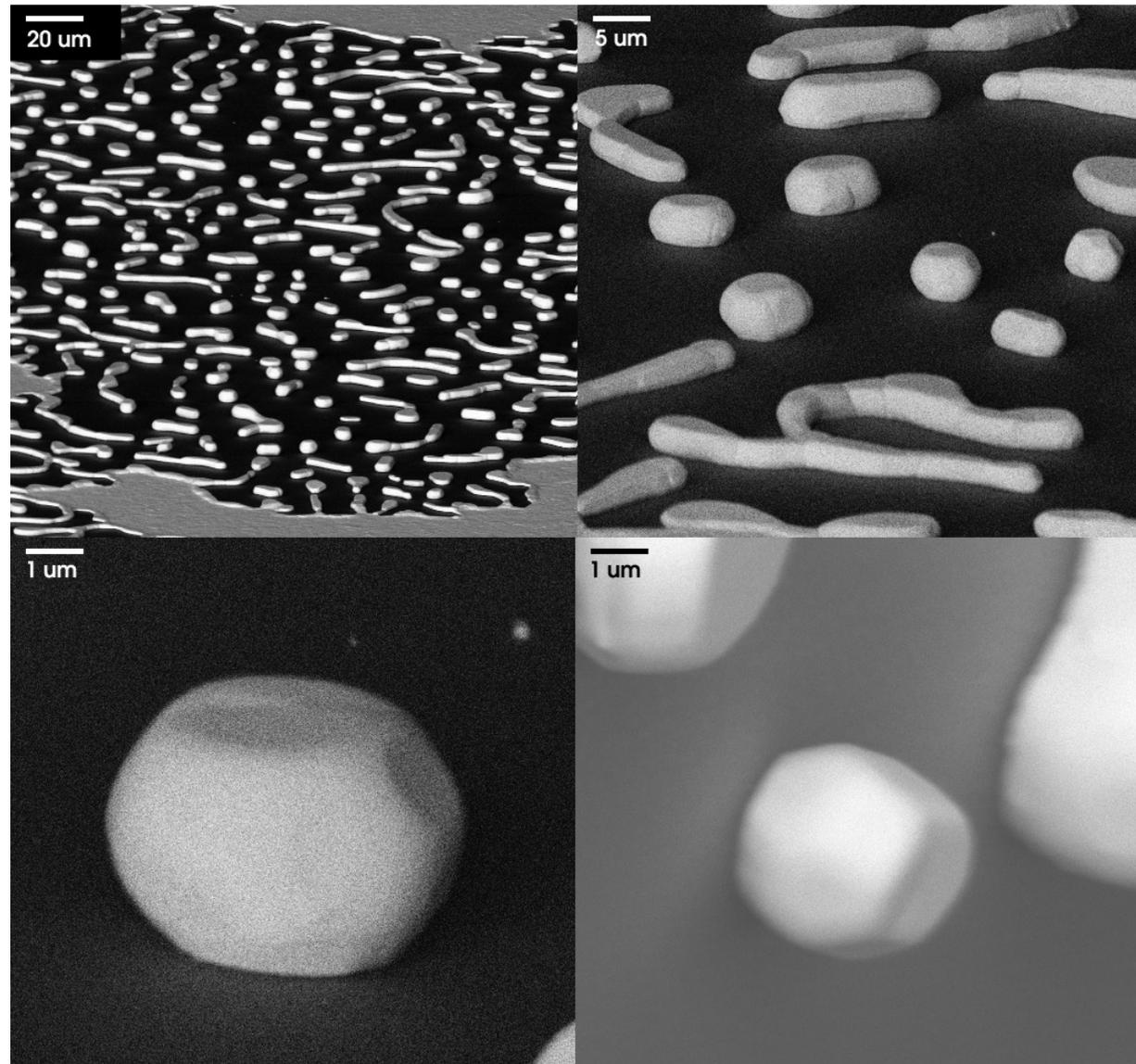


Coherent Diffraction from Crystals



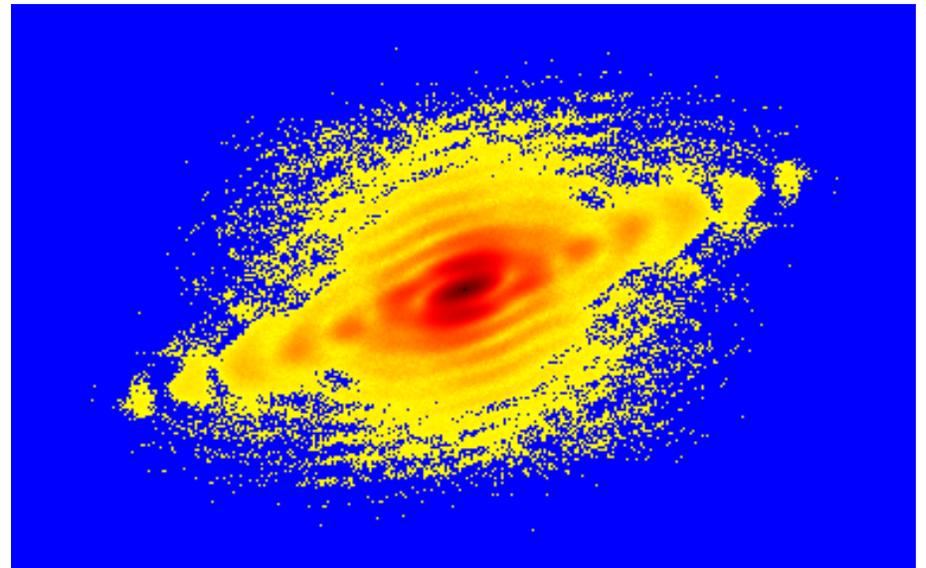
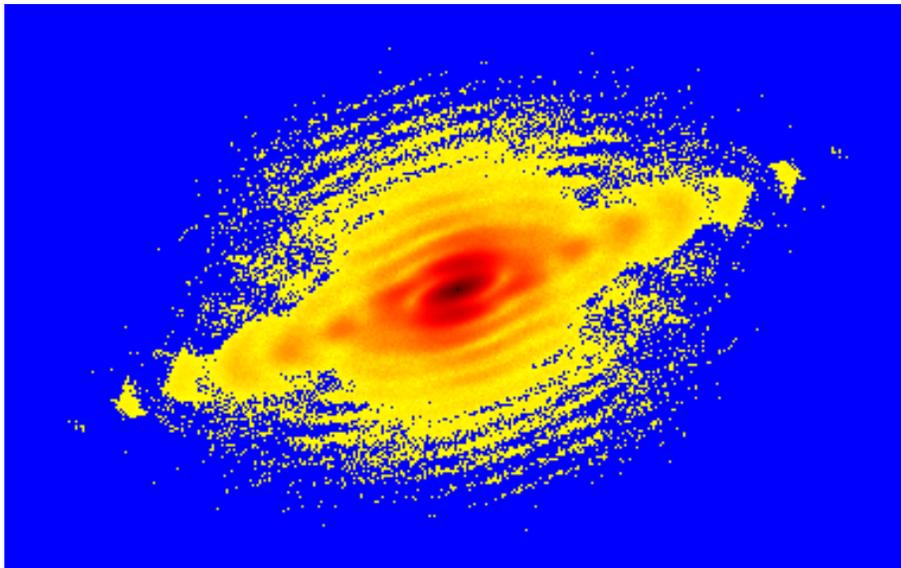
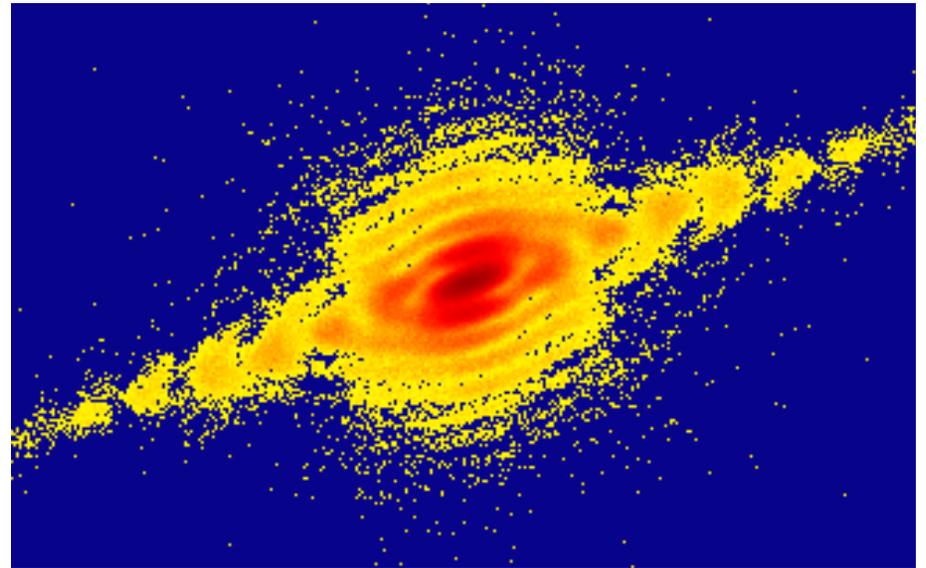
SEMS

- Au blanket film
- Quartz substrate
- Annealed at 950°C for 70 hrs.



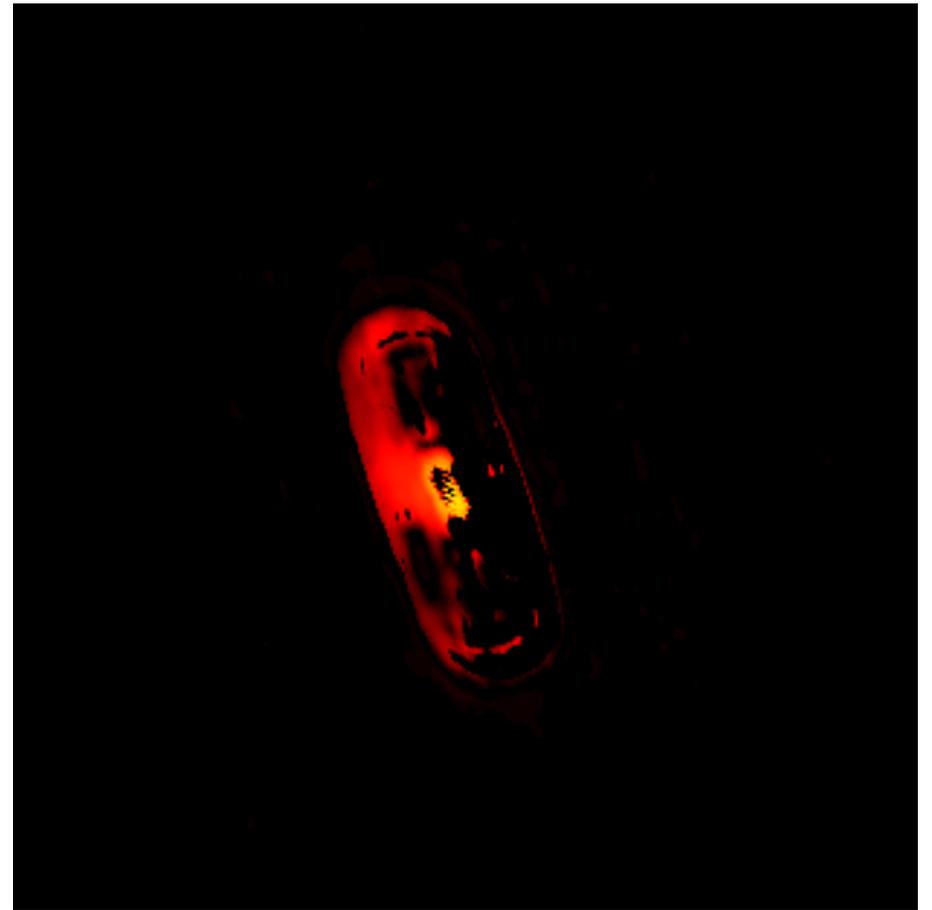
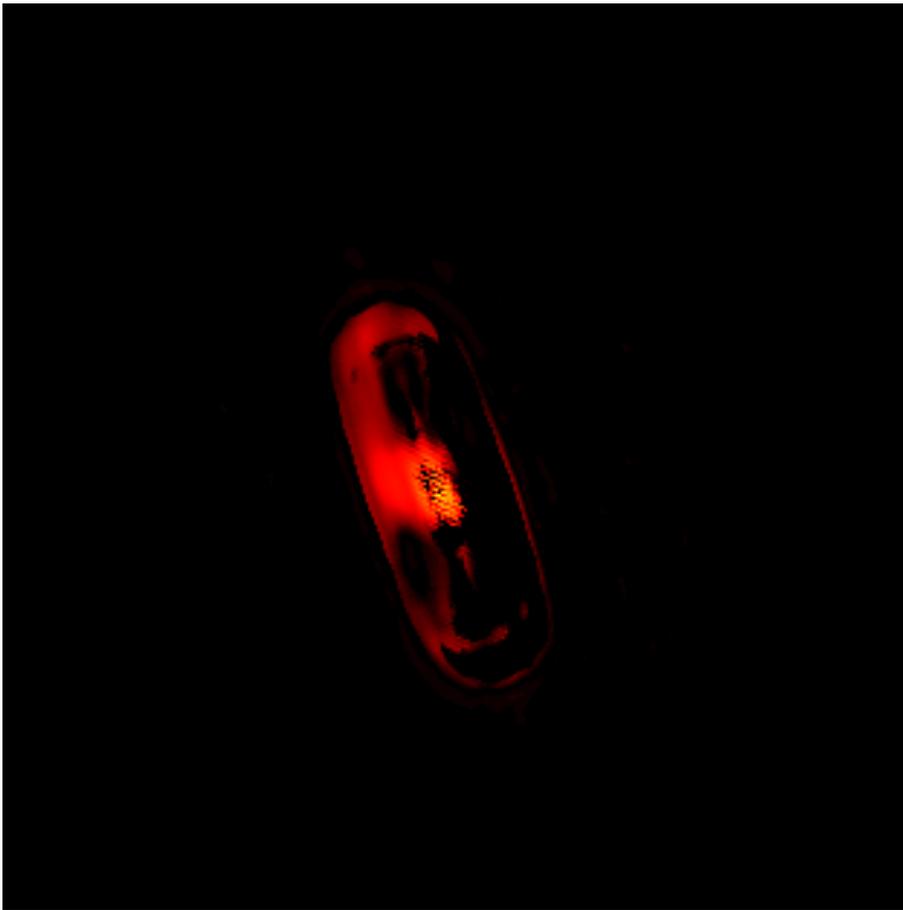
Symmetrized Data and two best fits

Chisq=0.0005

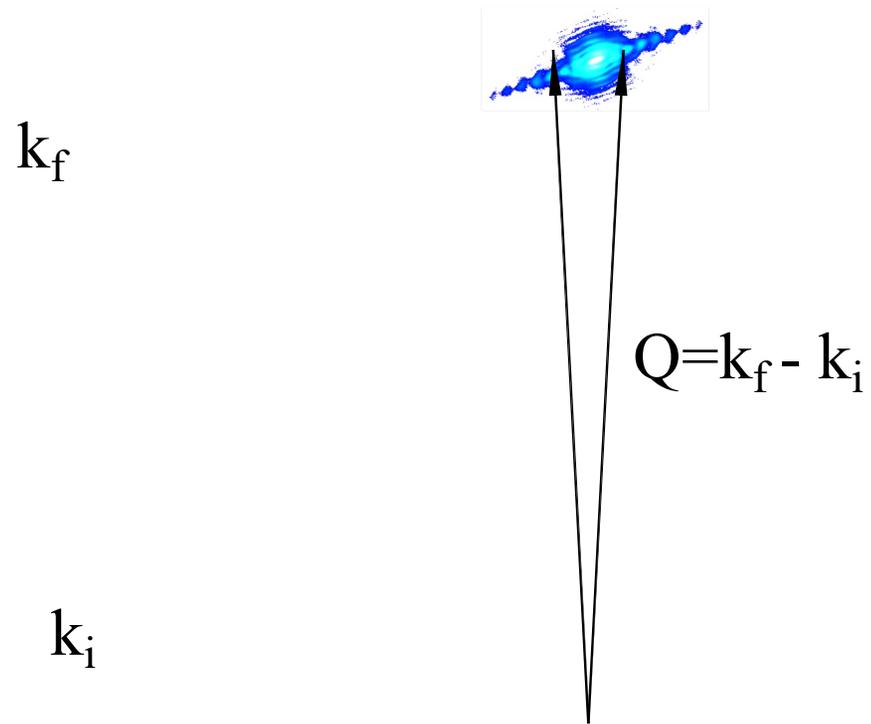


2D Reconstructions

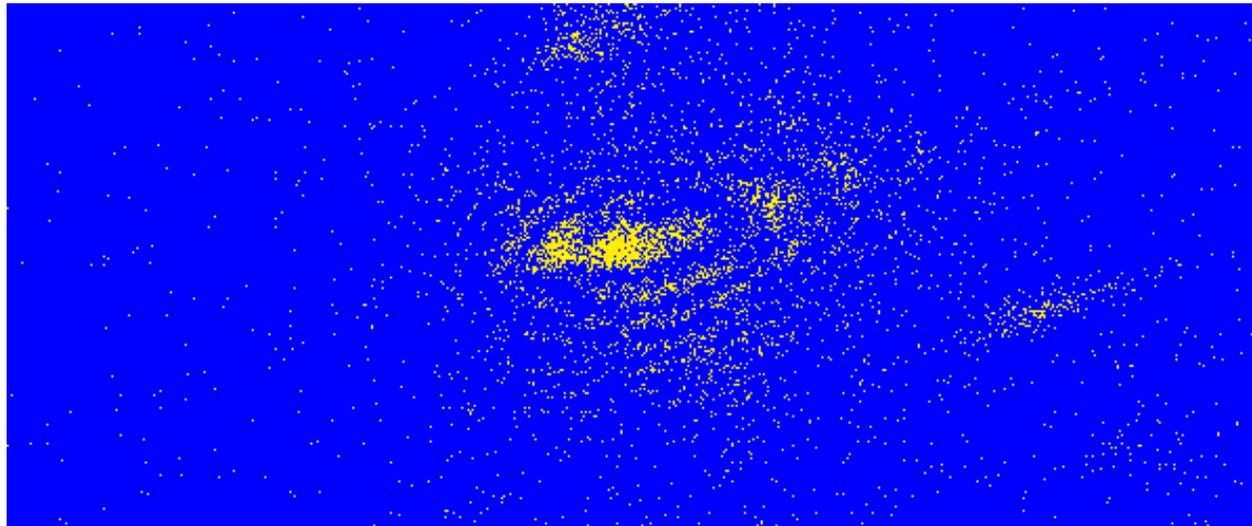
chisquare = 0.0005



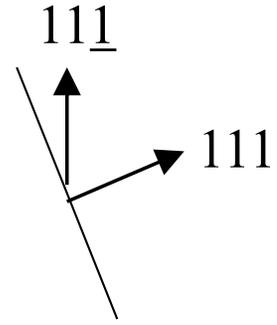
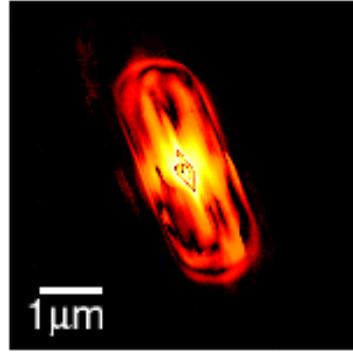
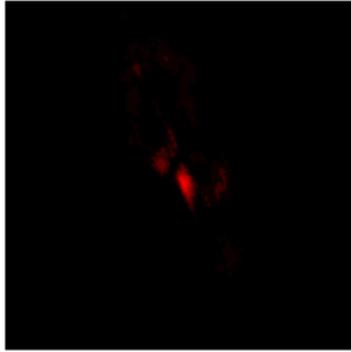
3D Diffraction Method



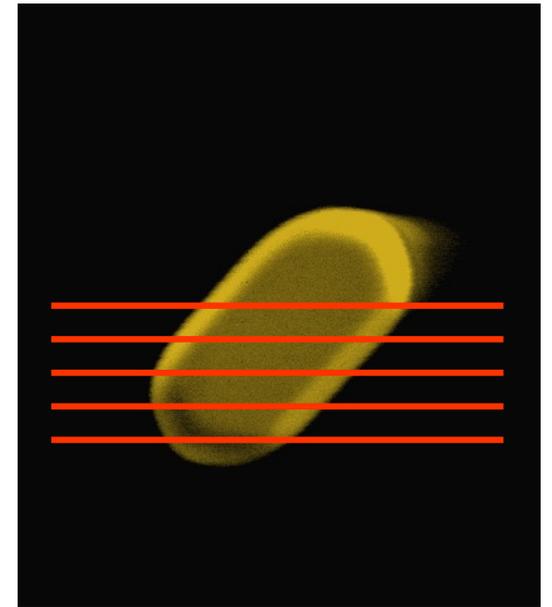
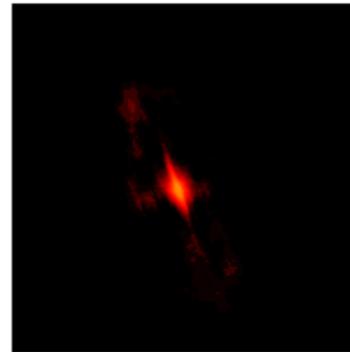
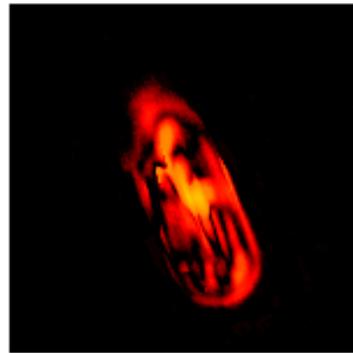
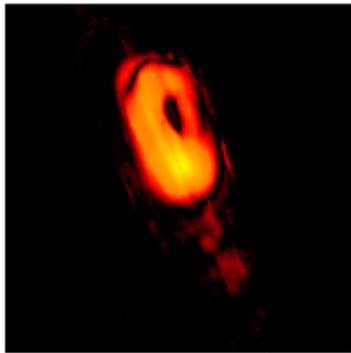
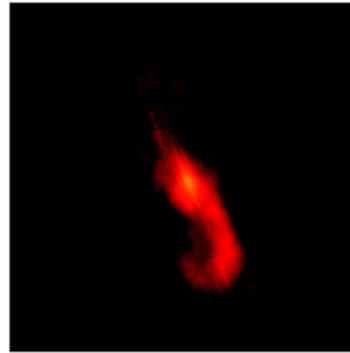
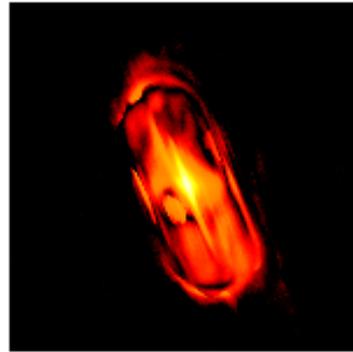
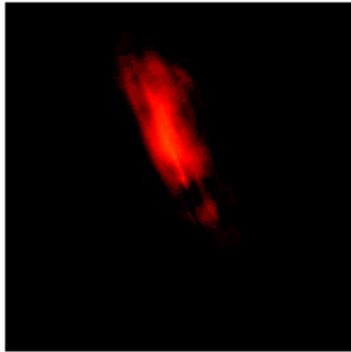
3D Diffraction Data 1 micron Au crystal



* Center is Symmetric *

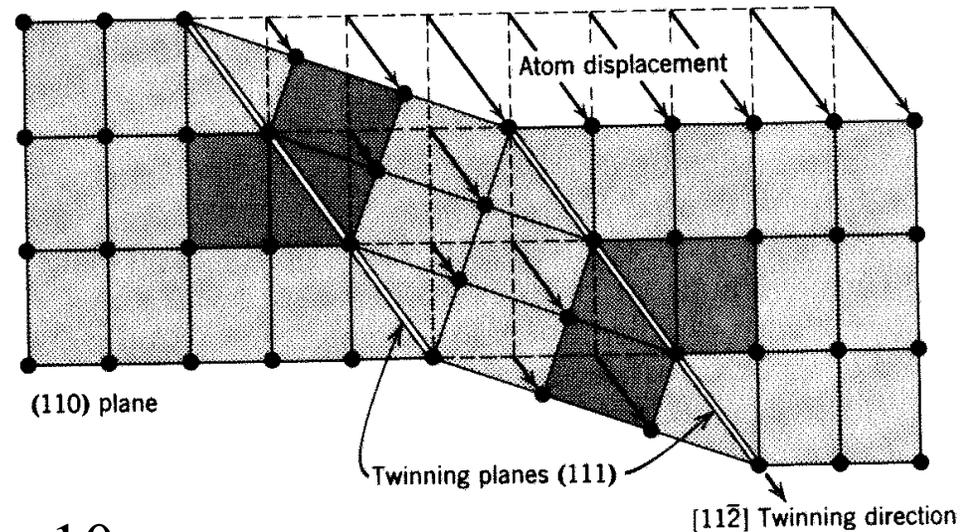


Slices through
plan view SEM:



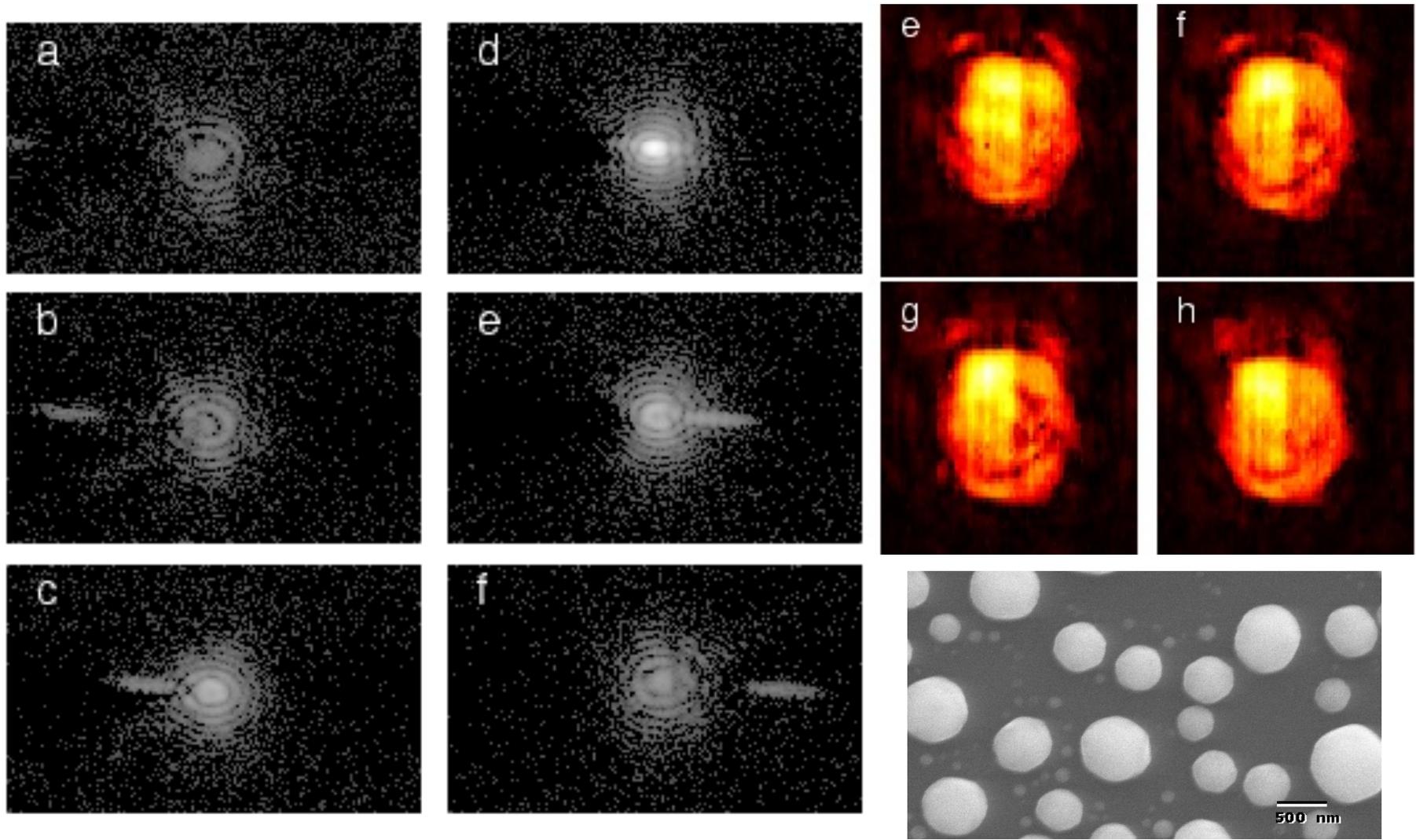
Twinning in deformed FCC metals

J. Wulff, "Structure and Property of Materials III" (1965)

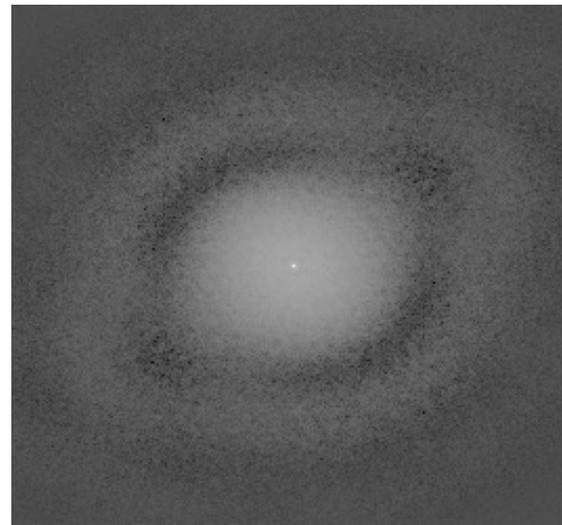
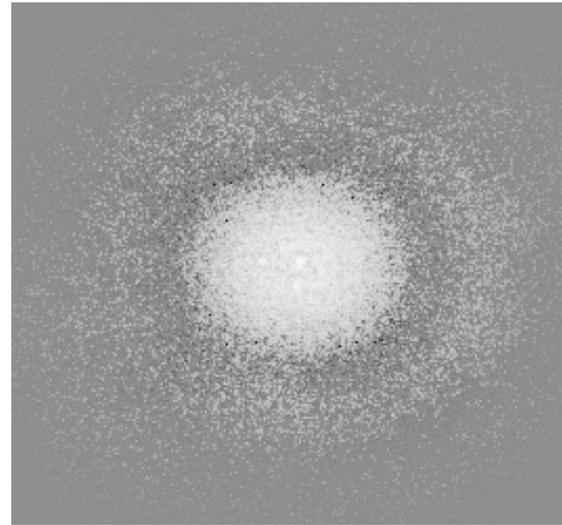
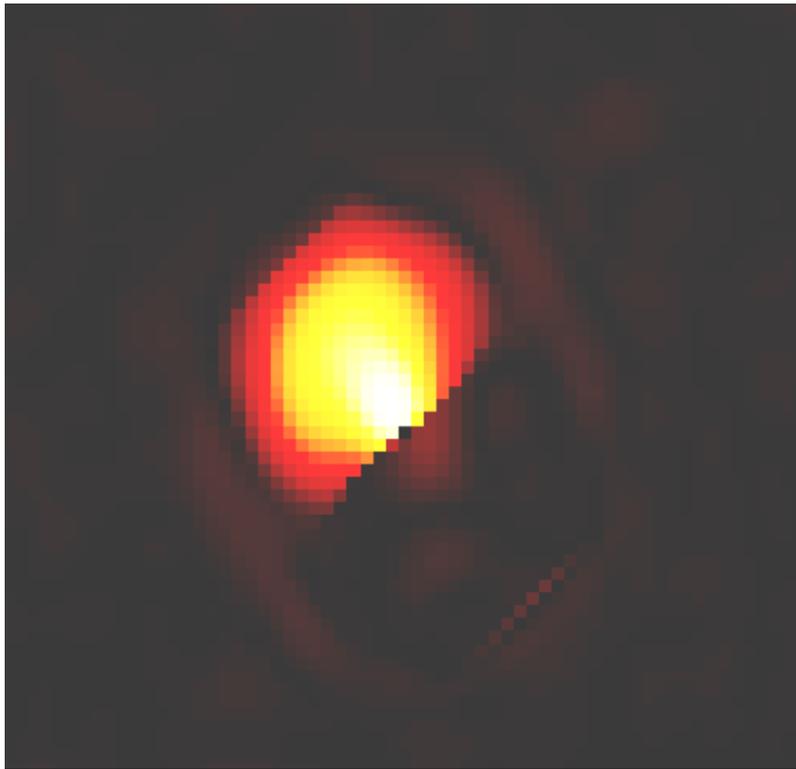


■ $\sim 10\mu\text{m}$
Cu

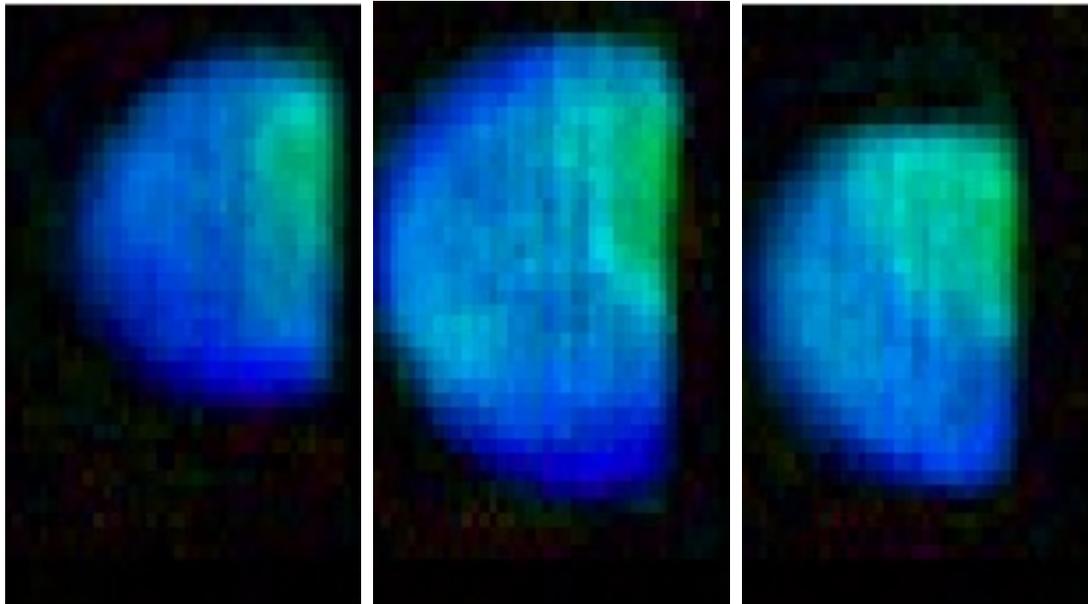
3D reconstruction of Pb nanocrystals



Reconstruction of Pb Nanocrystal



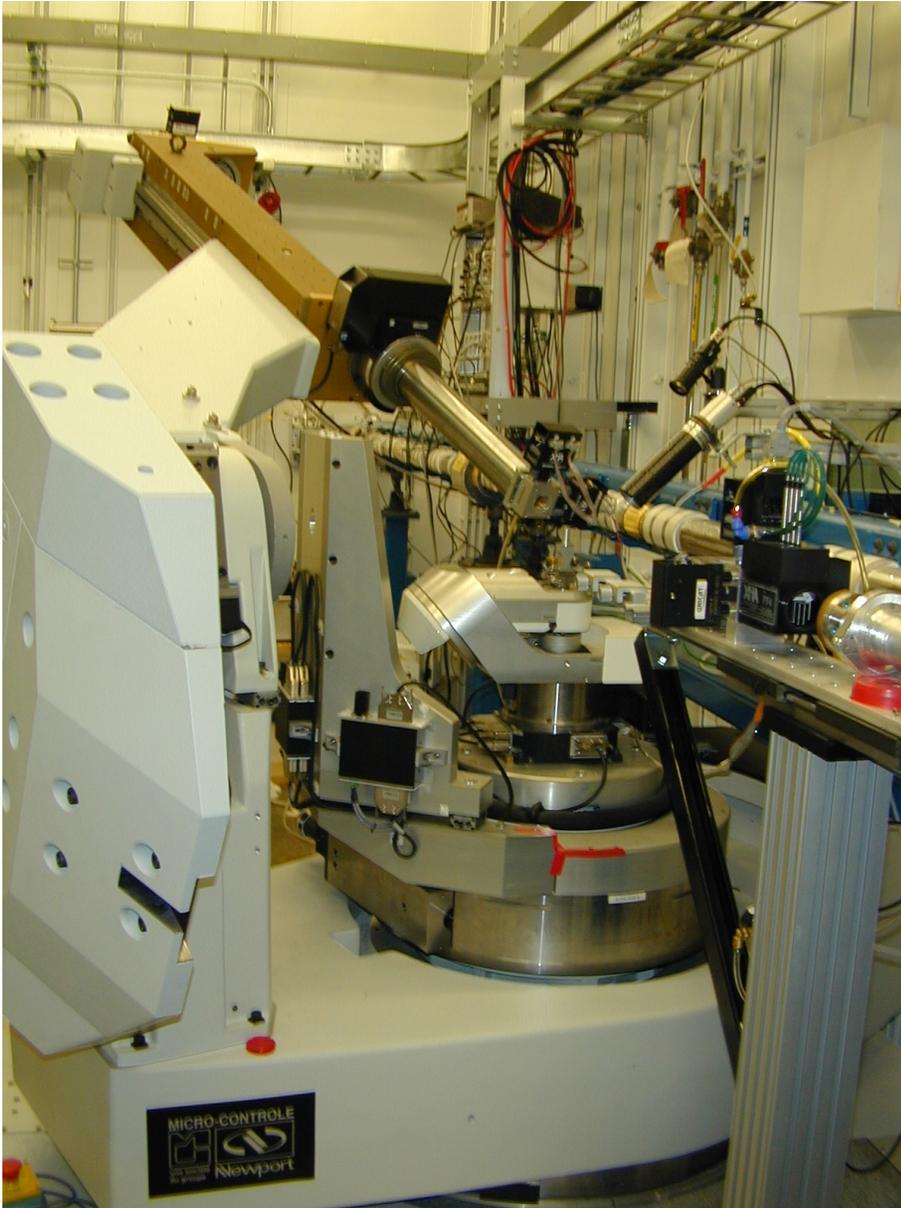
3D Phase Images of Lead Nanocrystals

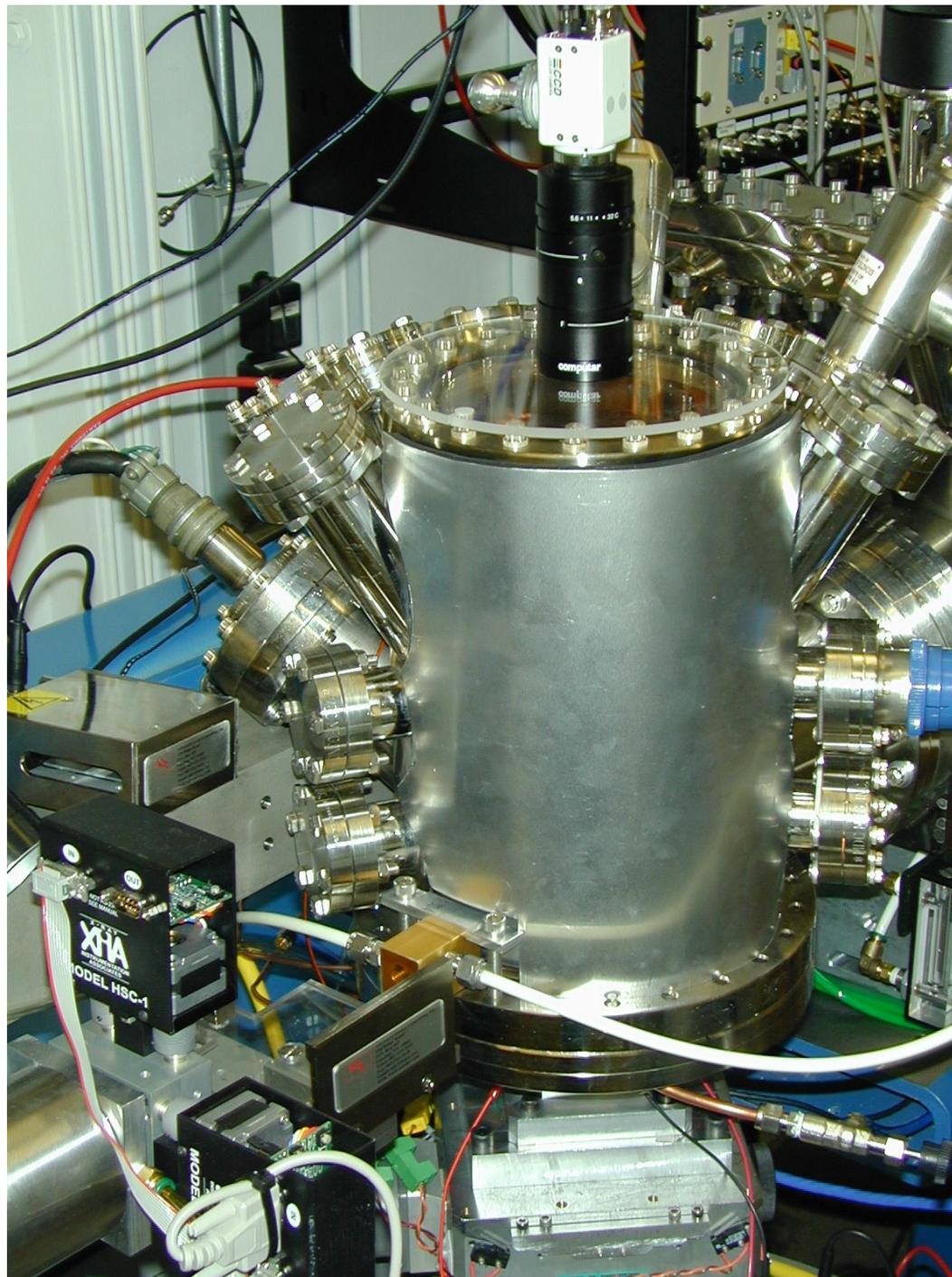


- 500nm Pb crystals grown **in-situ** in UHV system at APS (Argonne) on a SiO_2 support (vertical).

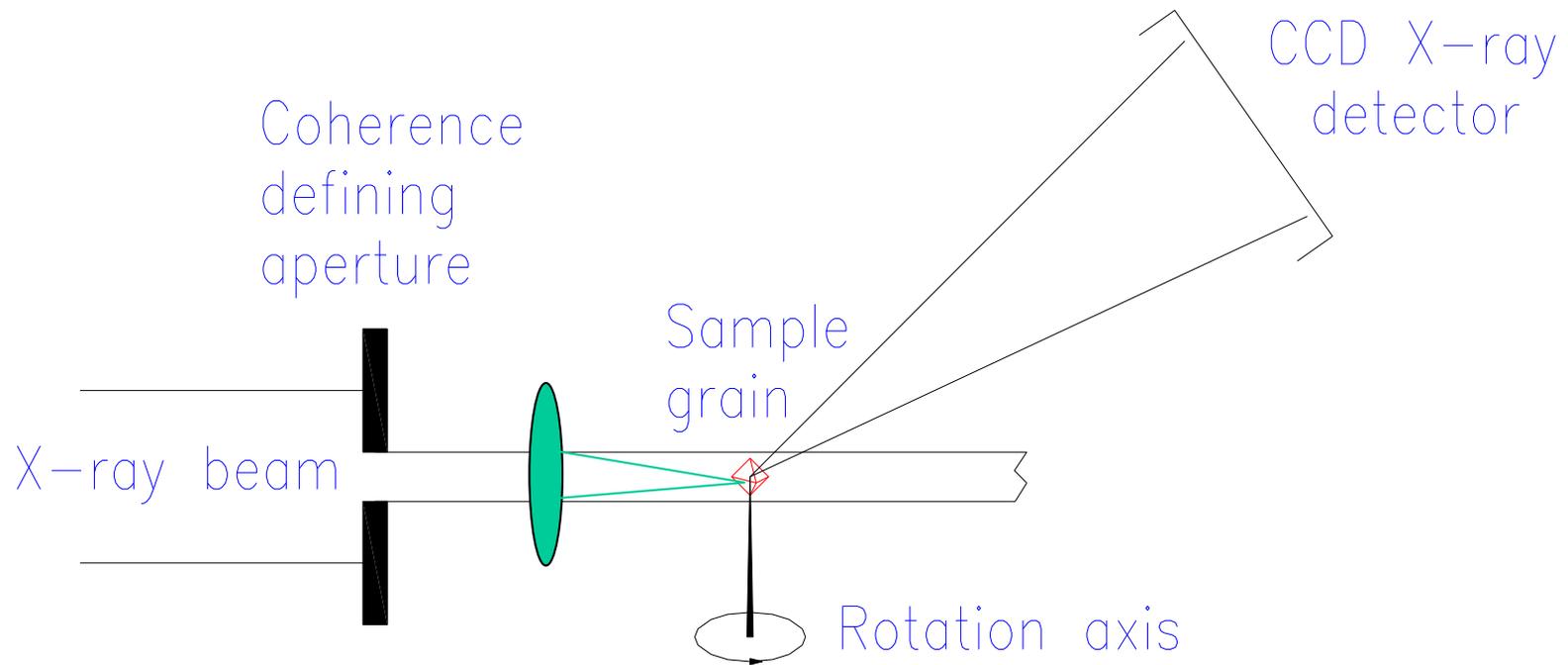
- 3D coherent X-ray diffraction data is inverted into hemi-spherical cross-sectional slices.

- These images are colored according to the **phase** of the density, which changes abruptly at an internal boundary.
- This plane is identified as a single **deformation fault** in the crystal.

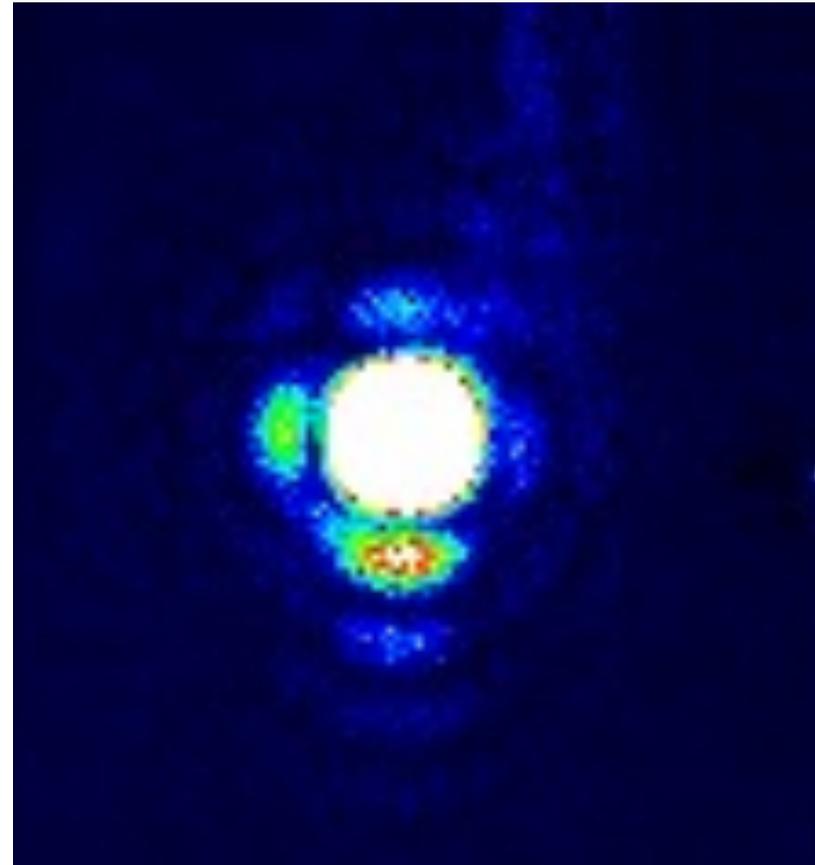
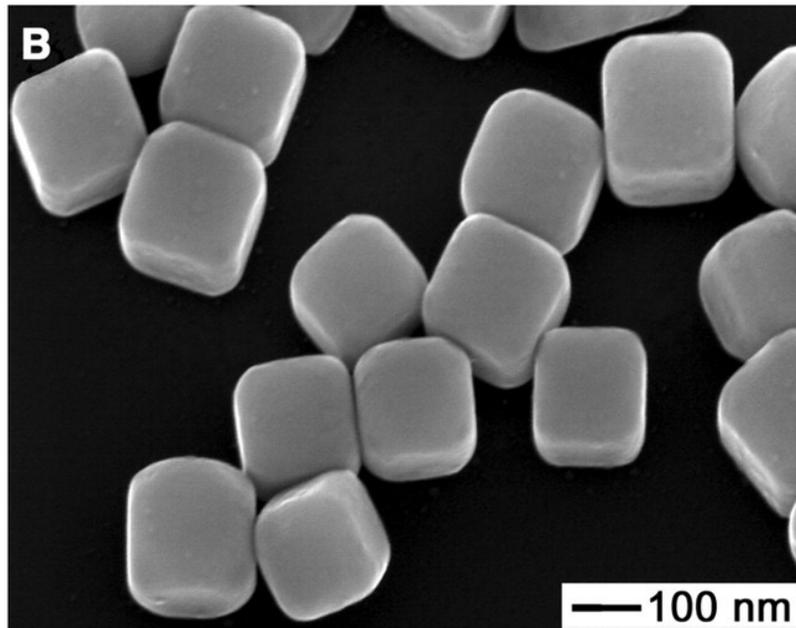




Lensless X-ray Microscope

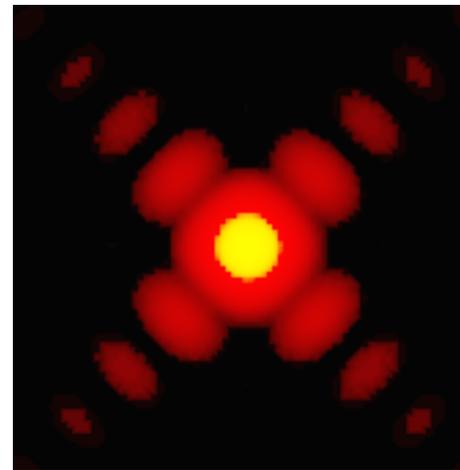
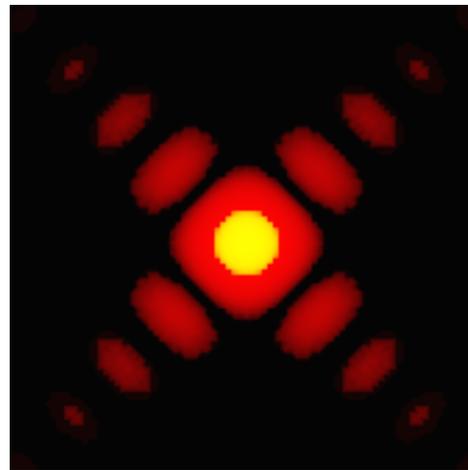


CXD from Silver Nanocubes



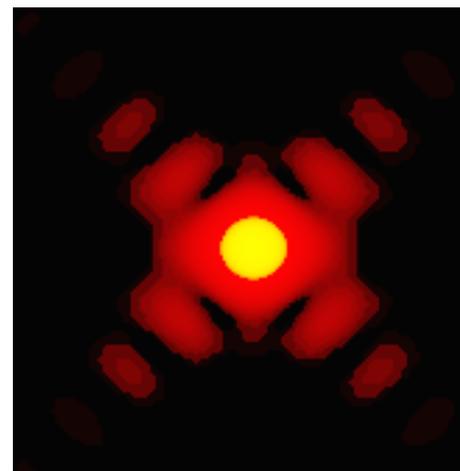
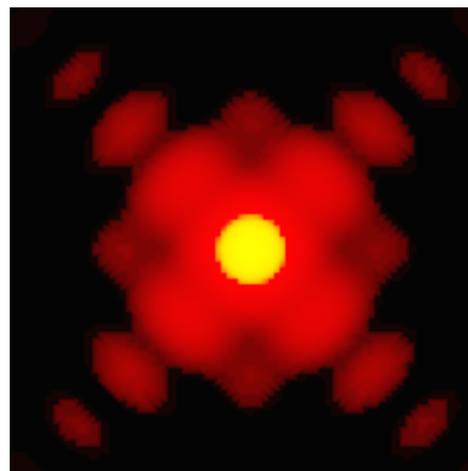
Yugang Sun and Younan Xia,
Science 298 2177 (2003)

Spherical and cylindrical waves



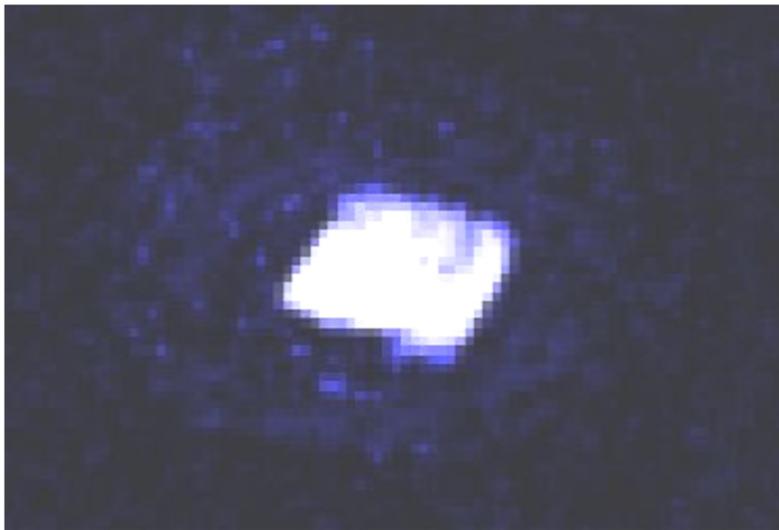
$\pi/4$

$\pi/2$

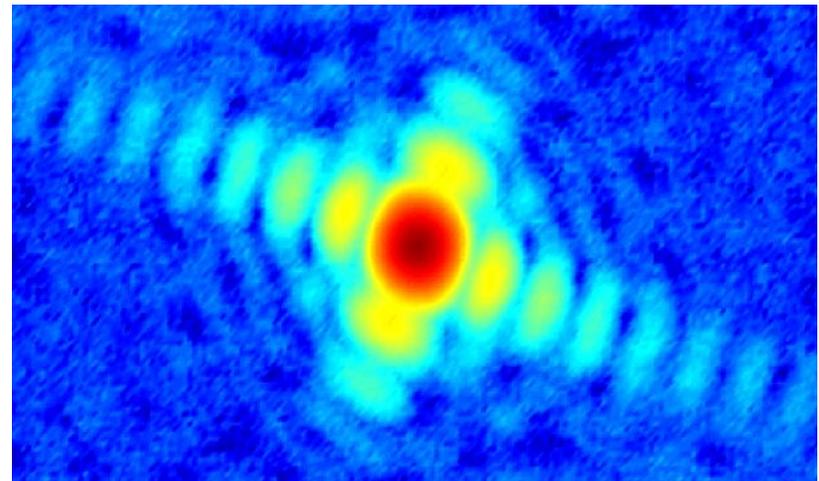
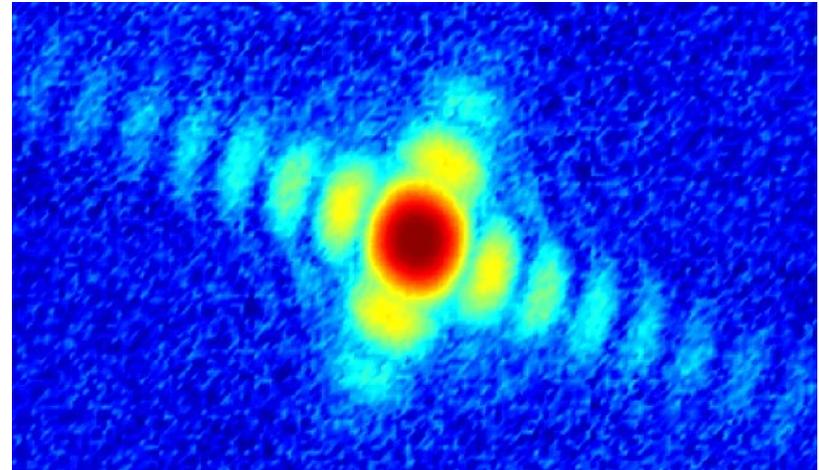


$\pi/4$ (x)

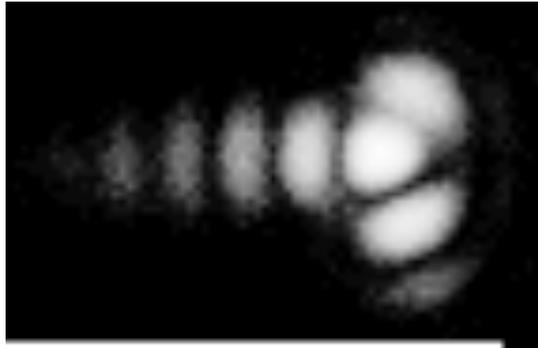
Reconstruction of Ag Nanocrystal



←→
200nm



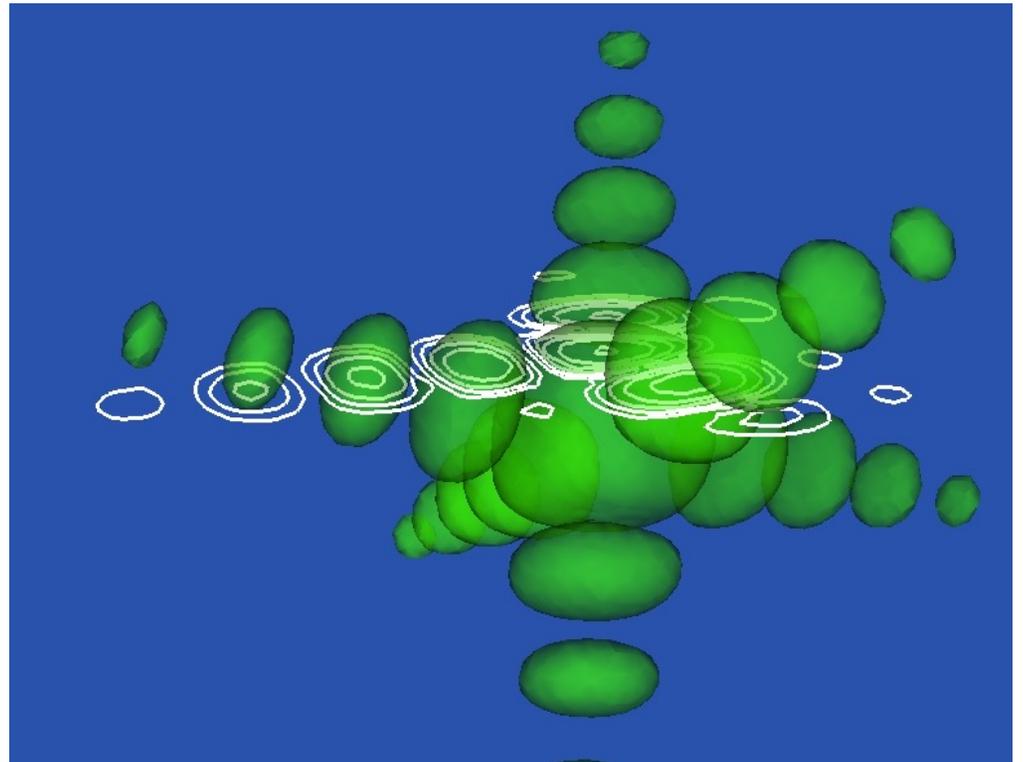
Miscentered Non-Centrosymmetric Reciprocal Space Slice



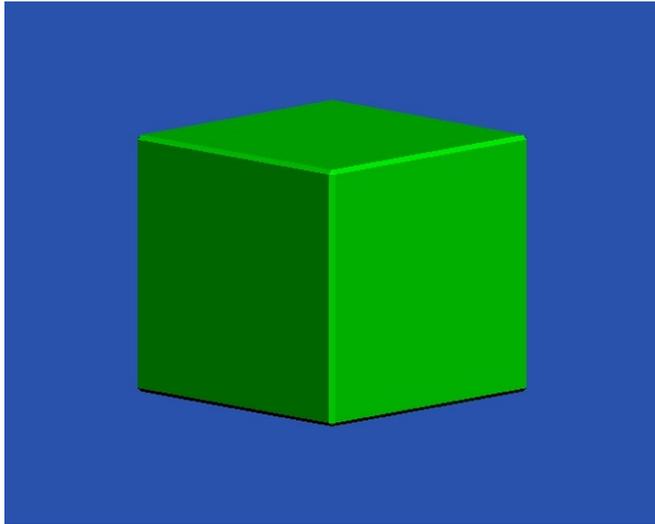
$$A_q \neq A_{\bar{q}}^*$$



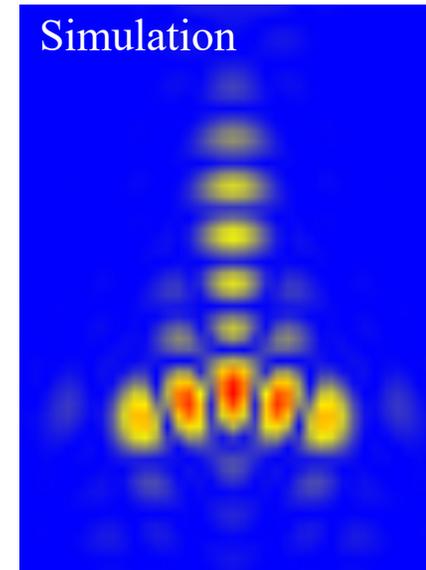
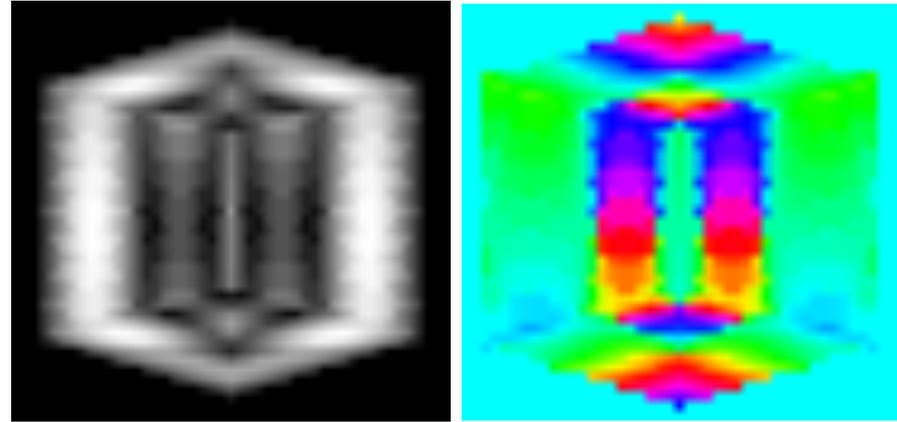
Real-space phase.



What can we expect to see?

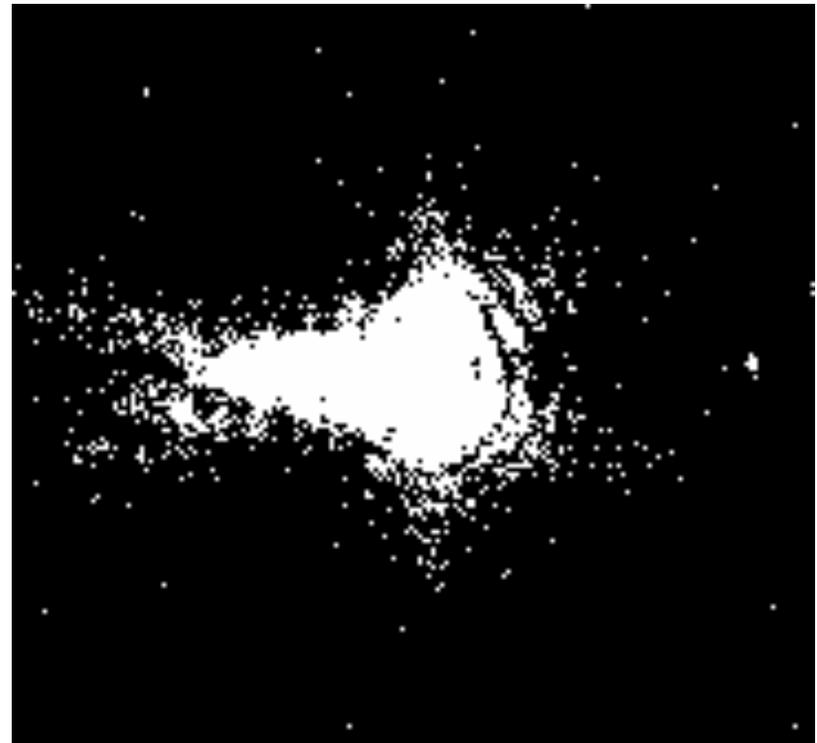
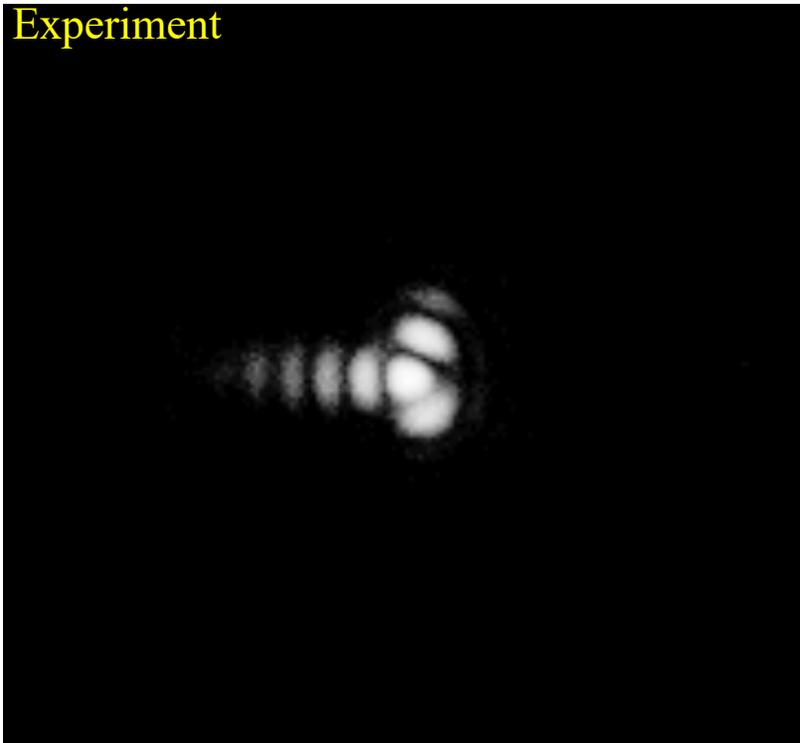


$$A(\bar{q}_o + \bar{q}_z) = \sum_i \underbrace{\sum_z \rho(x, y, z)}_{u_i(x, y)} e^{2\pi i \bar{q}_z \cdot \bar{z}_i} e^{2\pi i (\bar{q}_o) \cdot \bar{r}_i}$$

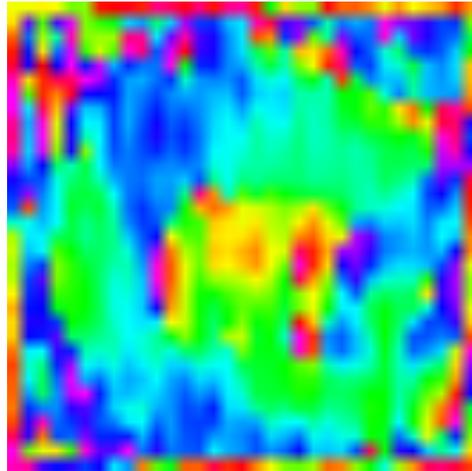
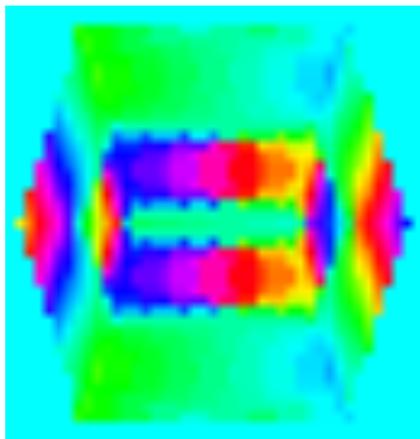
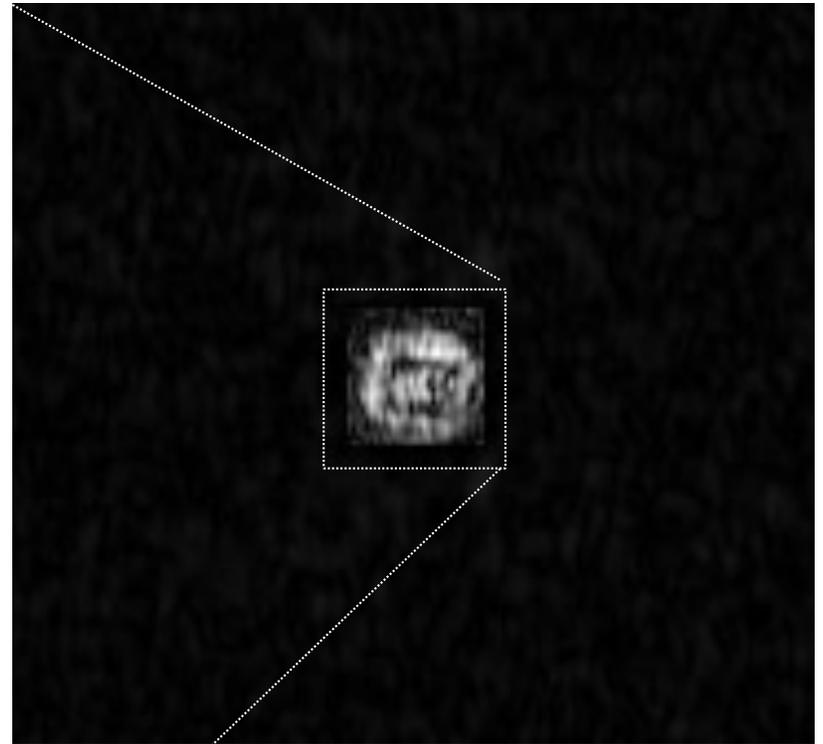
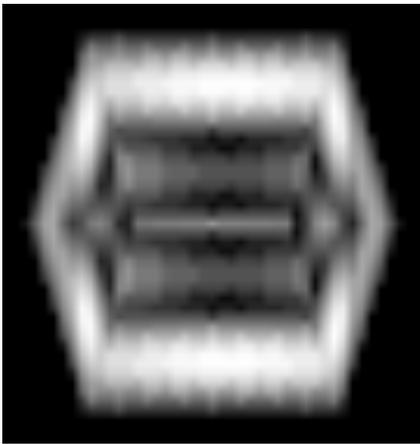


Data and Data Mask ($>7\%$ Max)

Experiment

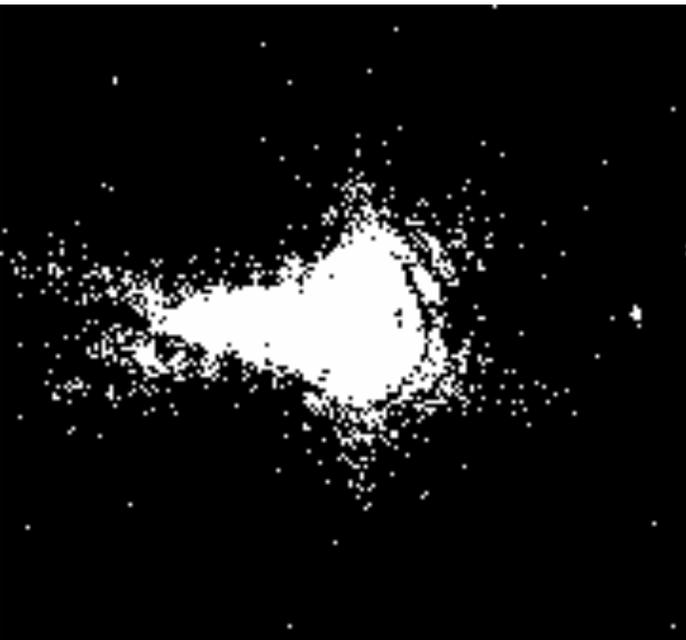
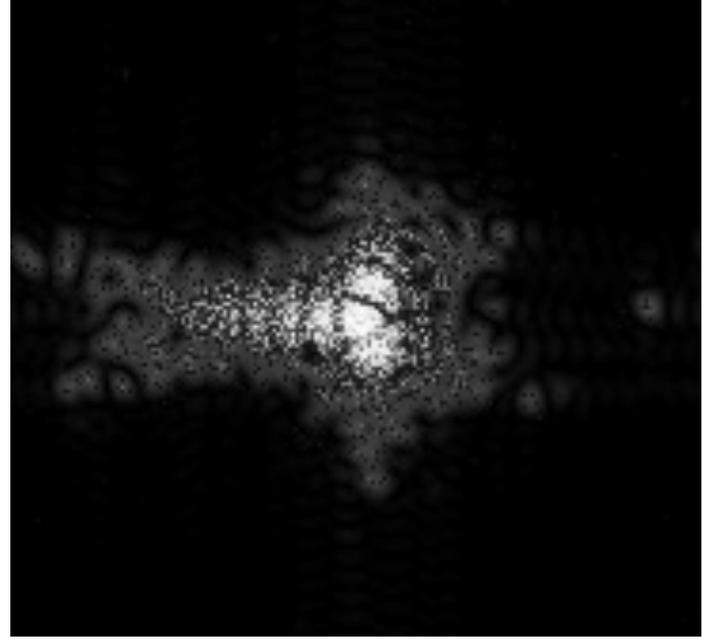
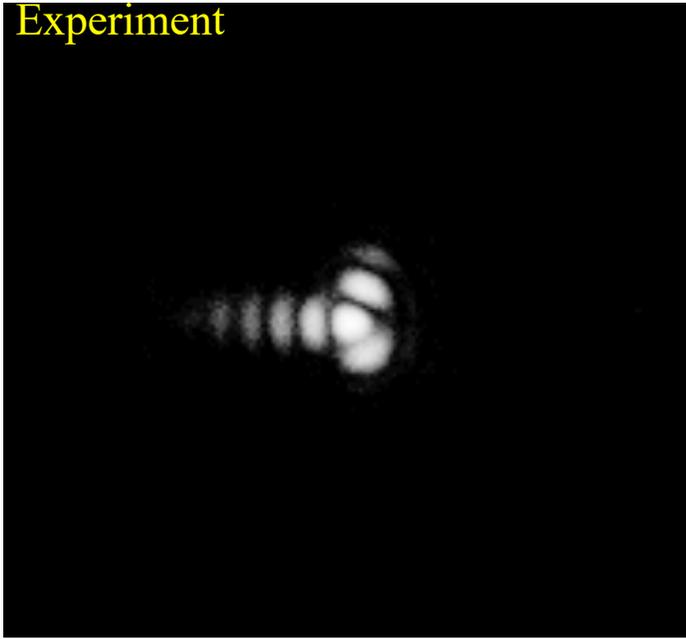


Direct Space Result (1000 Iterations)



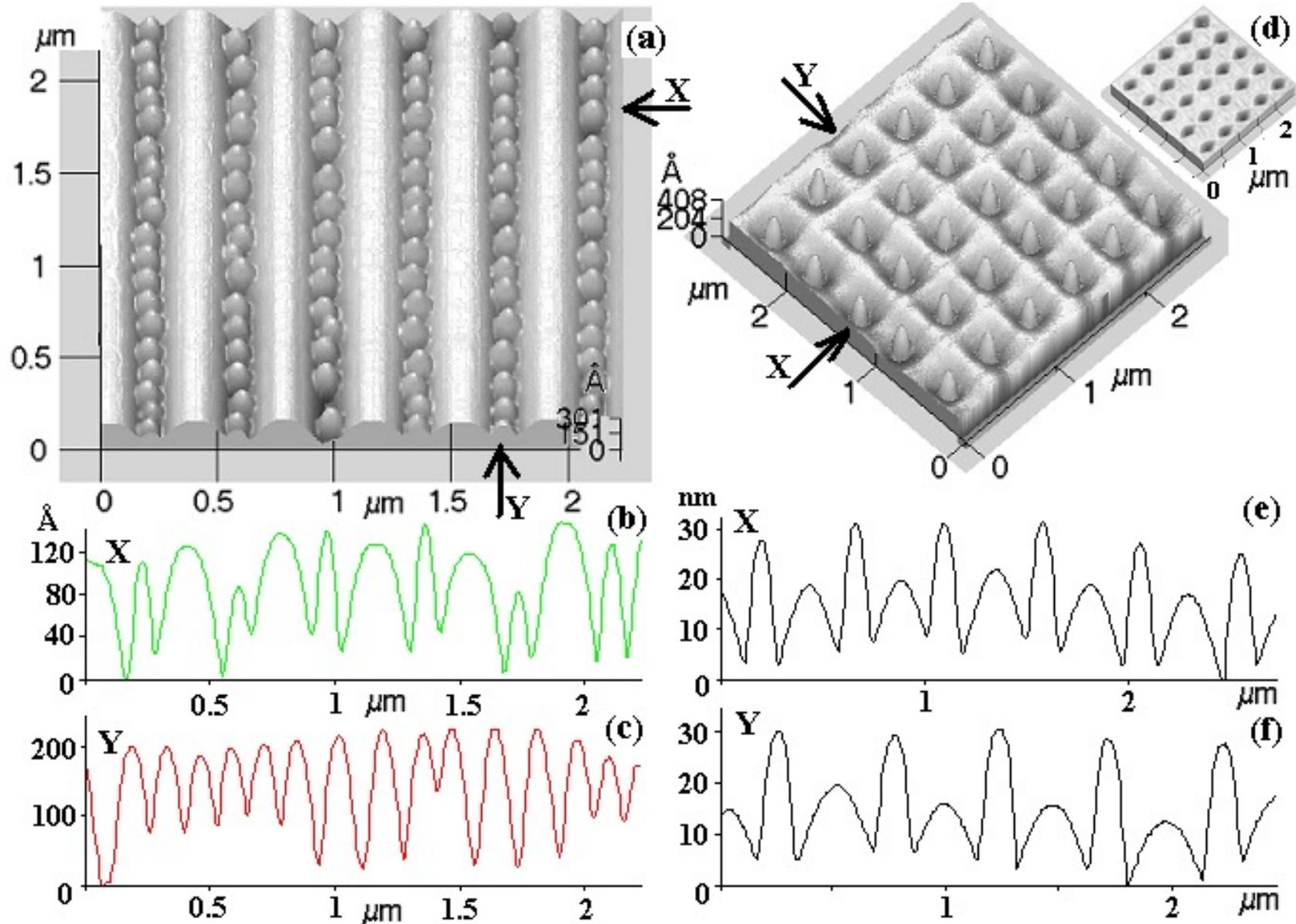
Reciprocal Space Result (1000 iterations)

Experiment



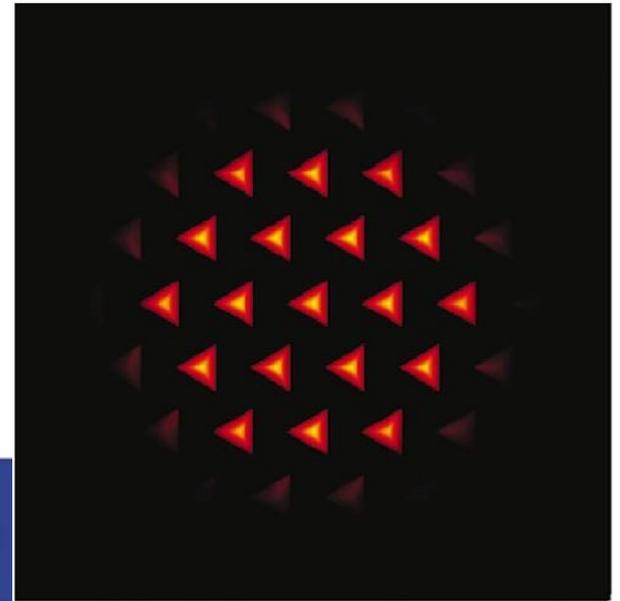
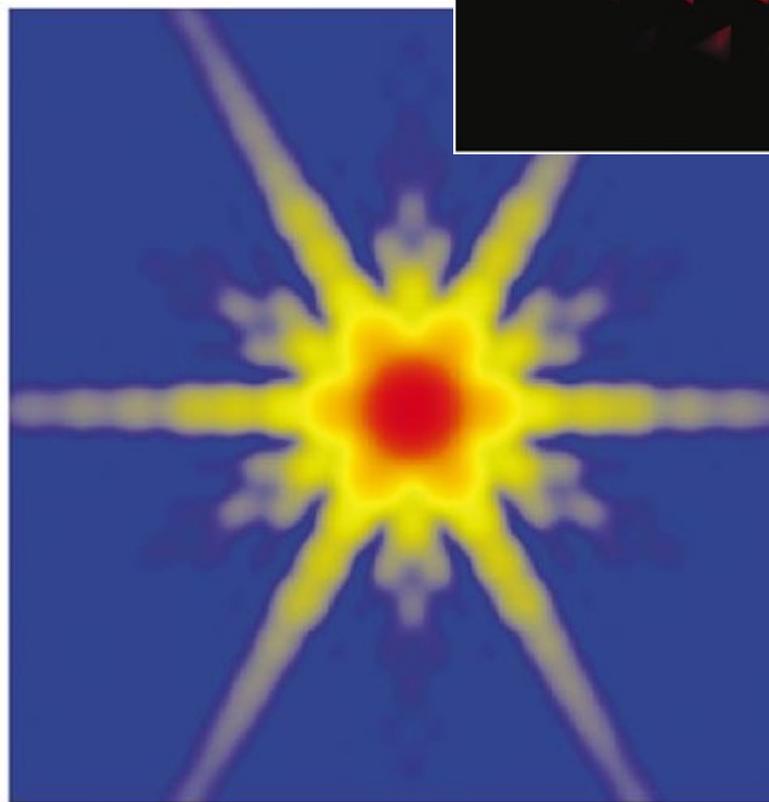
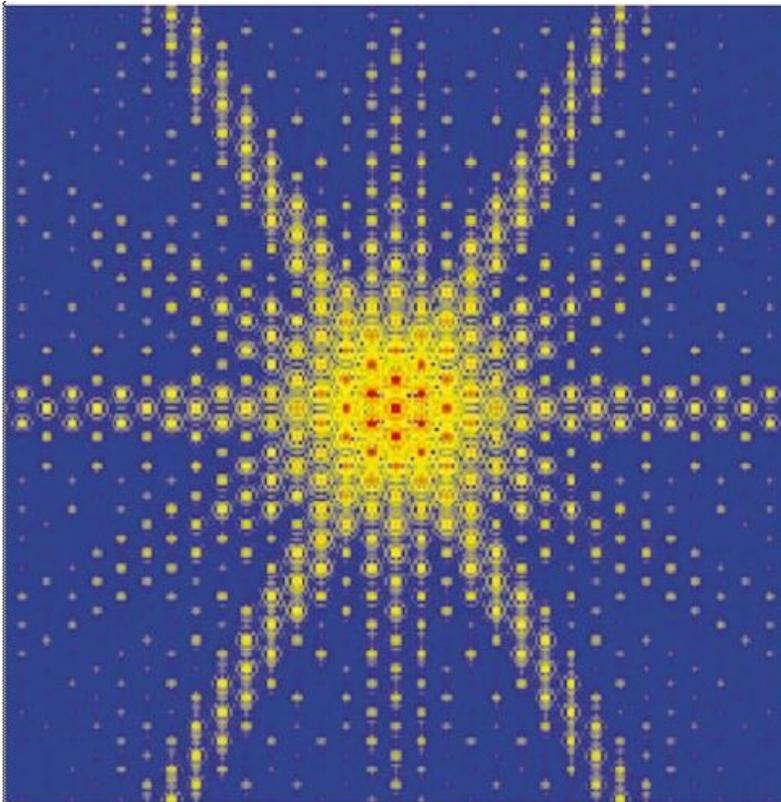
1D and 2D Quantum Dot Arrays

Zhenyang Zhong, G. Bauer, Johannes Kepler Universität Linz



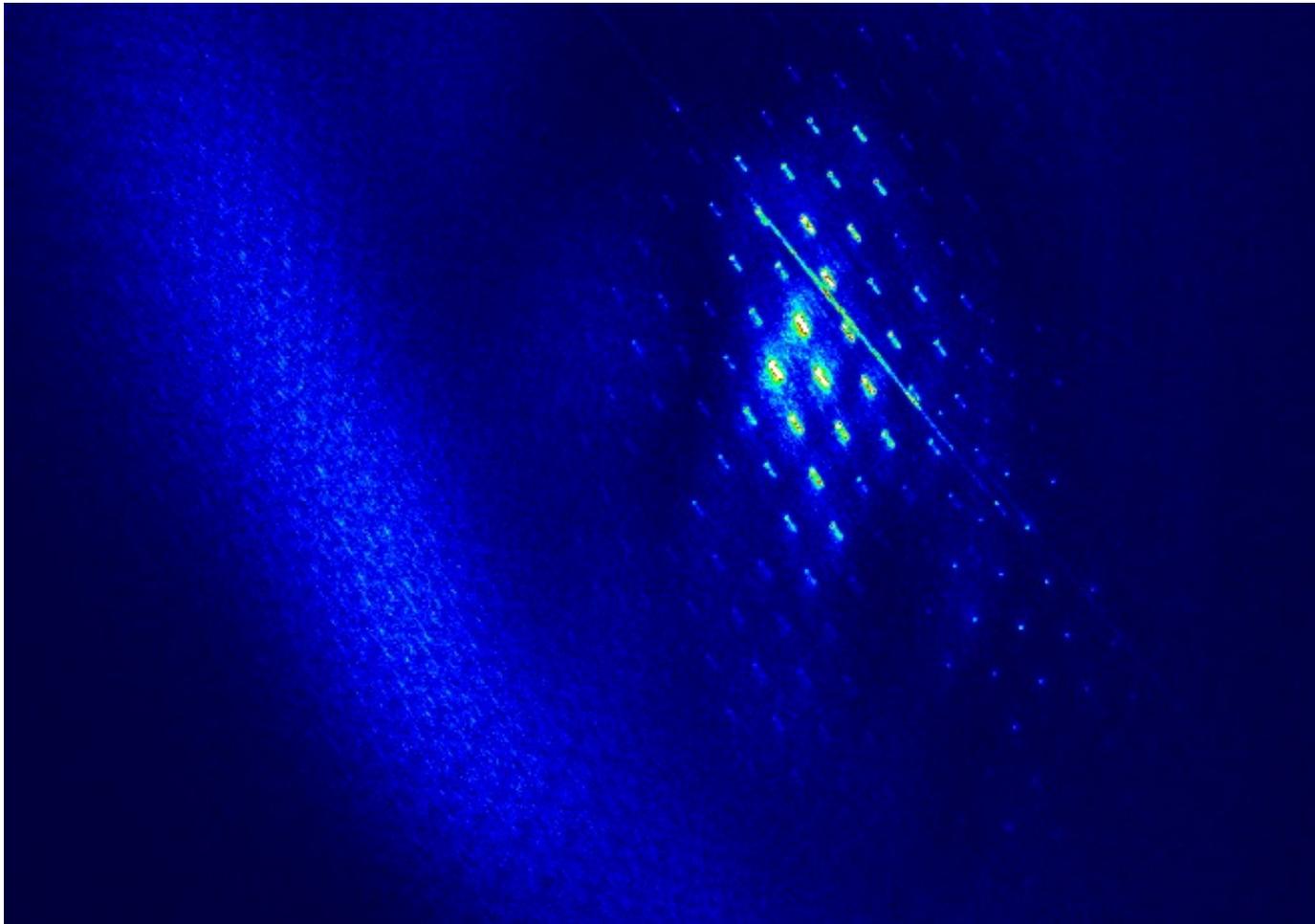
Vary Coherence (model)

I. A. Vartanyants and I. K. Robinson,
J. Sync. Rad. **10** 409 (2003)

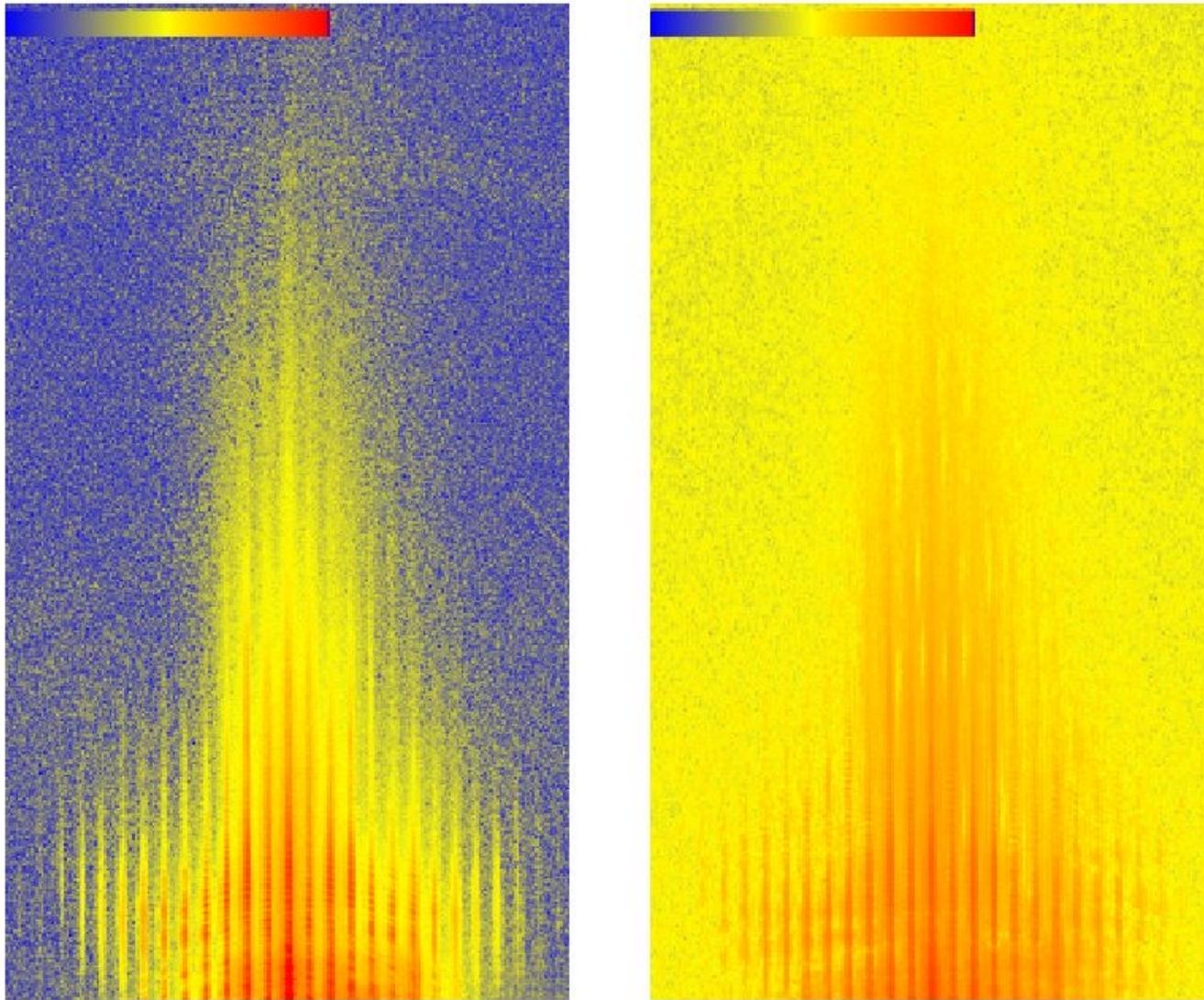


202 Diffraction from Ge QD array

with G. Bauer, Z. Zhong and T. H. Metzger

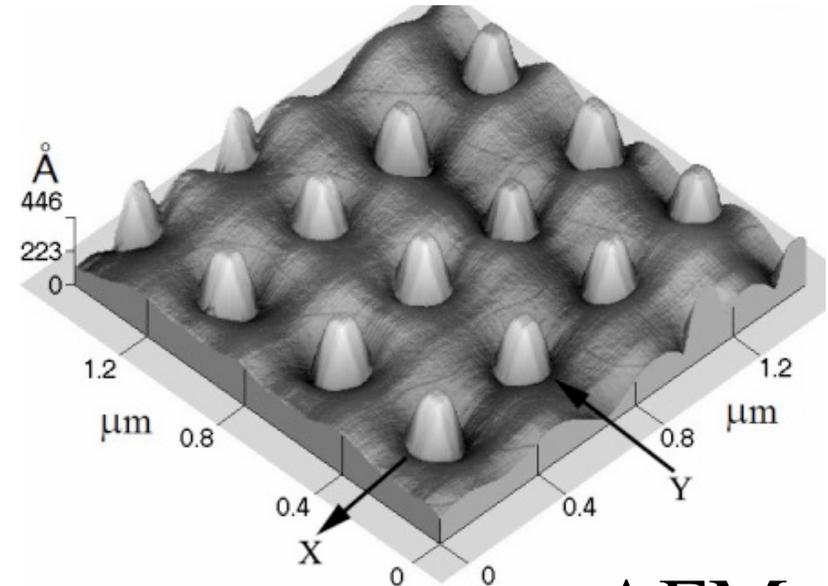
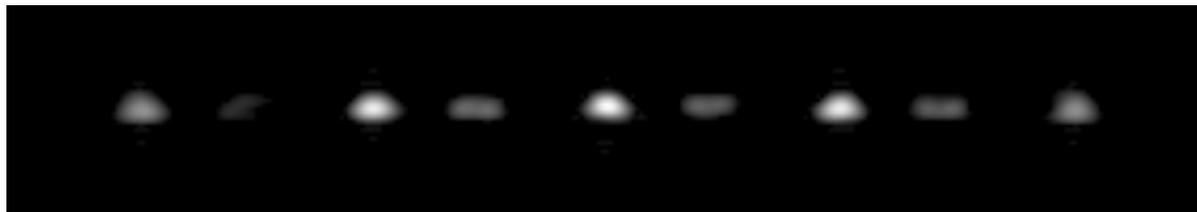
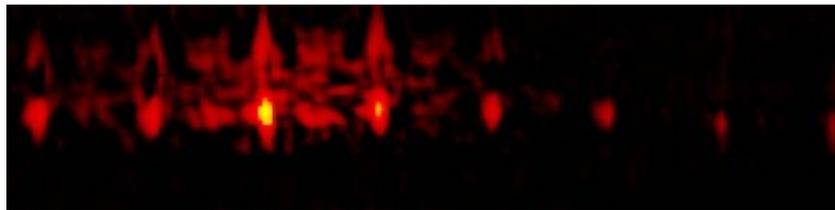
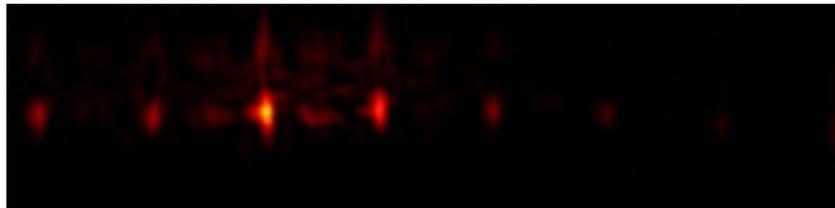


Result of fitting GISAXS data



Images from Fitting GISAXS

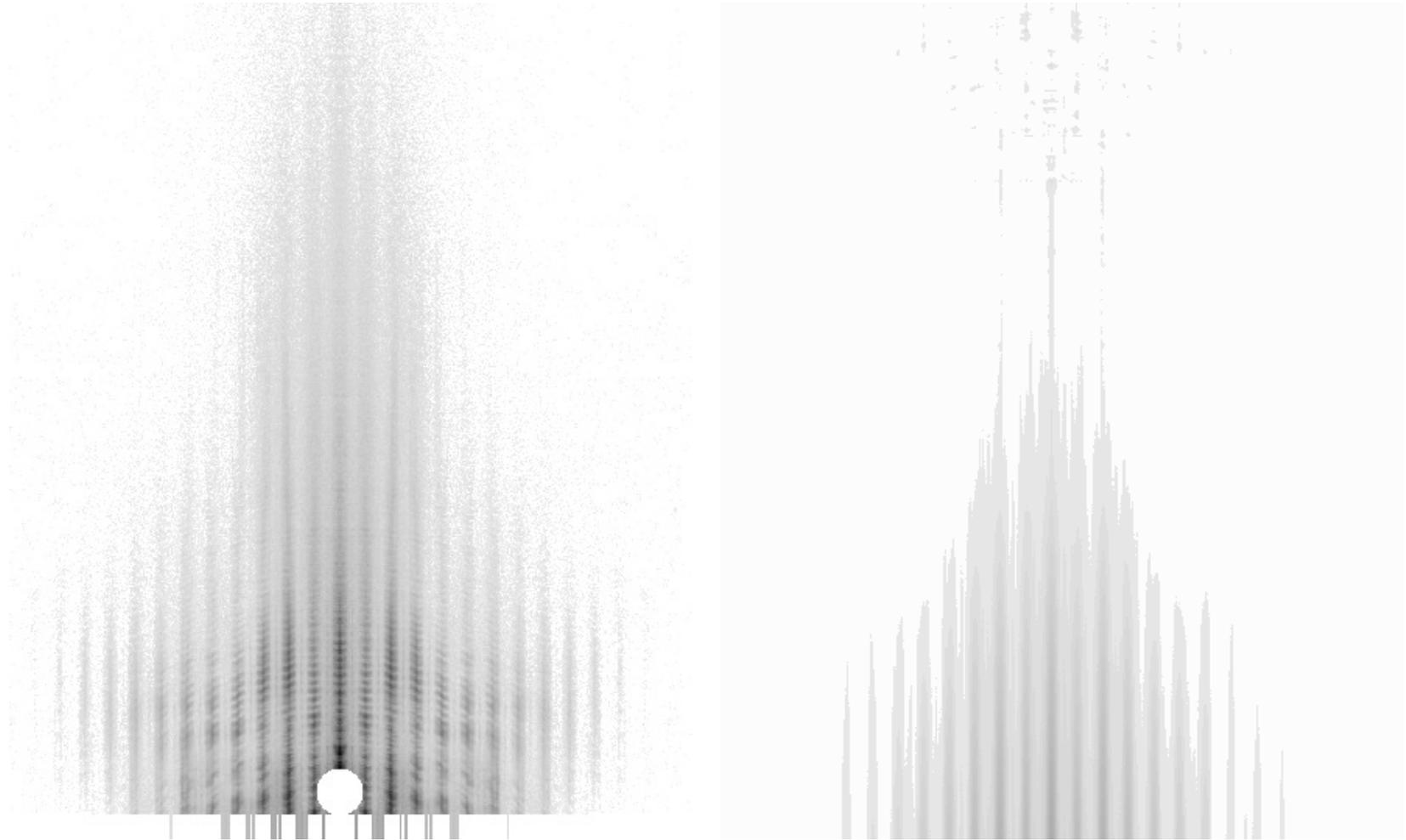
with Jeff Onken



AFM

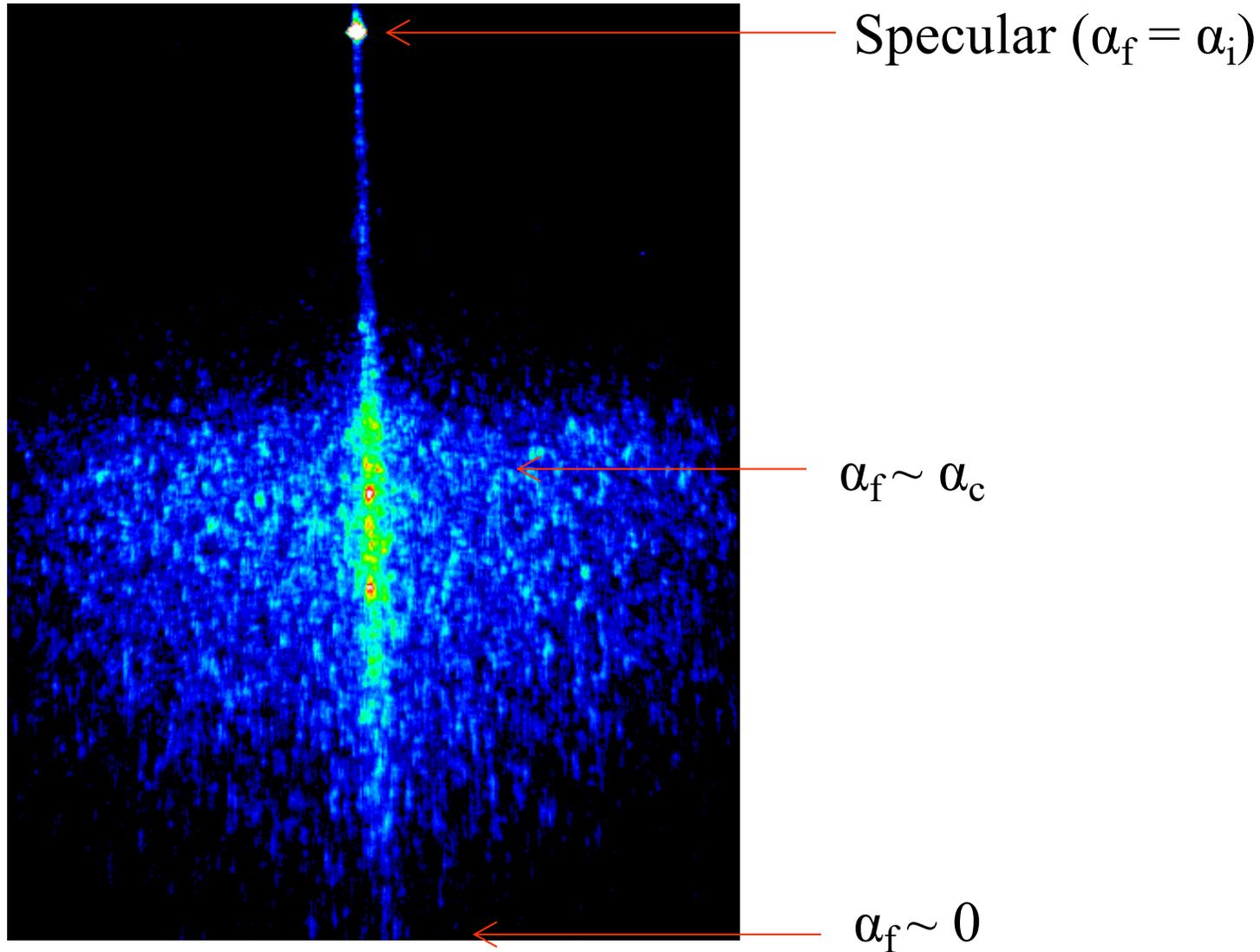
Mask used
as support

Diffraction pattern under constraint



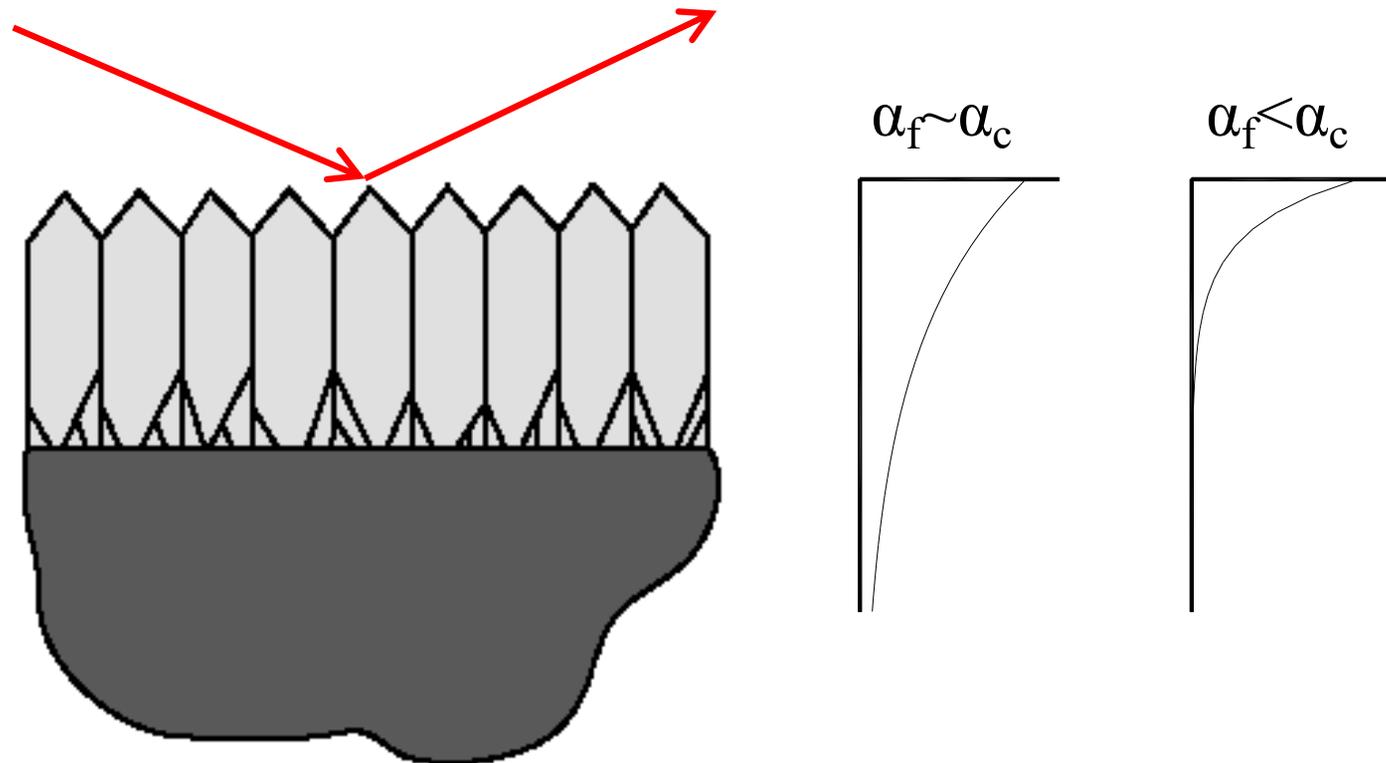
Fine Structure in “Yoneda” Peak

Grazing-exit diffraction from a 1000Å Au polycrystalline film

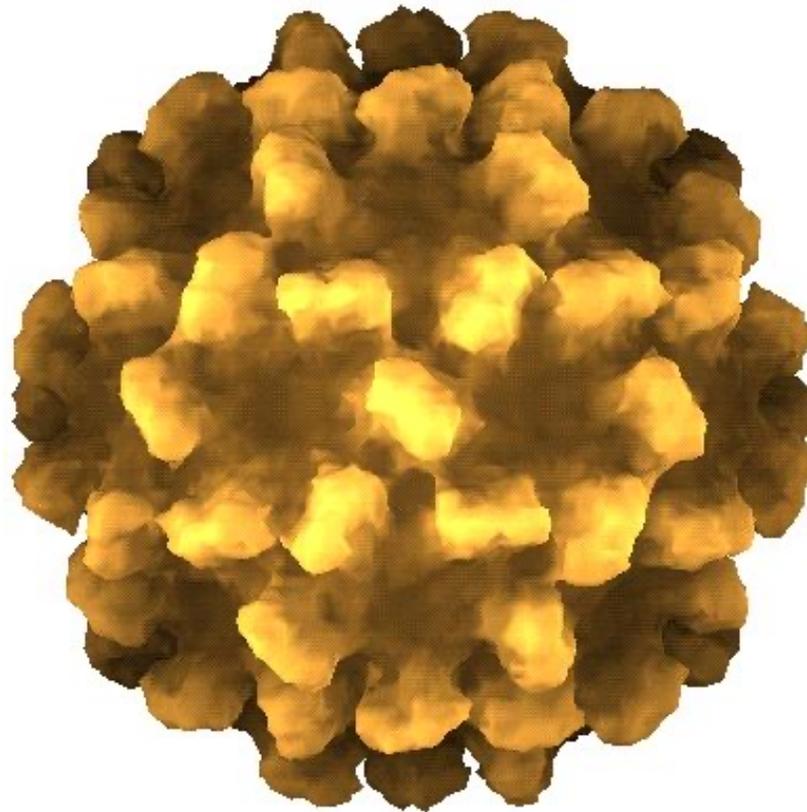


Competitive Grain Growth

C. V. Thompson, *Ann. Rev. Mat. Sci.* **30** 159 (2000)



Tomato Bushy Stunt Virus 1980



Conclusions and Outlook

- Inversion of CXD demonstrated
- Internal structure of Au Nanocrystals
- Preservation of coherence upon focussing
- Simple Quantum Dot structures possible now
- Single molecules one day