

# Coherent X-ray Diffraction analysis of Semiconductor Quantum Dot structures

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- Mark Pfeifer
- Garth Williams
- Curtis Benson

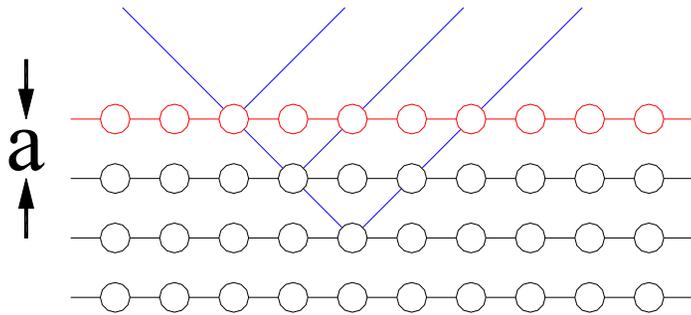
Department of Physics  
University of Illinois

Venture Business Laboratory  
Nagoya University  
October 2004

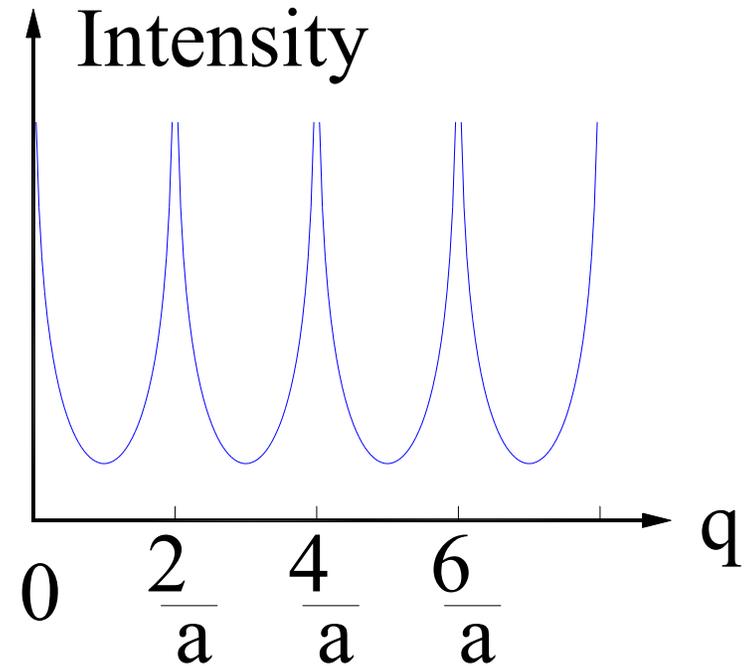
# Outline

- Direct analysis of CTRs
- Coherence in Diffraction
- Solving the **Phase** Problem
- Nanocrystal Shapes
- Quantum Dot structures
- How small can we go?

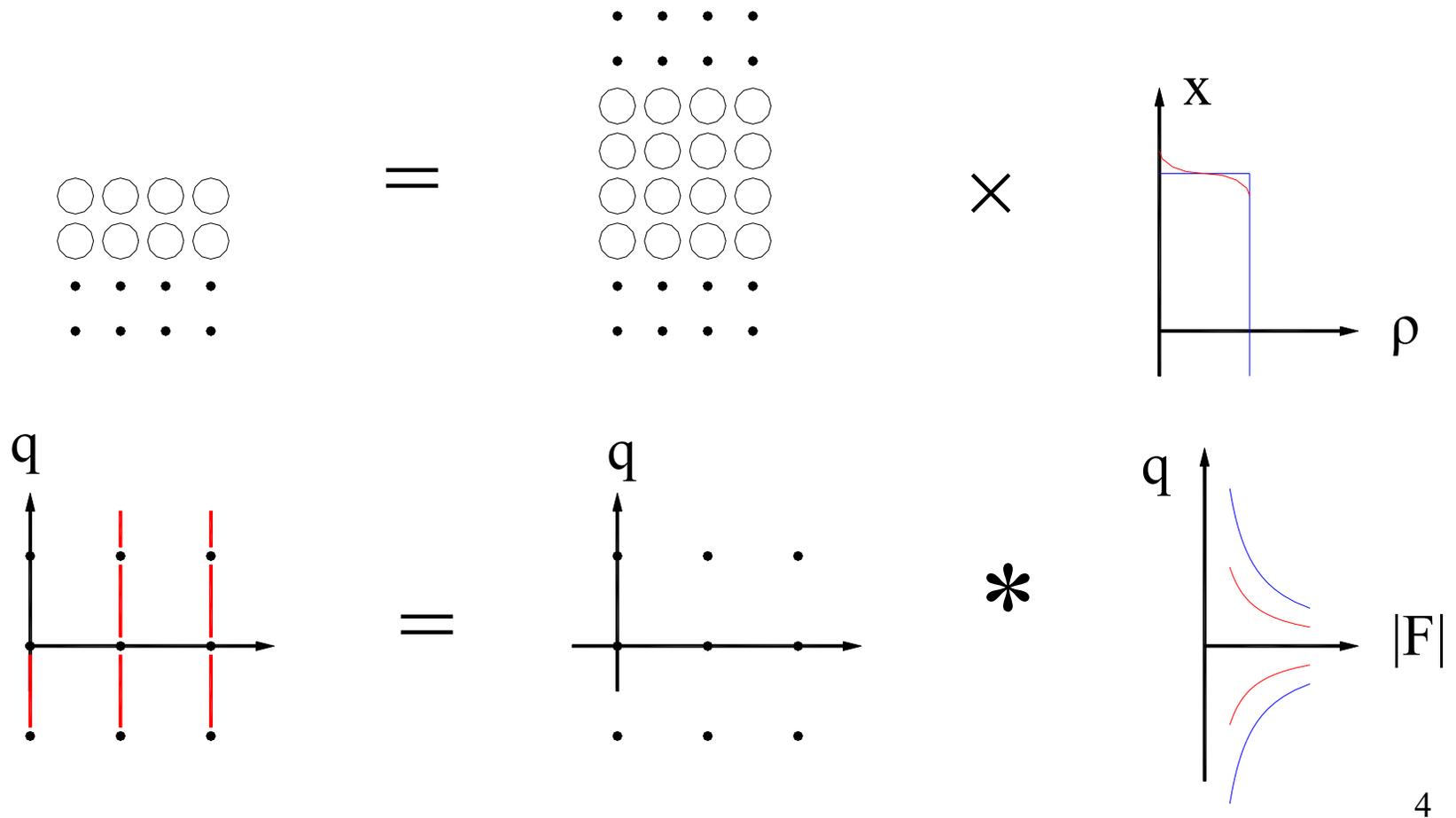
# Origin of Truncation Rods



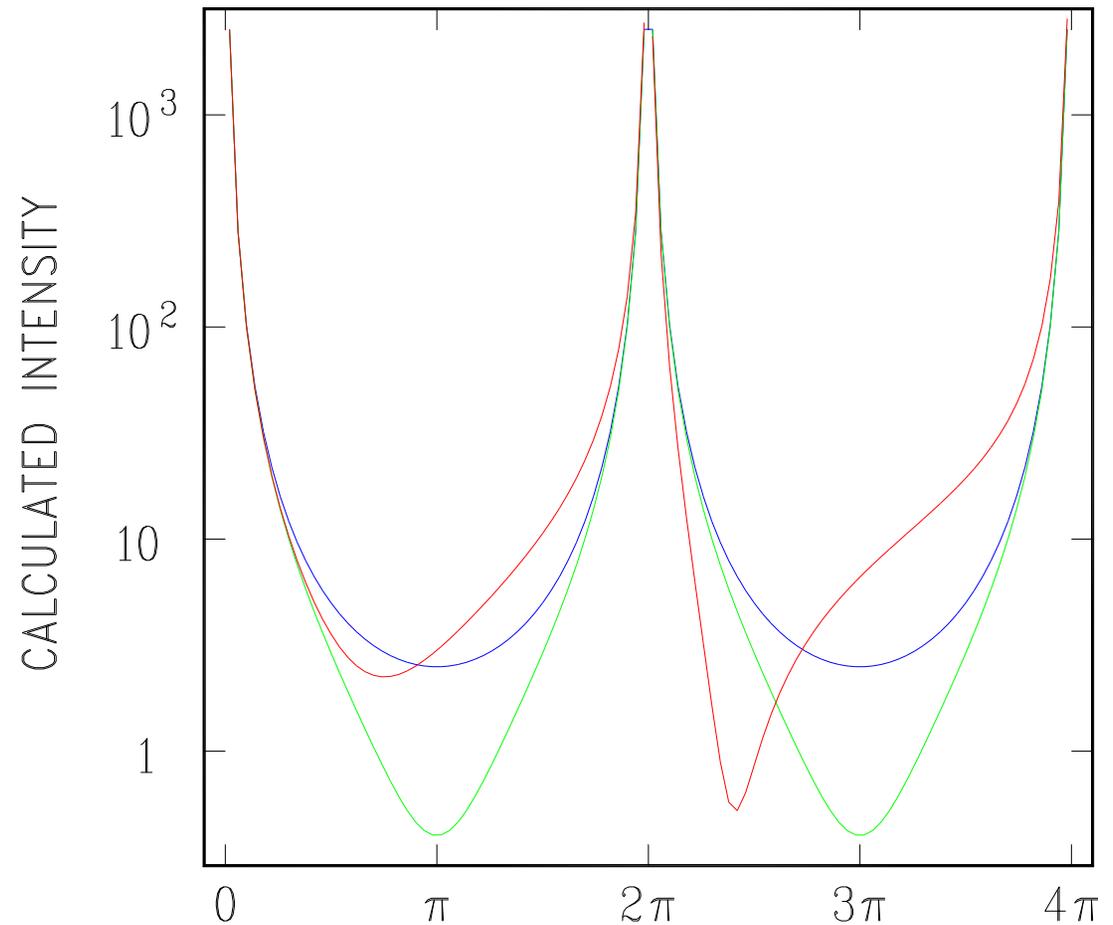
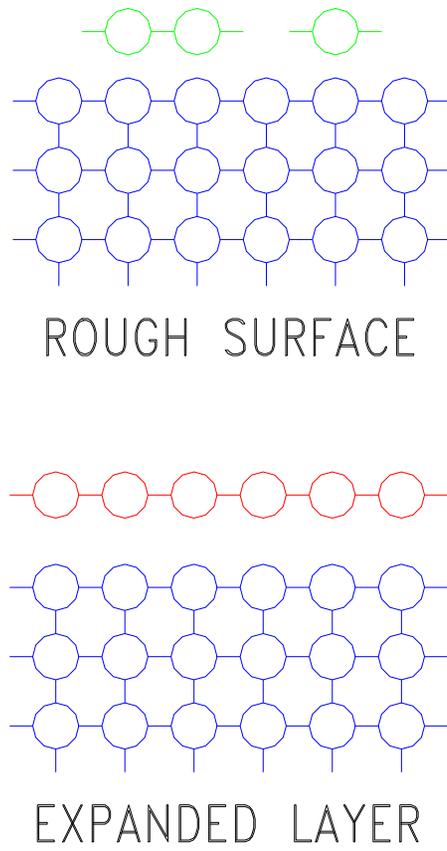
$$\begin{aligned} F_{CTR} &= \sum_{n=0}^{\infty} A_n \\ &= \sum_{n=0}^{\infty} f_L e^{inqa} \\ &= \frac{f_L}{1 - e^{iqa}} \end{aligned}$$



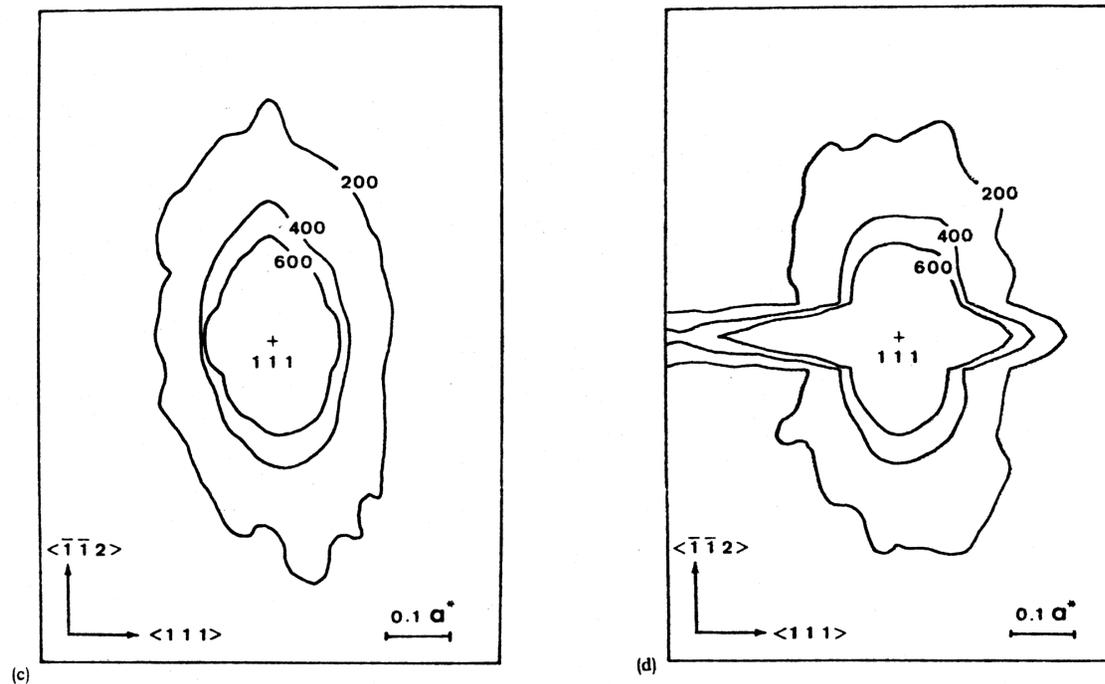
# CTR as Convolution



# CTR is Sensitive to Surface Structure



# Diffuse Scattering from Si Wafer



Unpolished wafer

40 microns removed

N. Kashiwagara, J. Harada and M. Ogino, J. Appl. Phys 54 2706 (1983)

# Diffraction as a Surface Integral

**Die äußere Form der Kristalle  
in ihrem Einfluß auf die Interferenzerscheinungen  
an Raumgittern**

**Von M. v. Laue**

Annalen der Physik [5] 26 55 (1936)

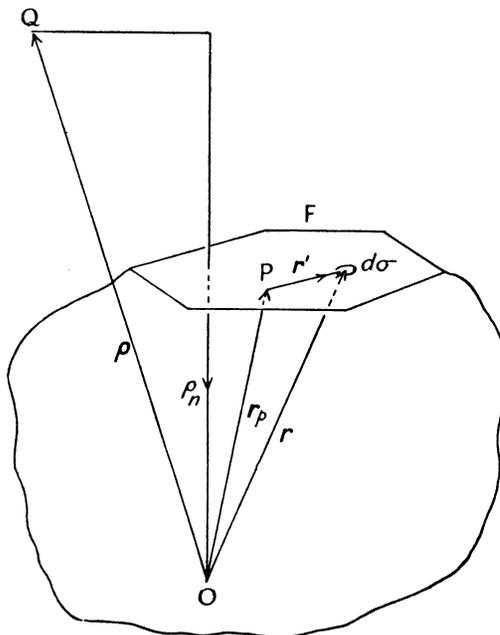
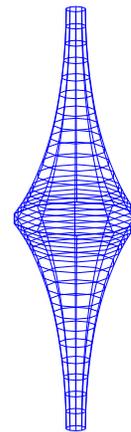
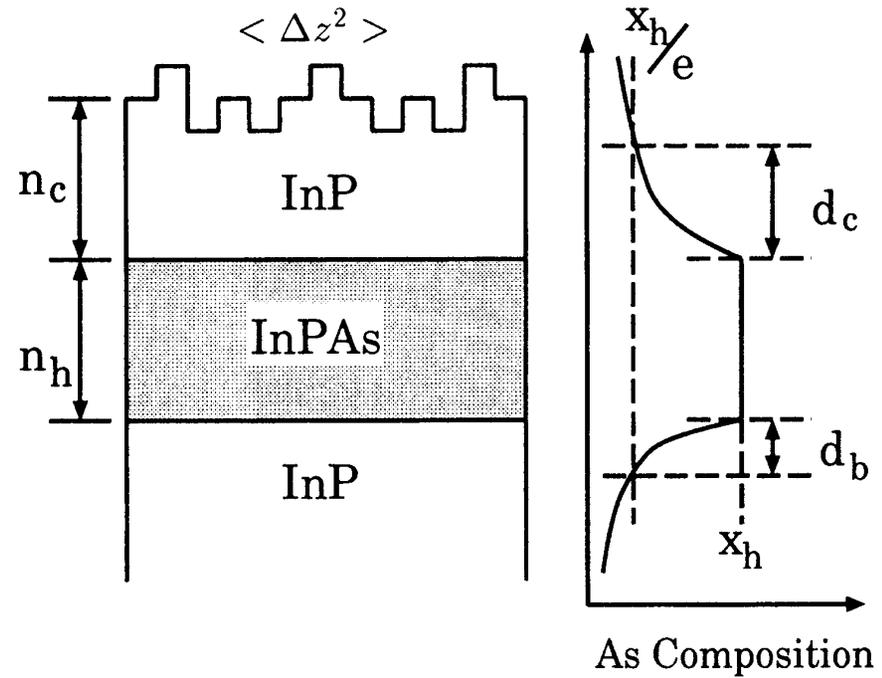
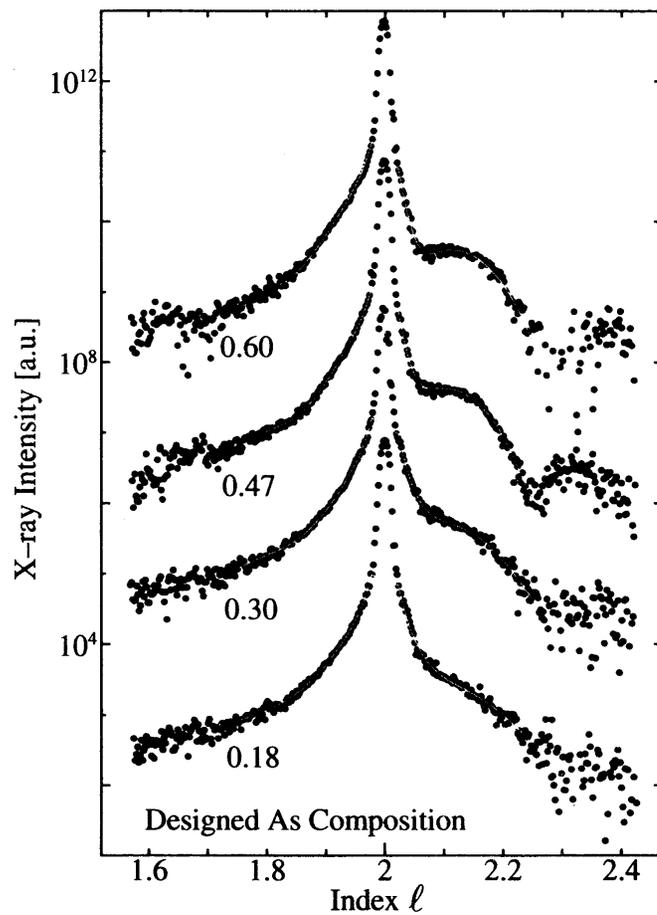


FIG. 200



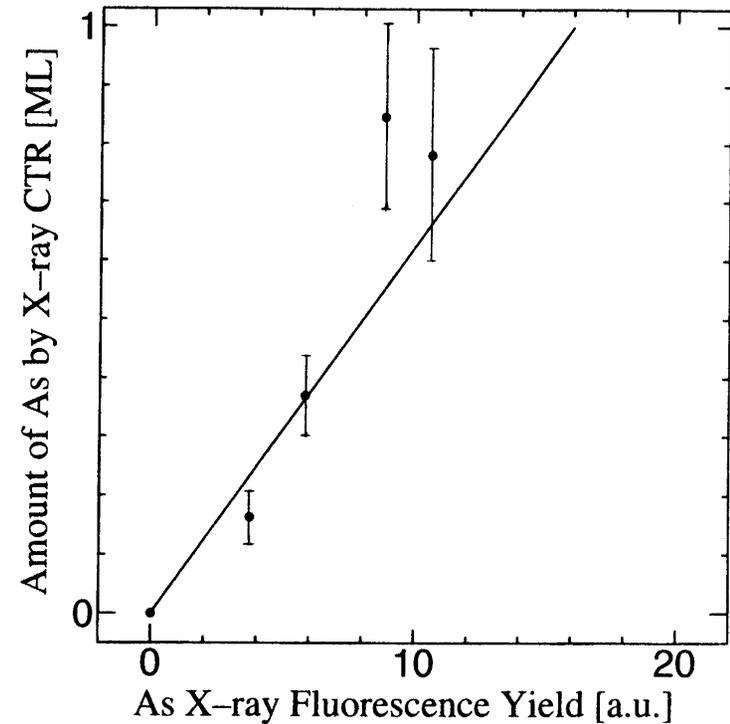
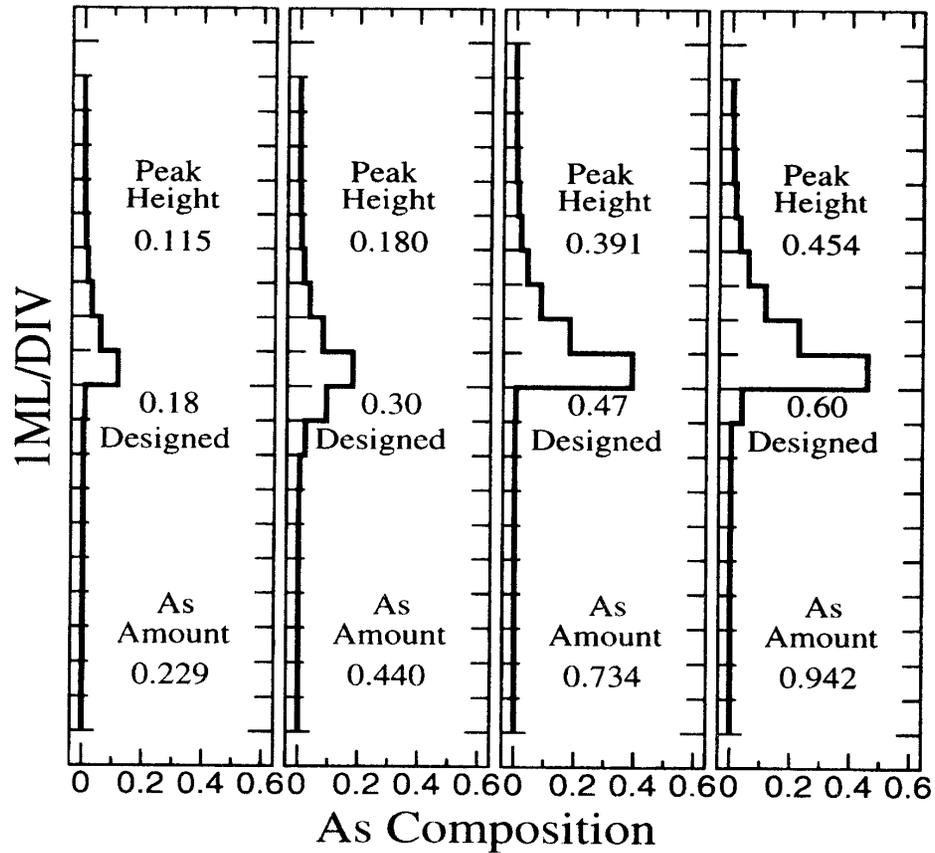
“Stacheln”

# As in InP/InPAs heterostructure



M. Tabuchi *et al* J. Appl. Phys 81 112 (1997)

# CTR agrees with Fluorescence



M. Tabuchi *et al* J. Appl. Phys 81 112 (1997)

# CTR of double-step structure



$$\begin{aligned} A_1(Q) &= \sum_{j=0}^{\infty} \rho_1 e^{iQaj} + \sum_{j=n}^{\infty} \rho_2 e^{iQaj} \\ &= (\rho_1 + \rho_2 e^{iQan}) \frac{1}{1 - e^{iQa}} \\ &= M_1(Q) \frac{1}{1 - e^{iQa}}. \end{aligned}$$

Perturbation limit:  $\rho_2 \ll \rho_1$

$$\begin{aligned} |M_1(Q)| &= |\rho_1 + \rho_2 e^{iQan}| \\ &\simeq \rho_1 + \rho_2 \cos(Qan) \end{aligned}$$

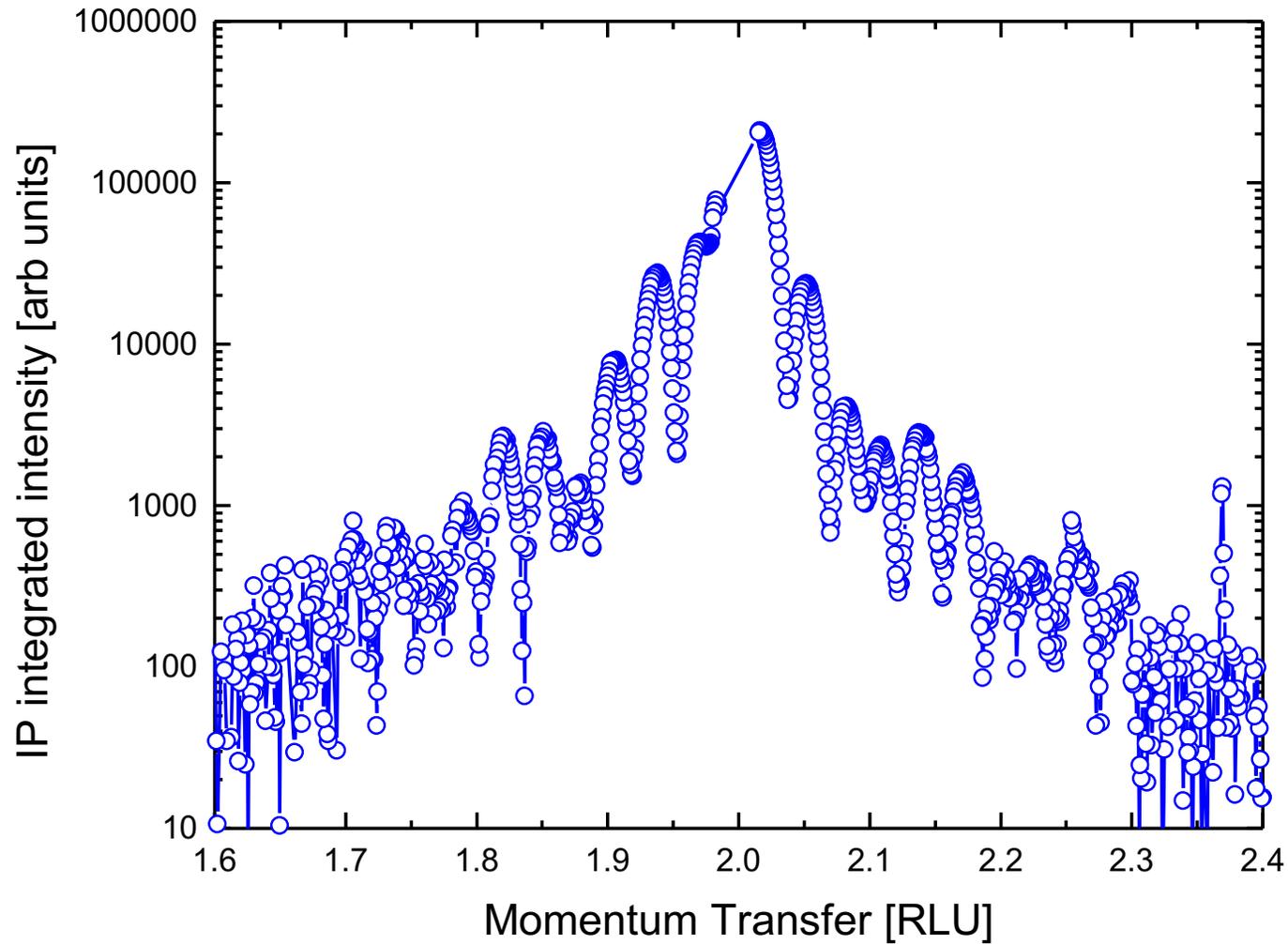
## Data Analysis Procedure

$$\begin{aligned} M(Q) &= \sqrt{I(Q)} / |A_0(Q)| \\ &= \sqrt{I(Q)} \sin(Qa/2). \end{aligned}$$

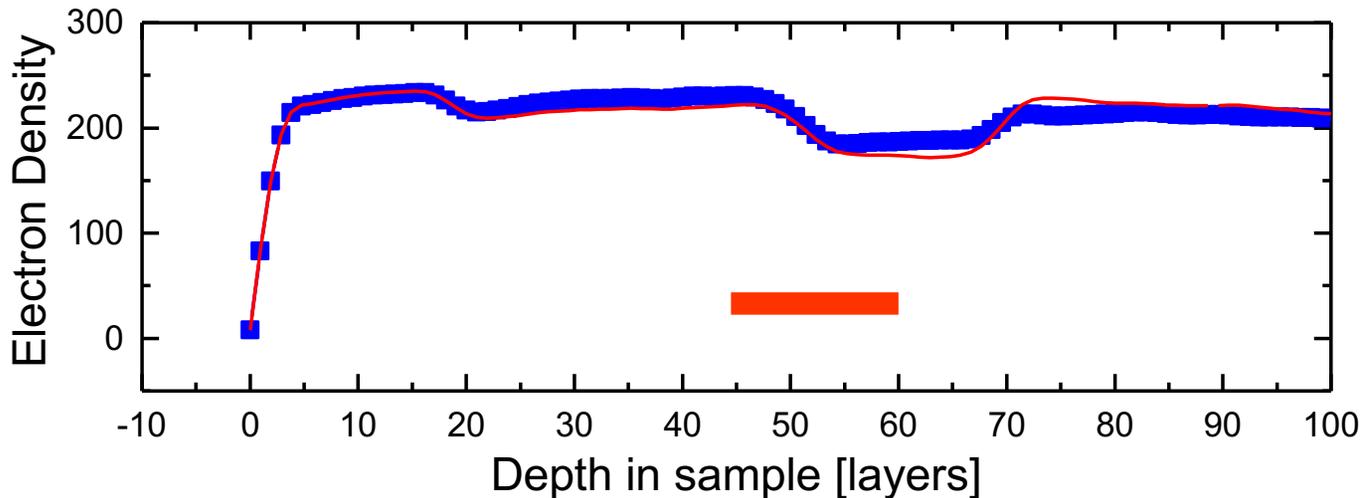
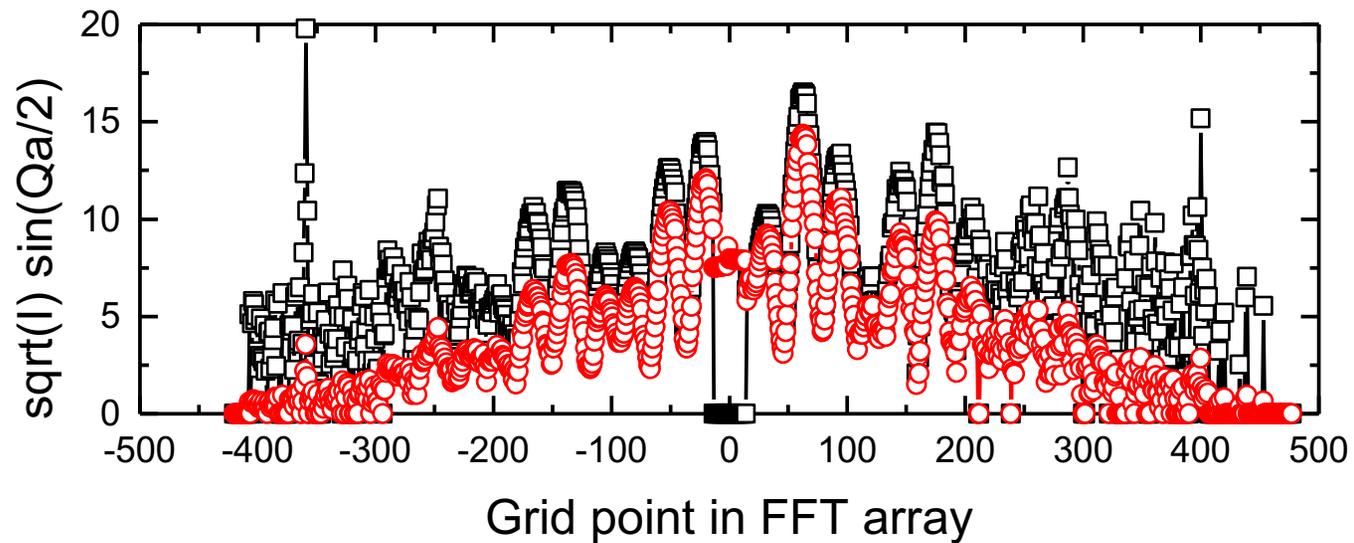
$$\rho(z) = \int_0^z \mathcal{F}\{\sqrt{I(Q)} \sin(Qa/2)\} dz'$$

# Test InP/GaAs/InP heterostructure

2IGA02231.dat 15ML GaInAs under 45ML InP



# Input and Output of FFT

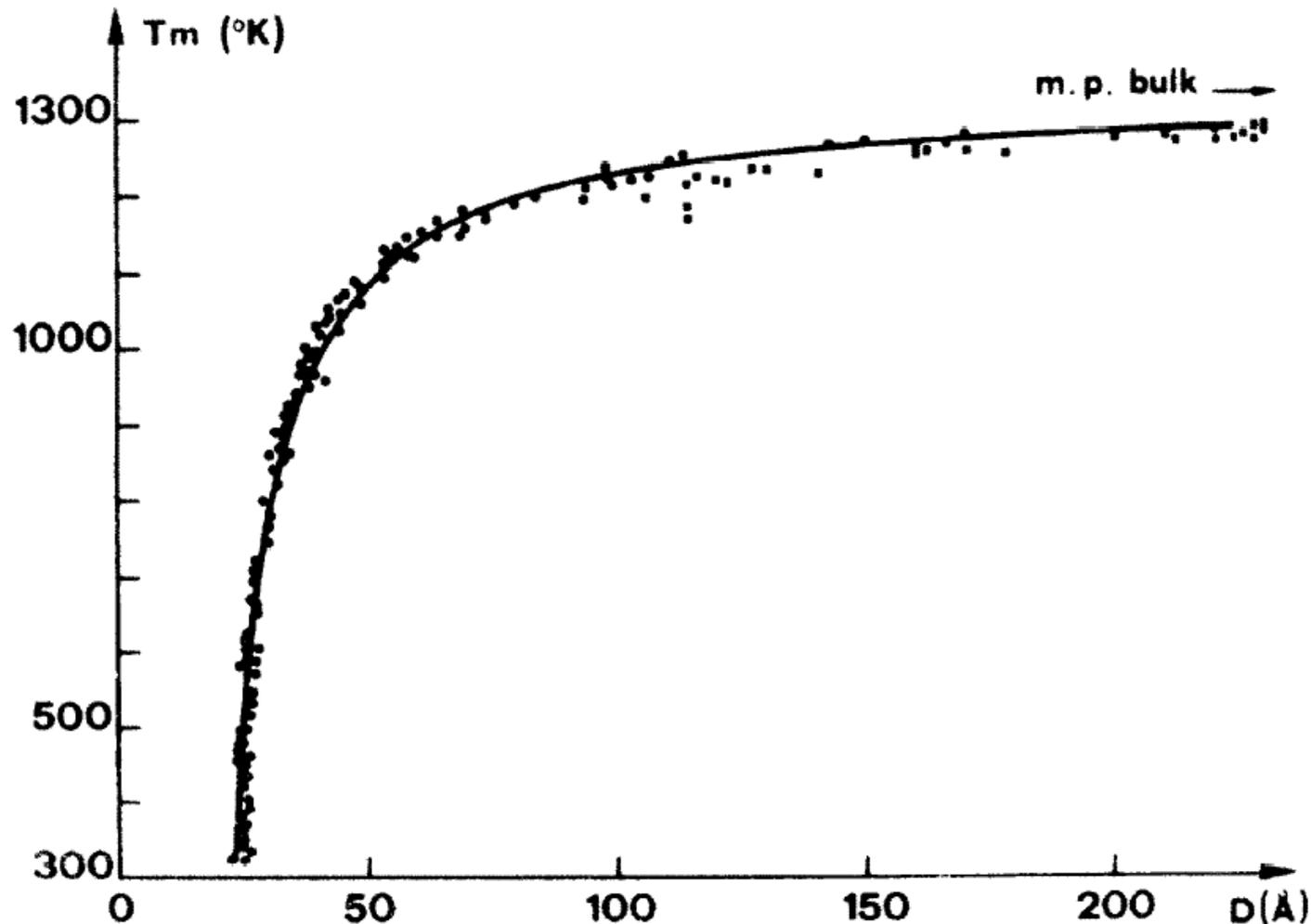


# Goals of Coherent Diffraction

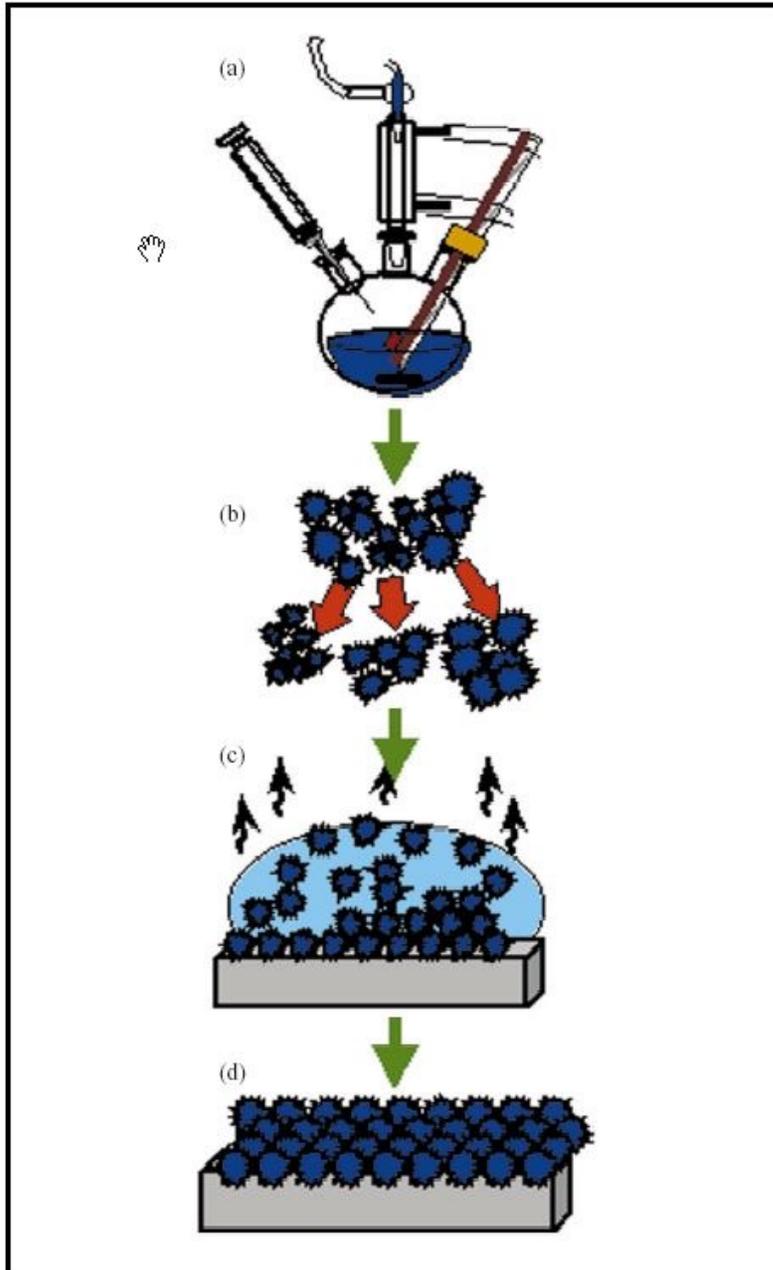
- Thermodynamic fluctuations
  - No ensemble average in CXD
- Probe of structure on **nm** scale
  - 1D, 2D and 3D
  - non-periodic object gives **continuous**  $F(\mathbf{q})$
- **Oversampling** (in reciprocal space) permits solution of the **phase** problem

# Size-dependent Melting of Au Particles

P. Buffat and J-P. Borel, Phys. Rev. A 2287-97 (1975)

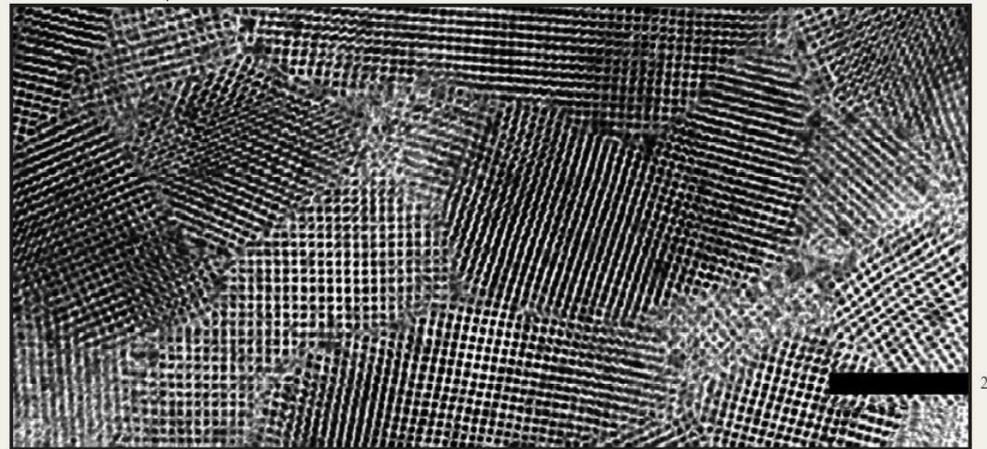


# Chemical Synthesis of Nanocrystals

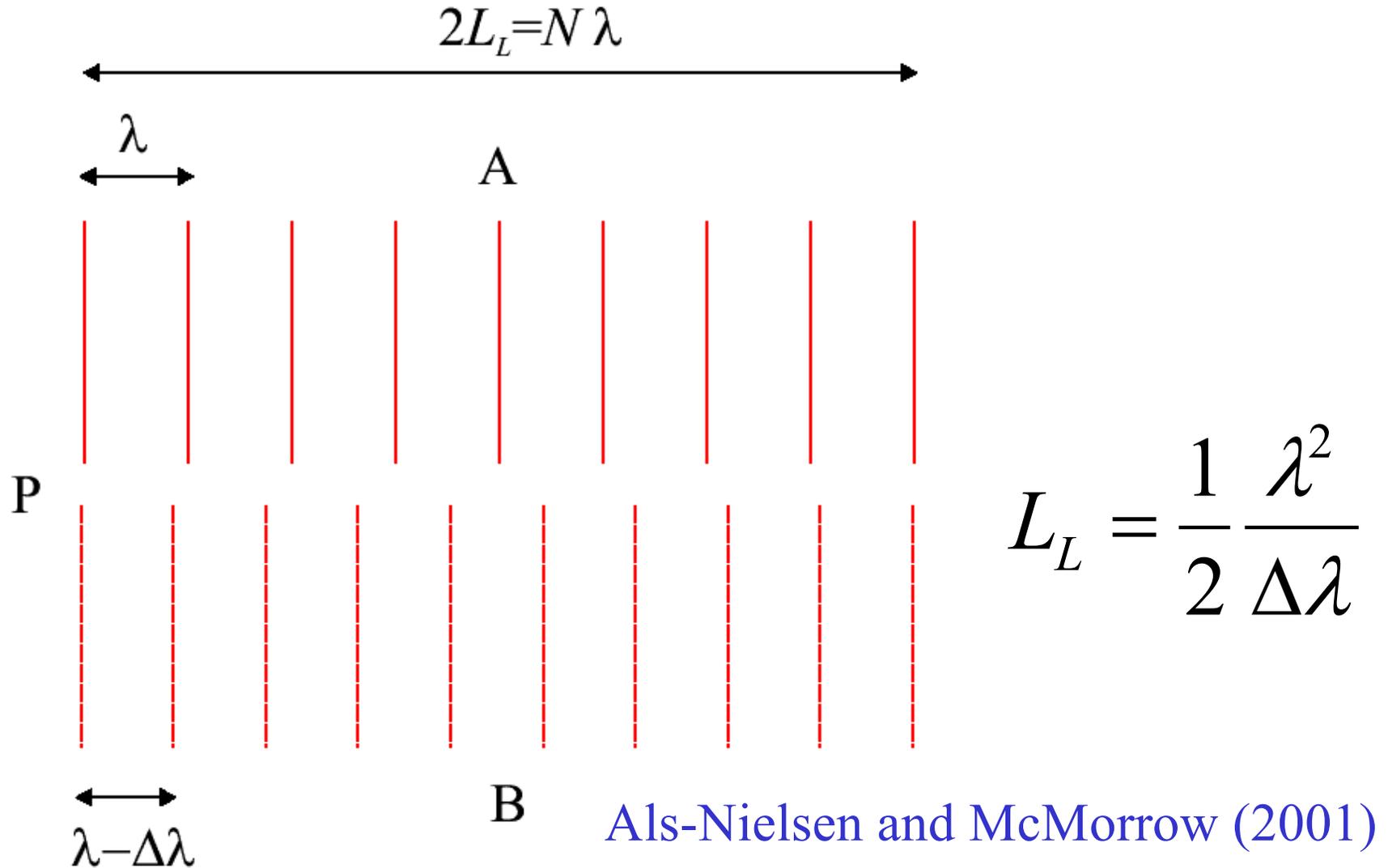


- Reactants introduced rapidly
- High temperature solvent
- Surfactant/organic capping agent
- Square superlattice (200nm scale)

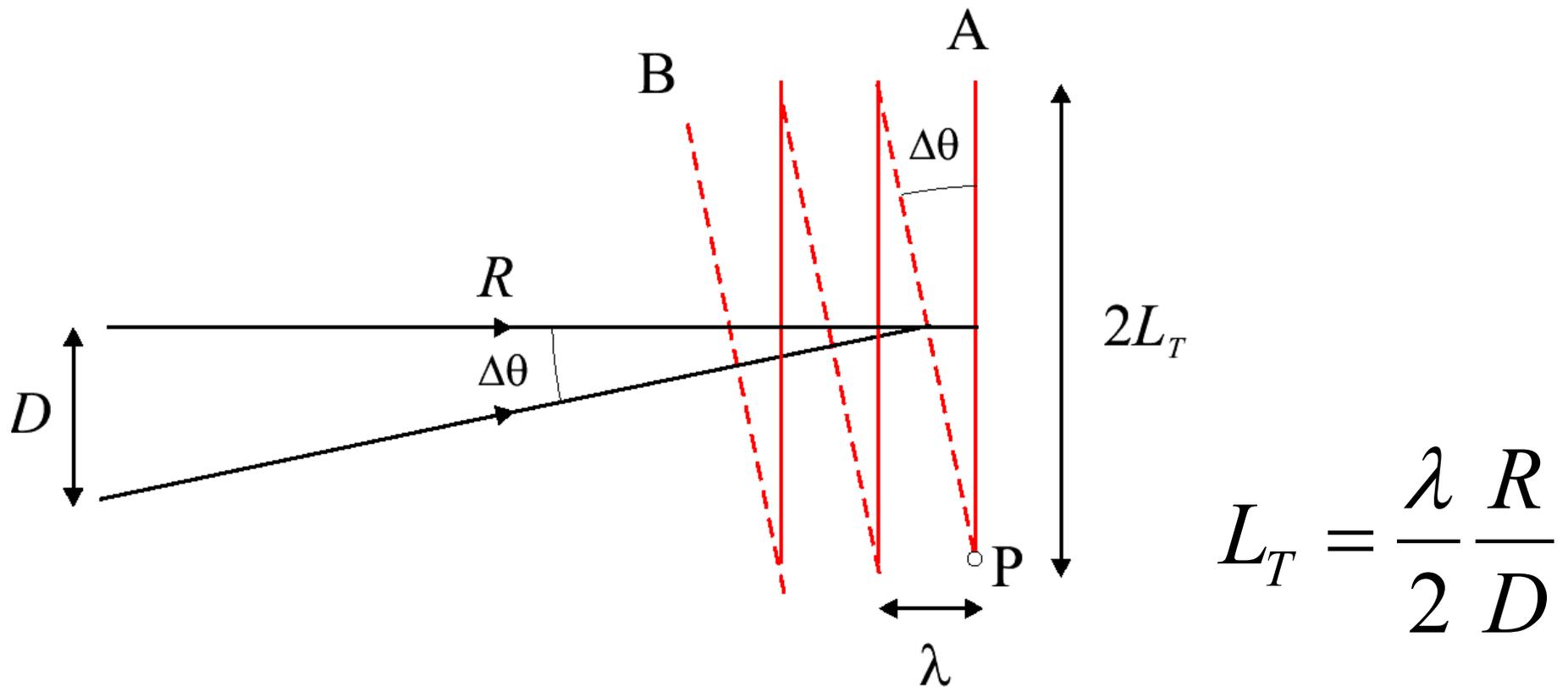
C. B. Murray, IBM J. Res. & Dev. **45**  
**47** (2001)



# Longitudinal Coherence



# Lateral (Transverse) Coherence



$$L_T = \frac{\lambda R}{2 D}$$

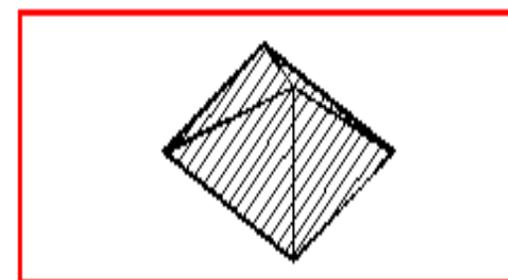
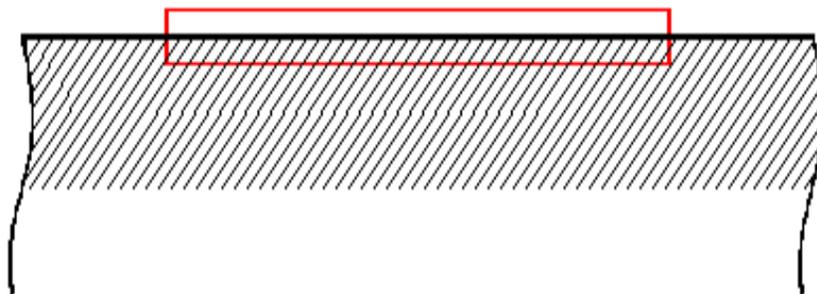
Als-Nielsen and McMorrow (2001)

# Coherence at Spring8, APS or ESRF

Typical of 3rd Generation (undulator) Synchrotron Source

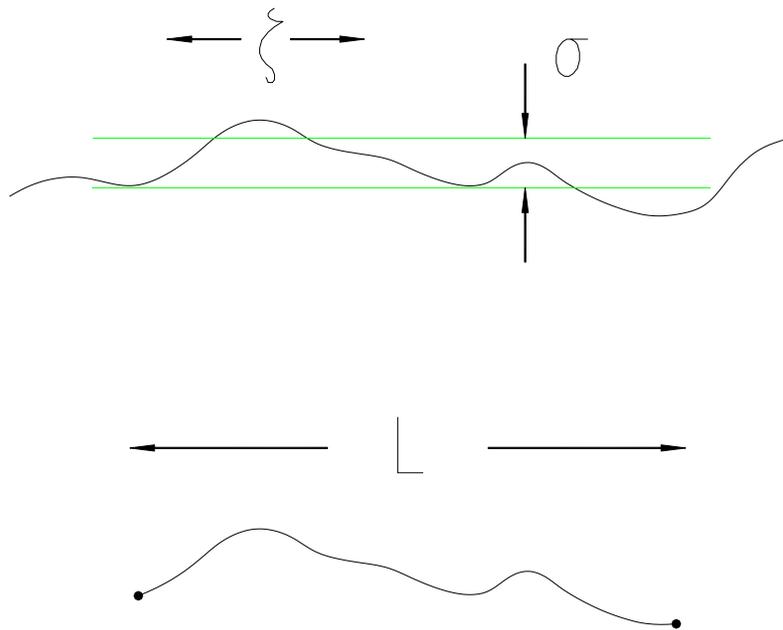
Coherence of	$\xi_{\text{VER}}$	$\xi_{\text{HORIZ}}$	$\xi_{\text{LONG}}$	Flux
Raw Undulator	35 $\mu\text{m}$	9 $\mu\text{m}$	0.004 $\mu\text{m}$	$2 \times 10^{12}$
Si(111) Monochromator	35 $\mu\text{m}$	9 $\mu\text{m}$	1 $\mu\text{m}$	$1 \times 10^{10}$
C(111) Monochromator	35 $\mu\text{m}$	9 $\mu\text{m}$	3 $\mu\text{m}$	$3 \times 10^9$

Coherent region defined by slits

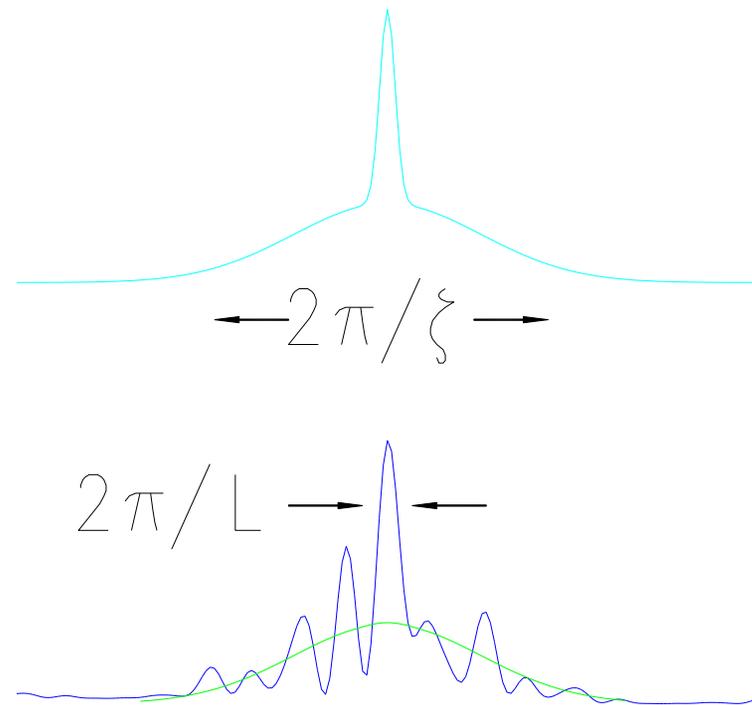


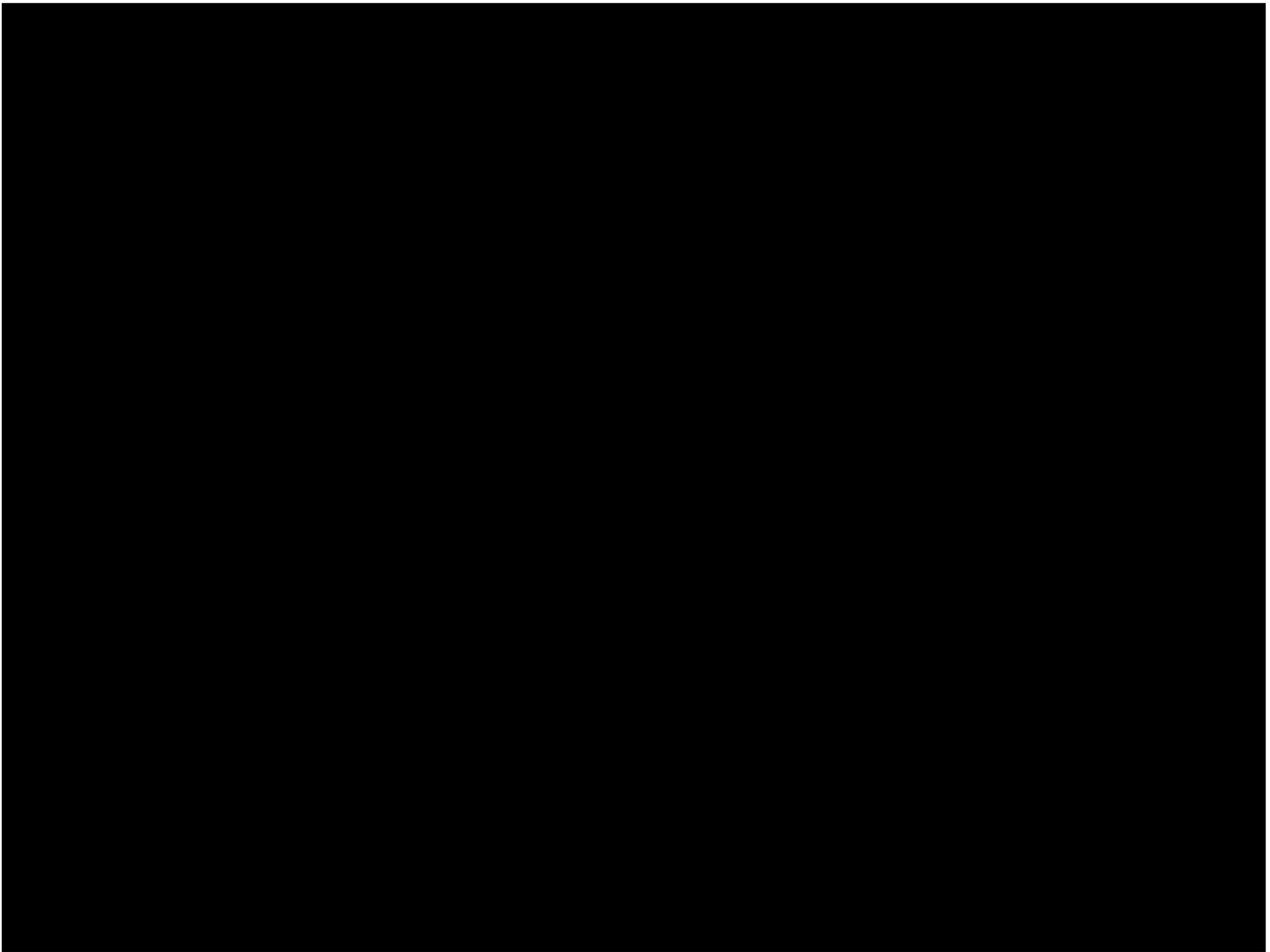
# Diffuse Scattering acquires Structure using CXD

Real Space

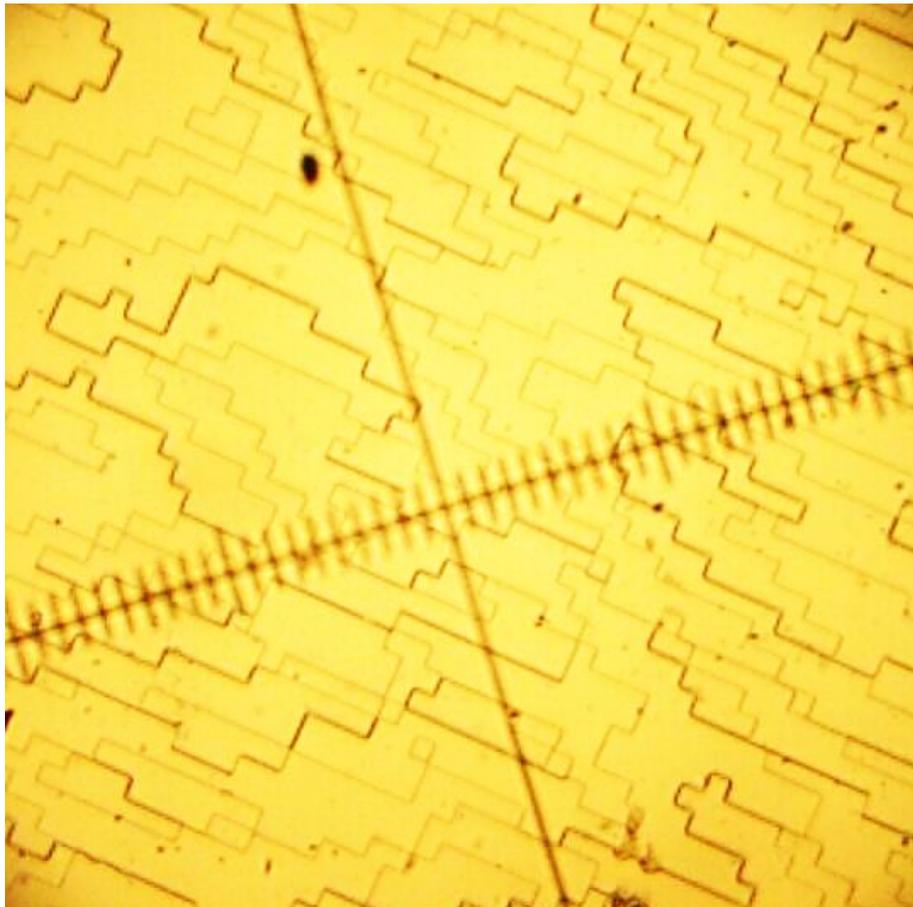


Reciprocal Space

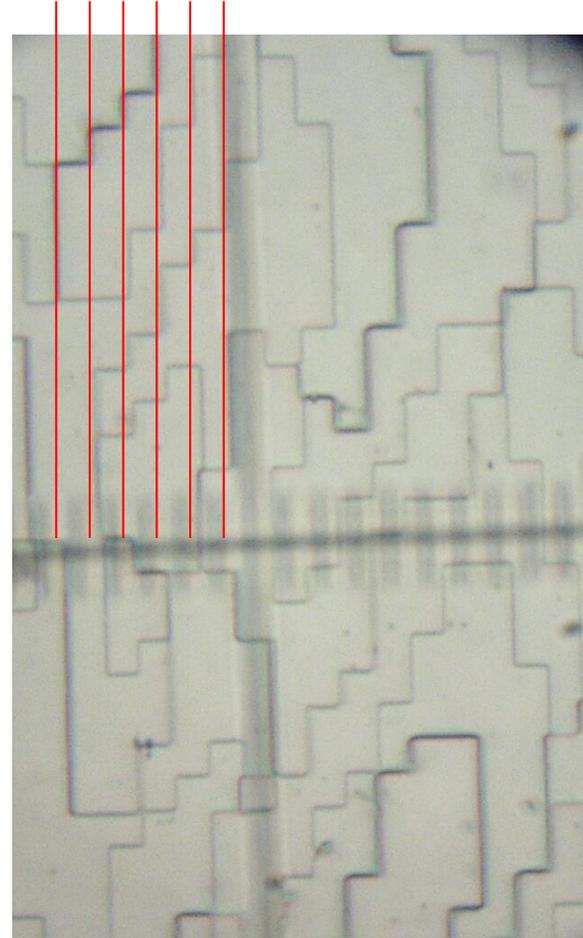




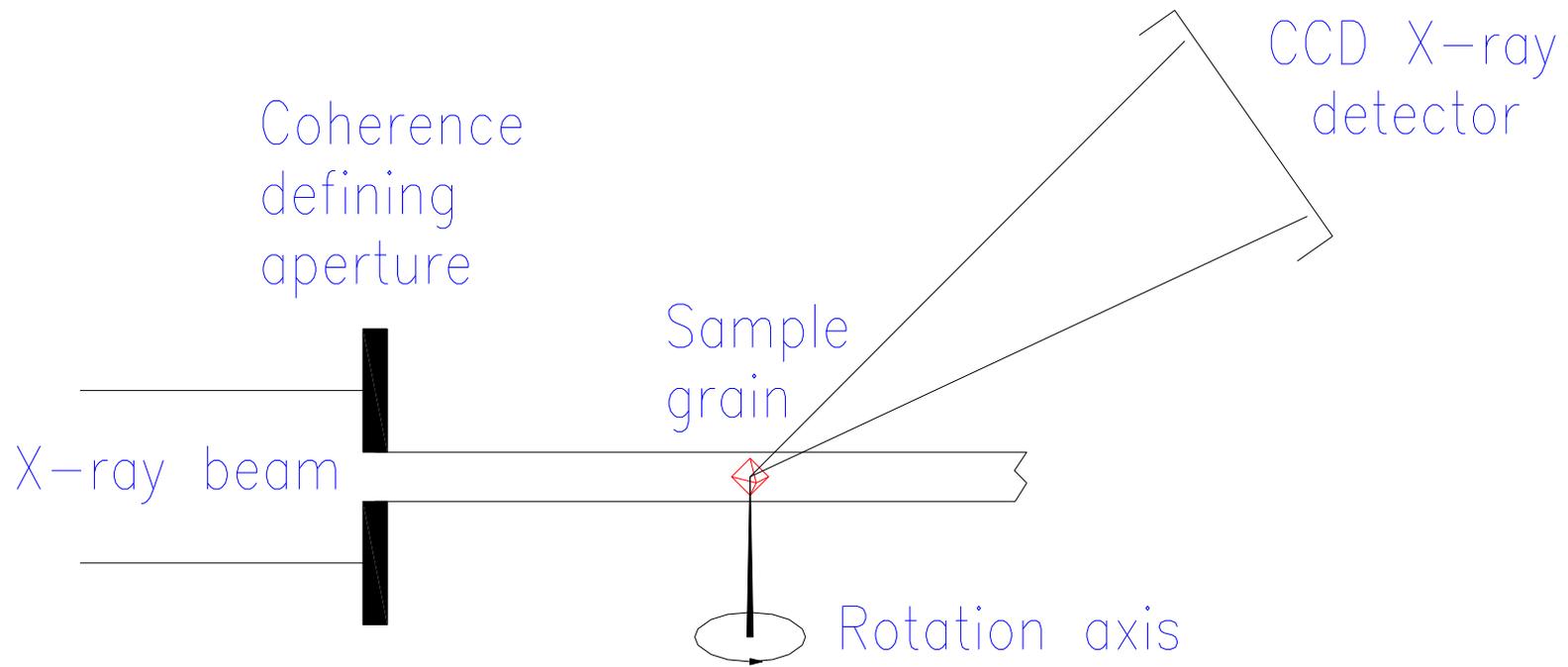
# Microscope Images of Gratings



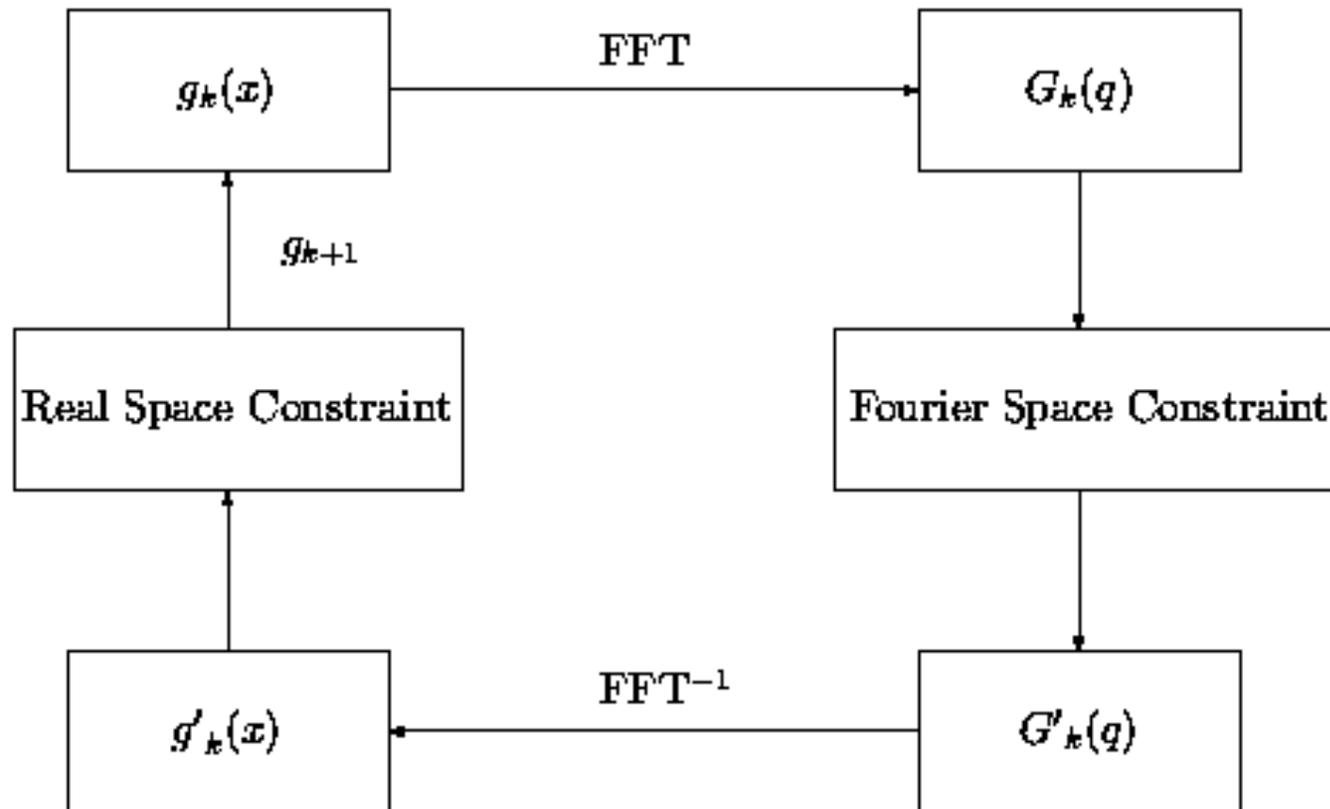
5 $\mu$ m grid lines



# Lensless X-ray Microscope



# Generic “Error Reduction” method



J. R. Fienup *Appl. Opt.* 21 2758 (1982)

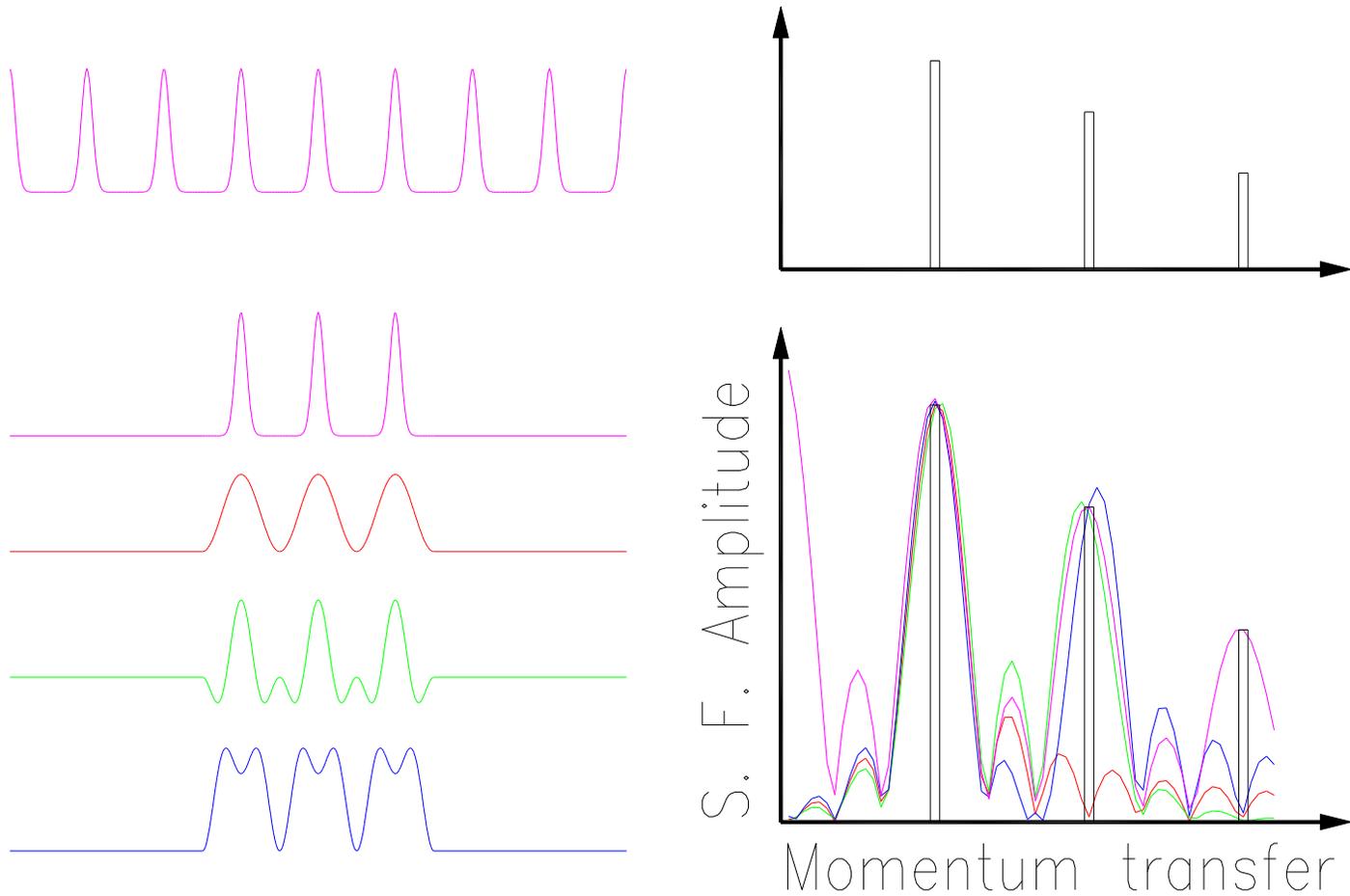
R. W. Gerchberg and W. O. Saxton *Optik* 35 237 (1972)

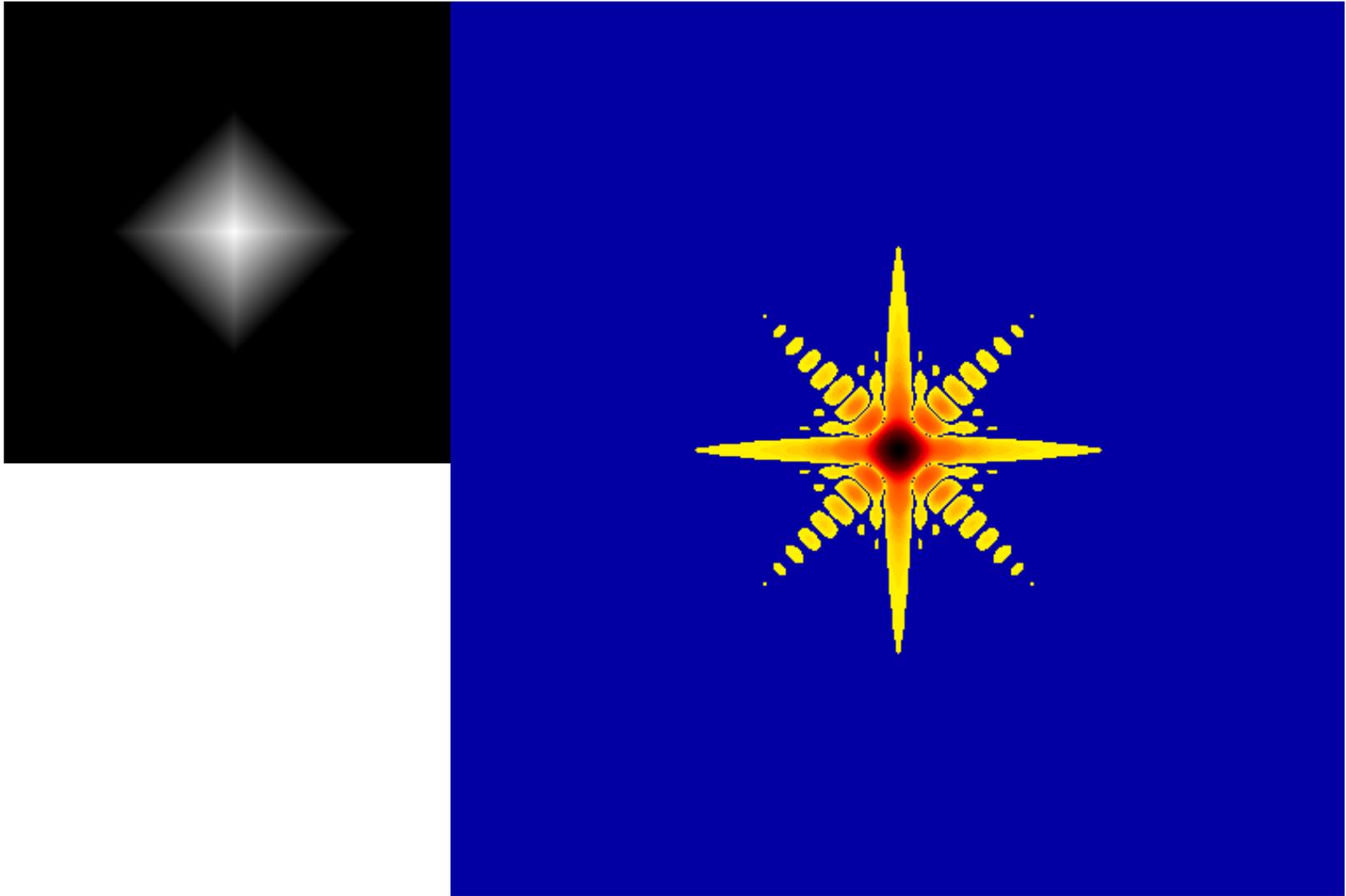
# Real-space Constraints in Crystallography

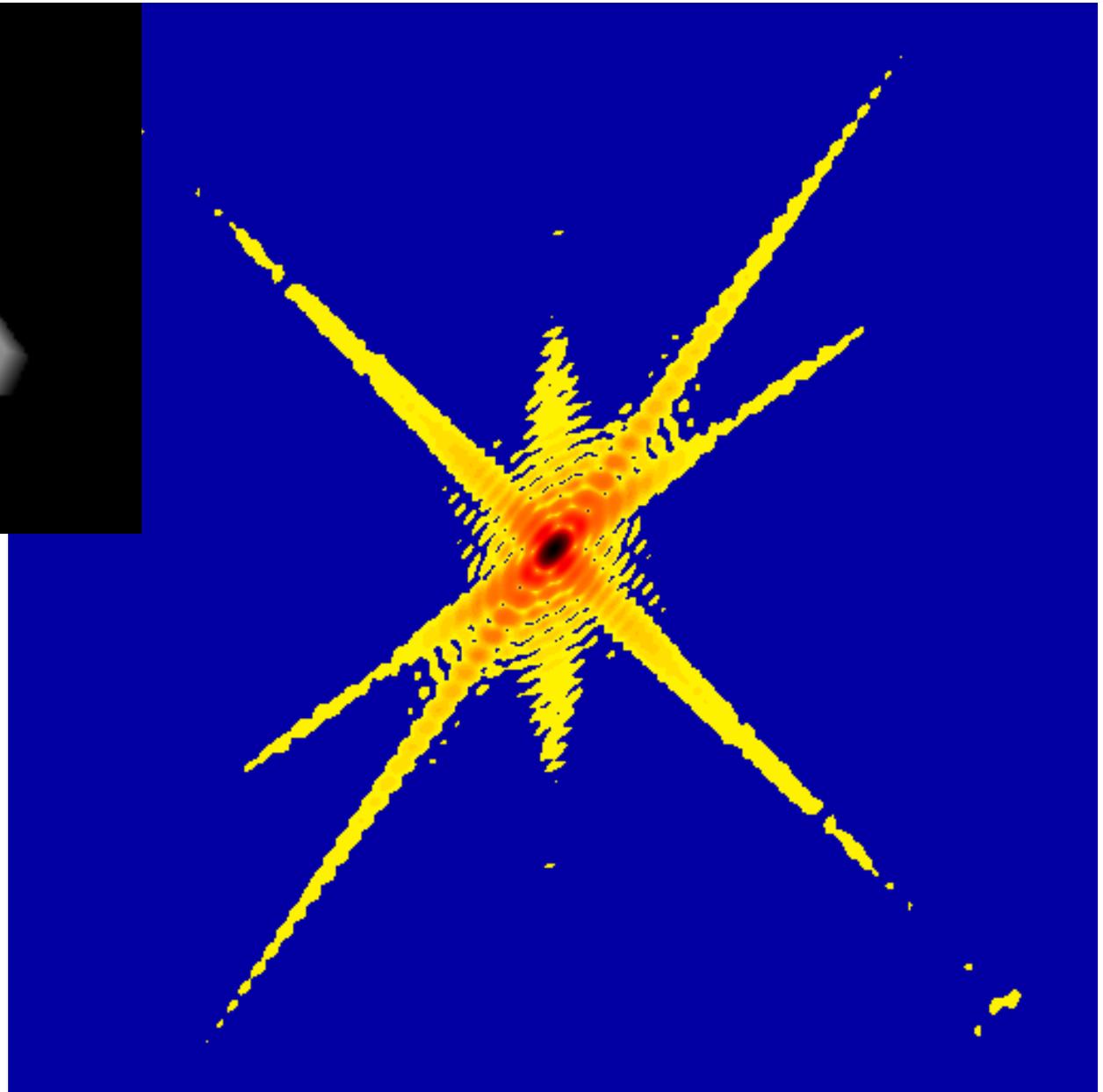
R. P. Millane, J. Opt. Soc Am. A **13** 725 (1996)

- ‘Positivity’ and ‘Atomicity’ constraints (Sayre)
- Finite **support**, molecular envelope
- Solvent flattening/Molecular replacement
- Non-crystallographic symmetry
- Non-uniqueness is ‘pathologically rare’ ( $d > 1$ )
- Uses memory to avoid stagnation (Fienup HIO)

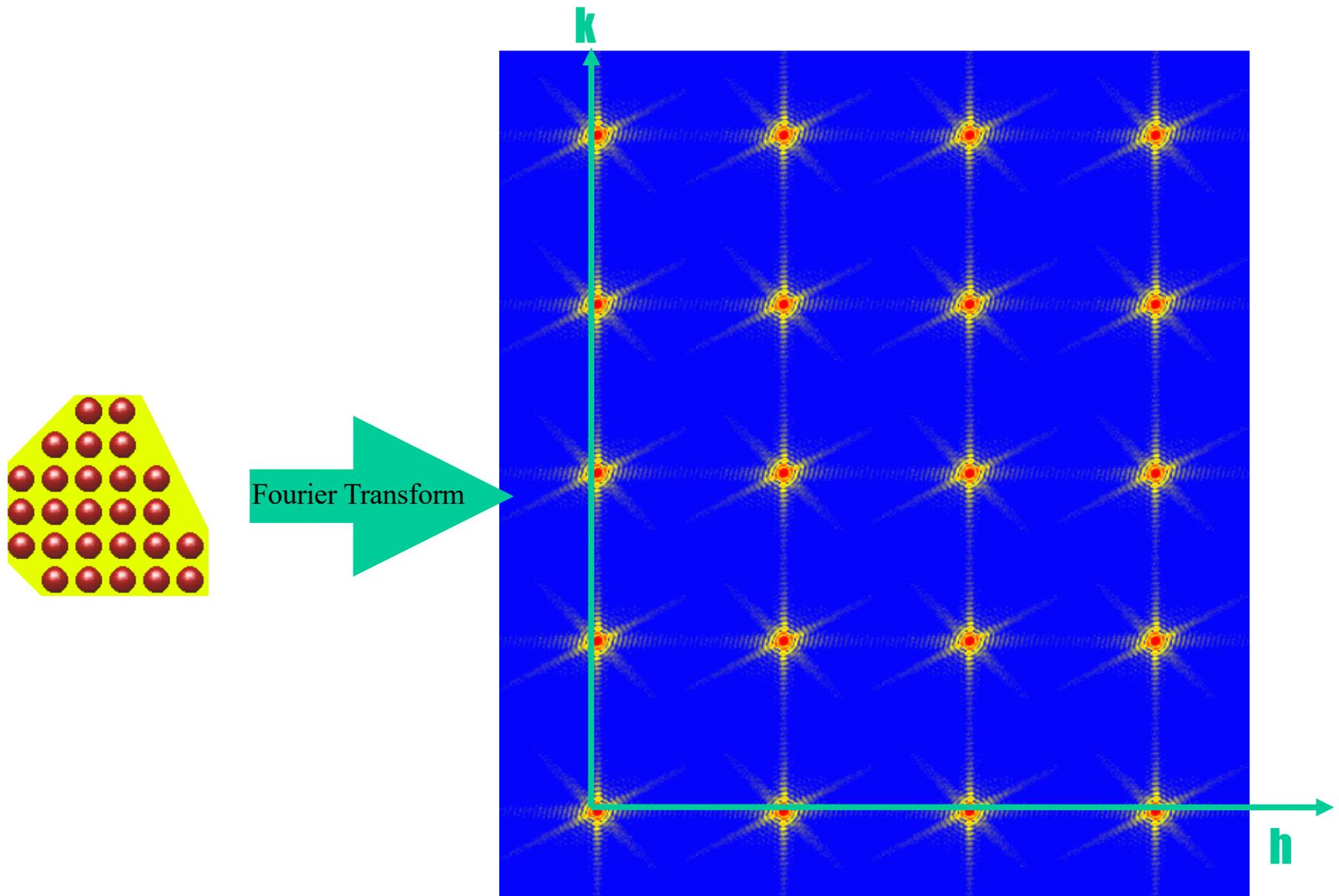
# Phase Problem: Finite-size Effect





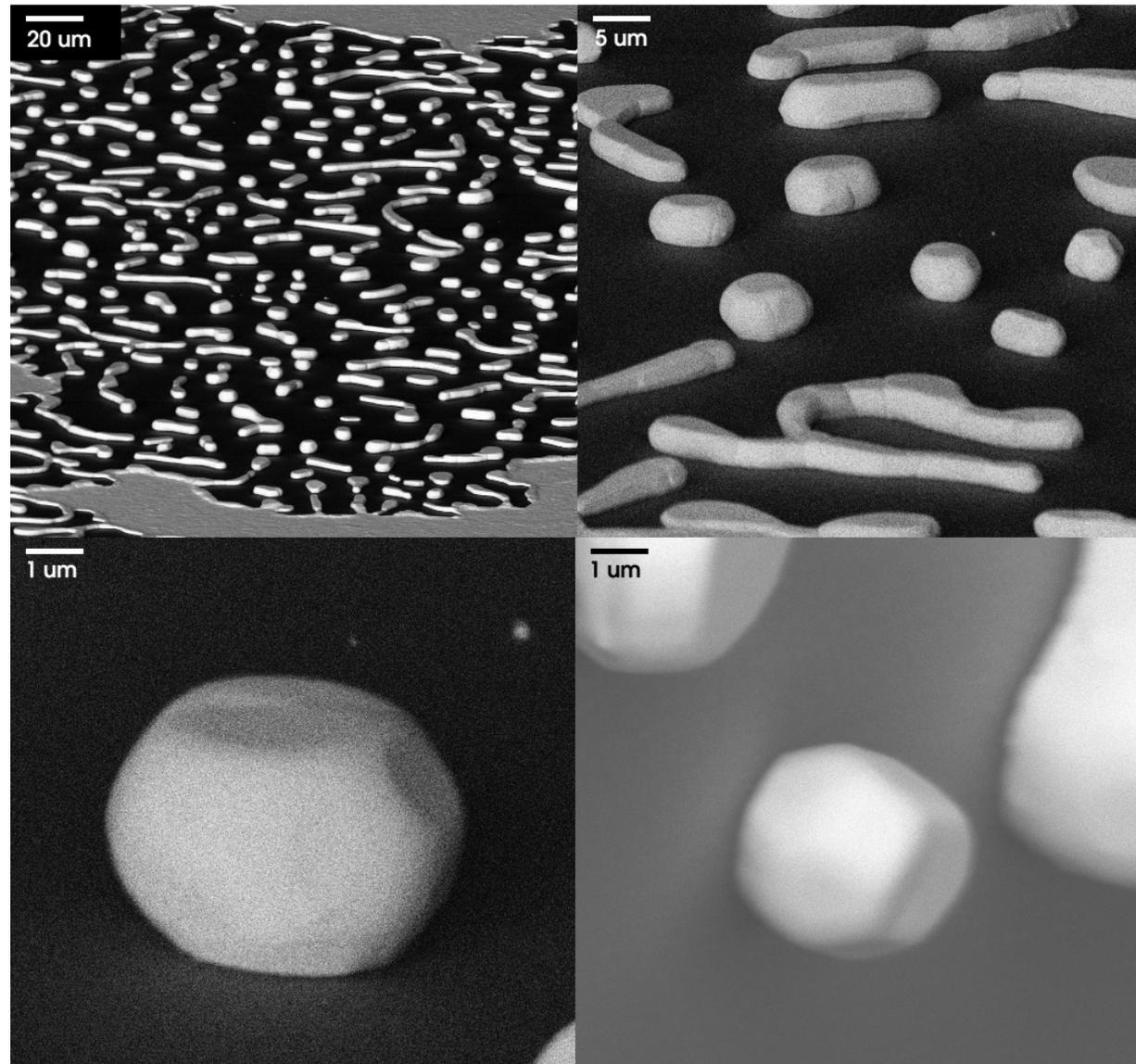


# Coherent Diffraction from Crystals



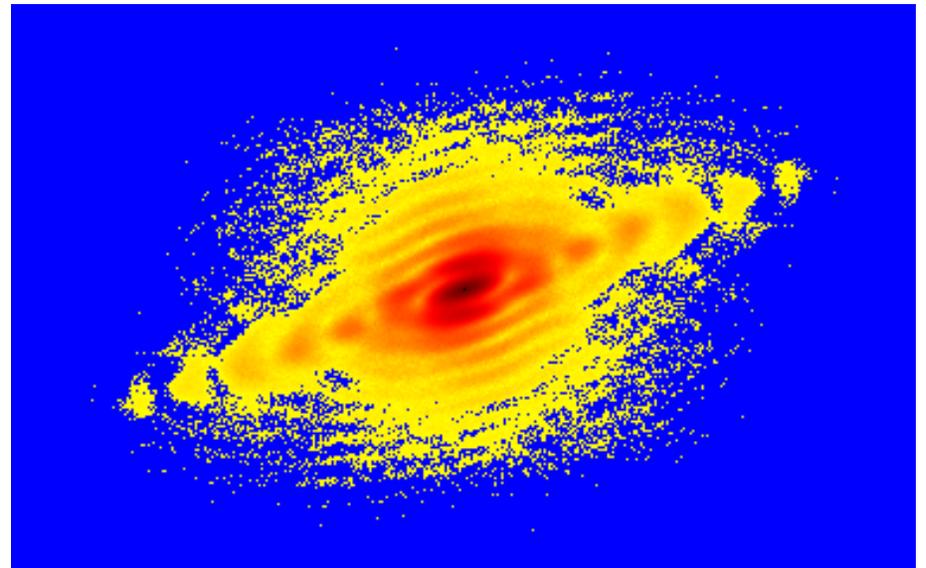
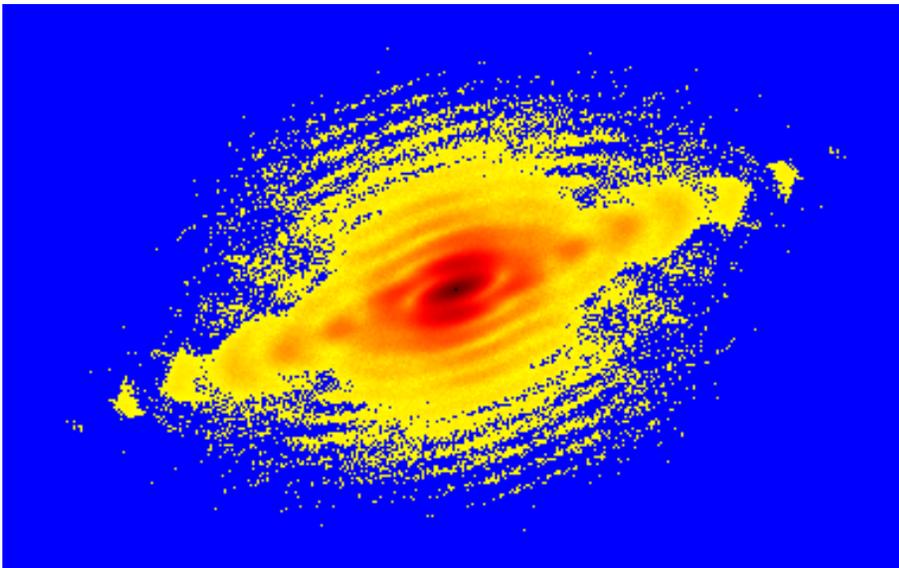
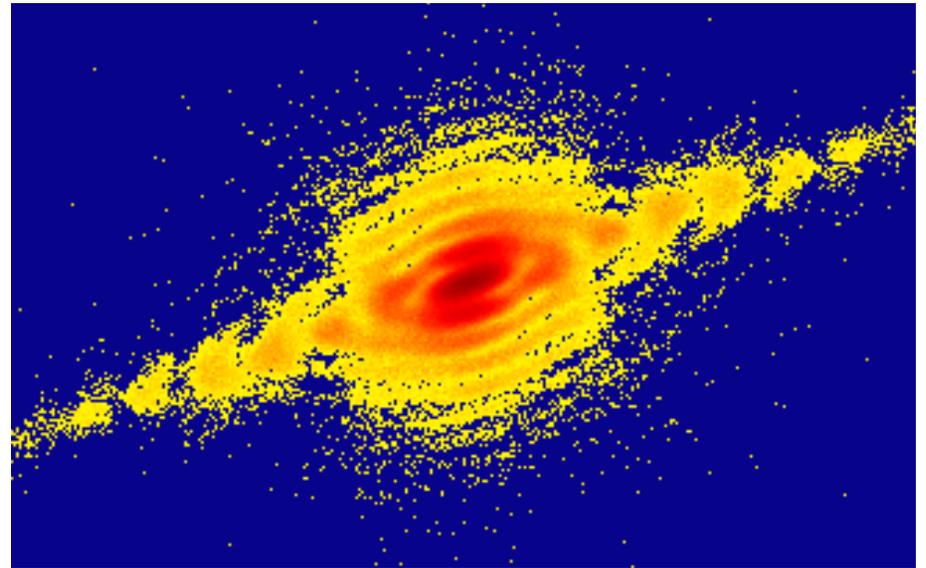
# SEMS

- Au blanket film
- Quartz substrate
- Annealed at 950°C for 70 hrs.



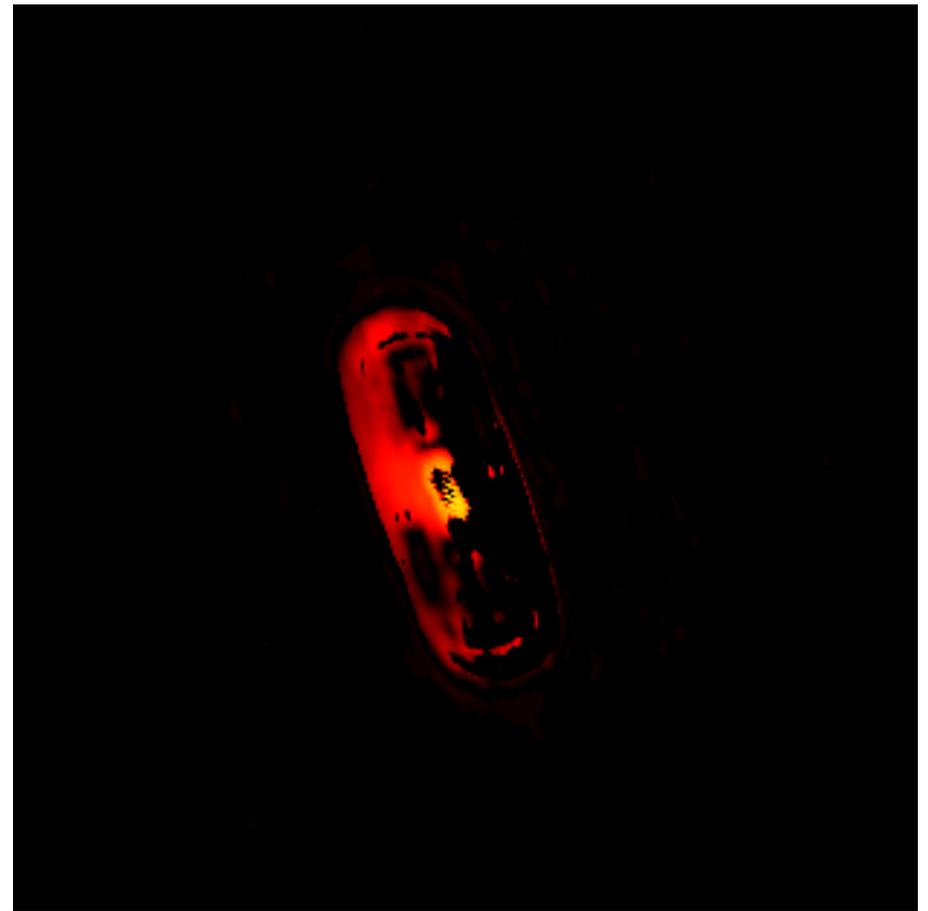
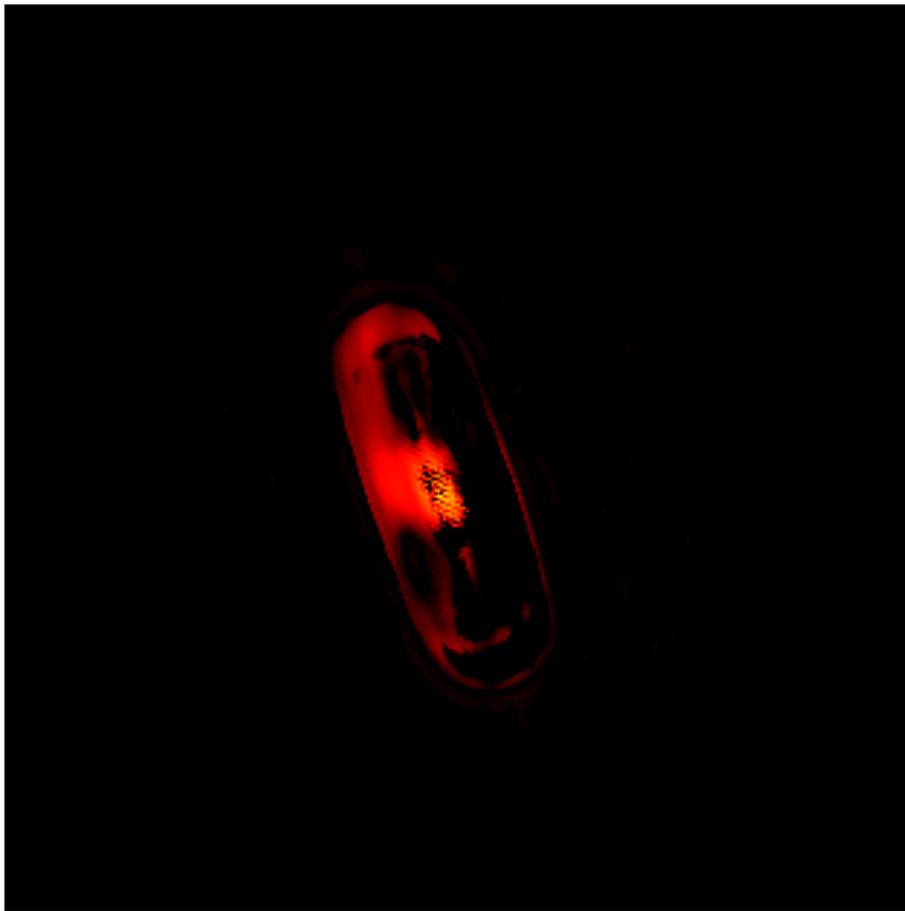
# Symmetrized Data and two best fits

Chisq=0.0005

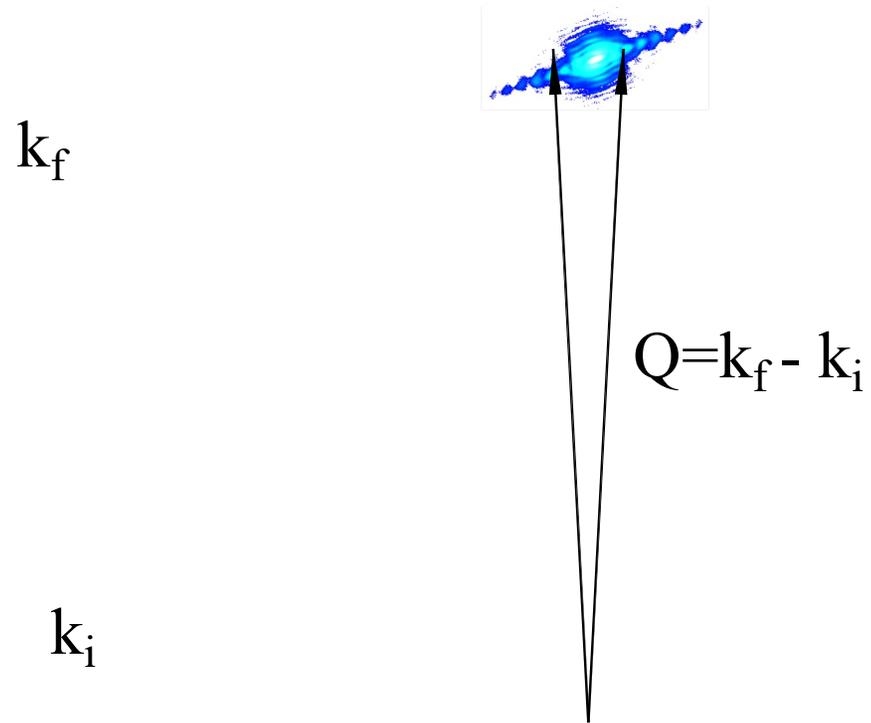


# 2D Reconstructions

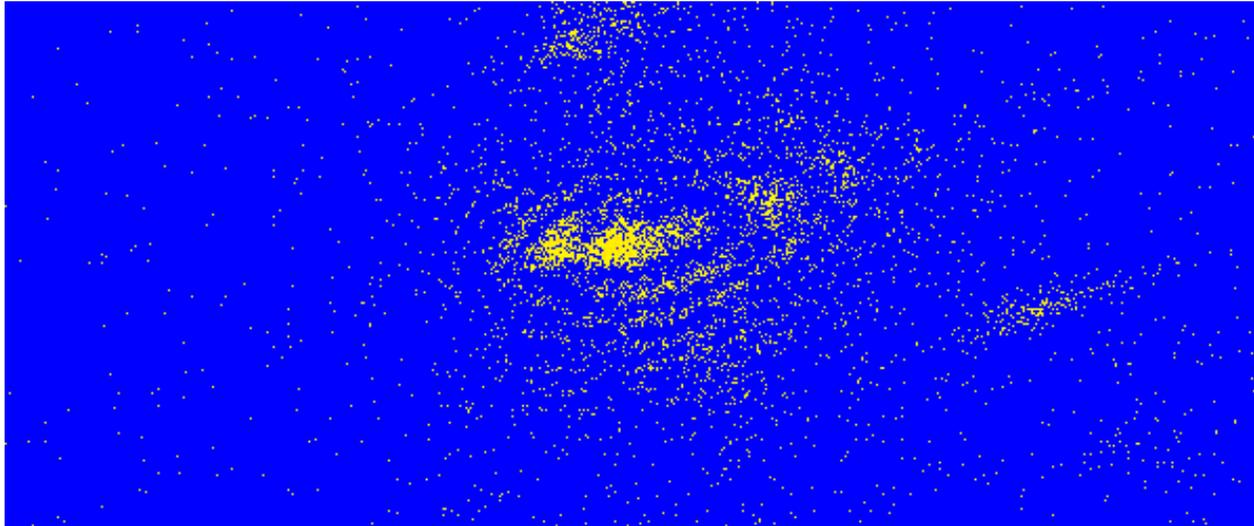
chisquare = 0.0005



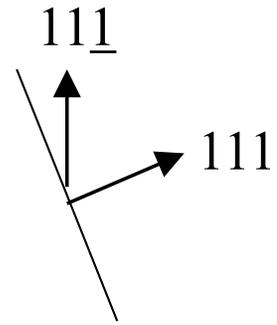
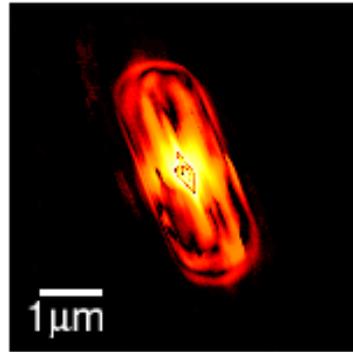
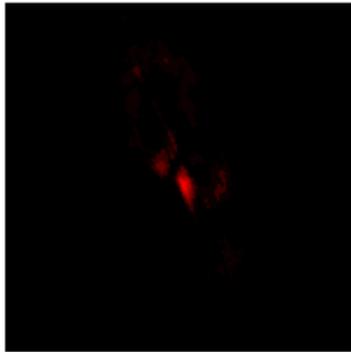
# 3D Diffraction Method



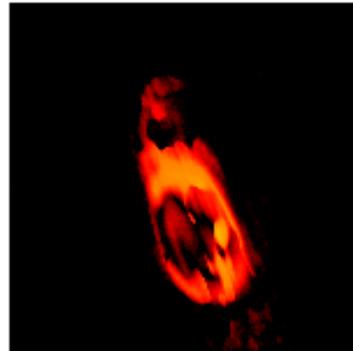
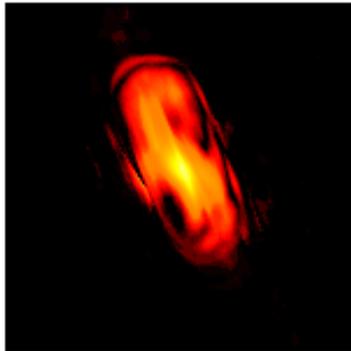
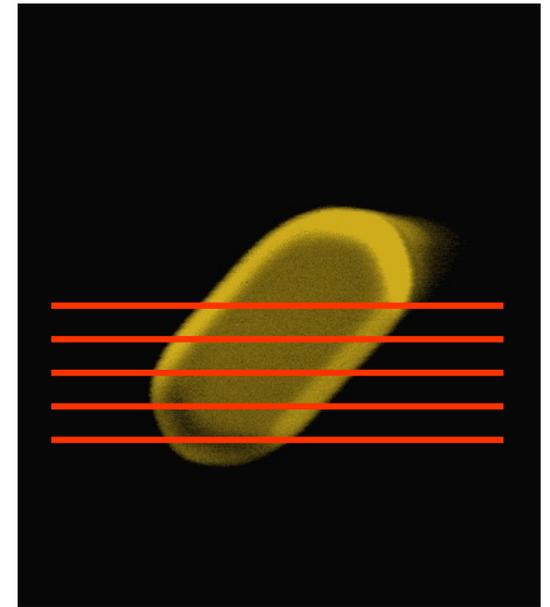
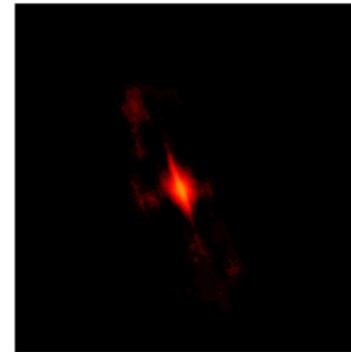
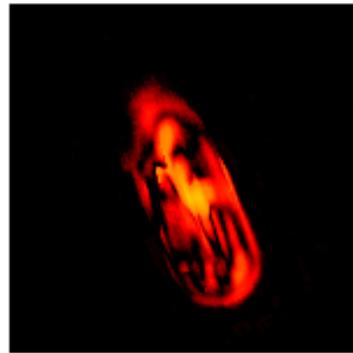
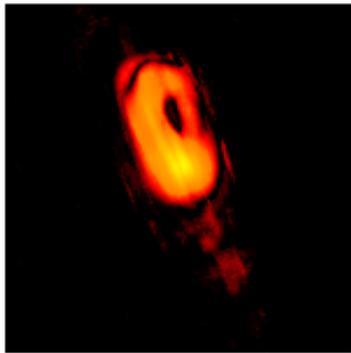
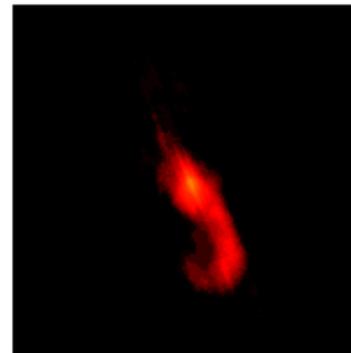
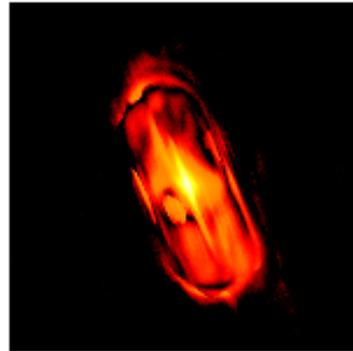
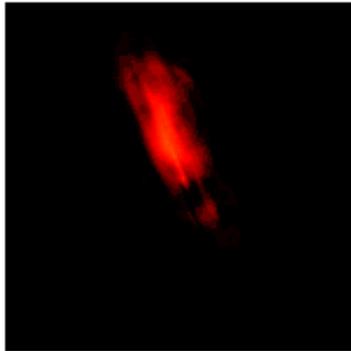
# 3D Diffraction Data 1 micron Au crystal



\* Center is Symmetric \*

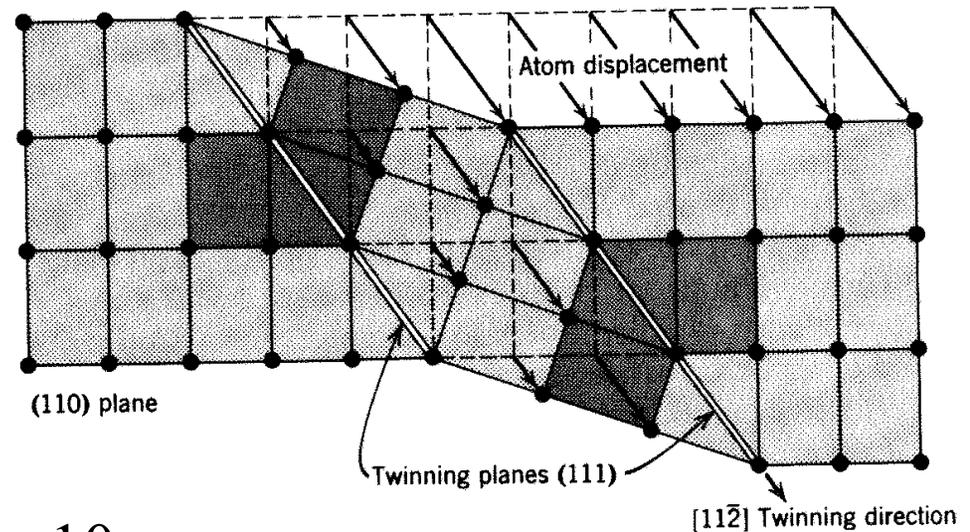
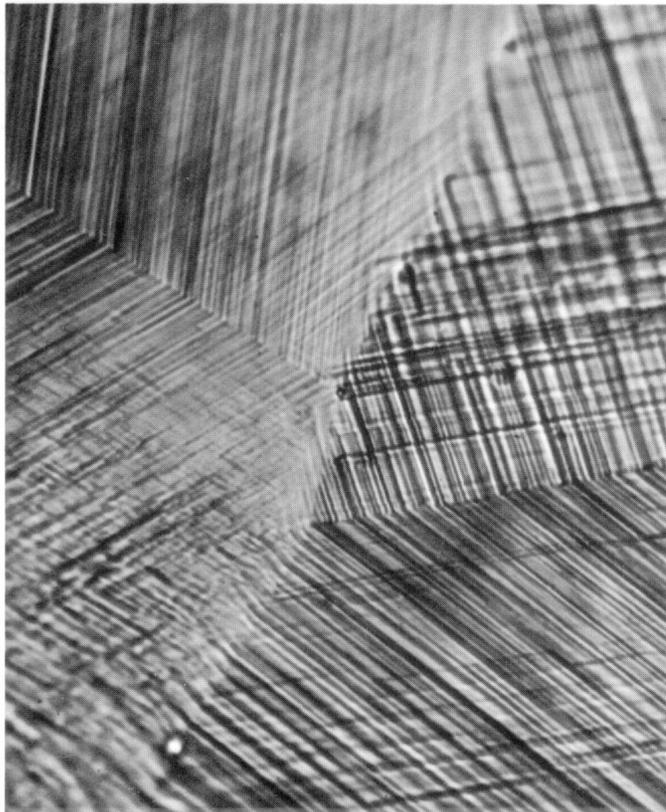


Slices through  
plan view SEM:

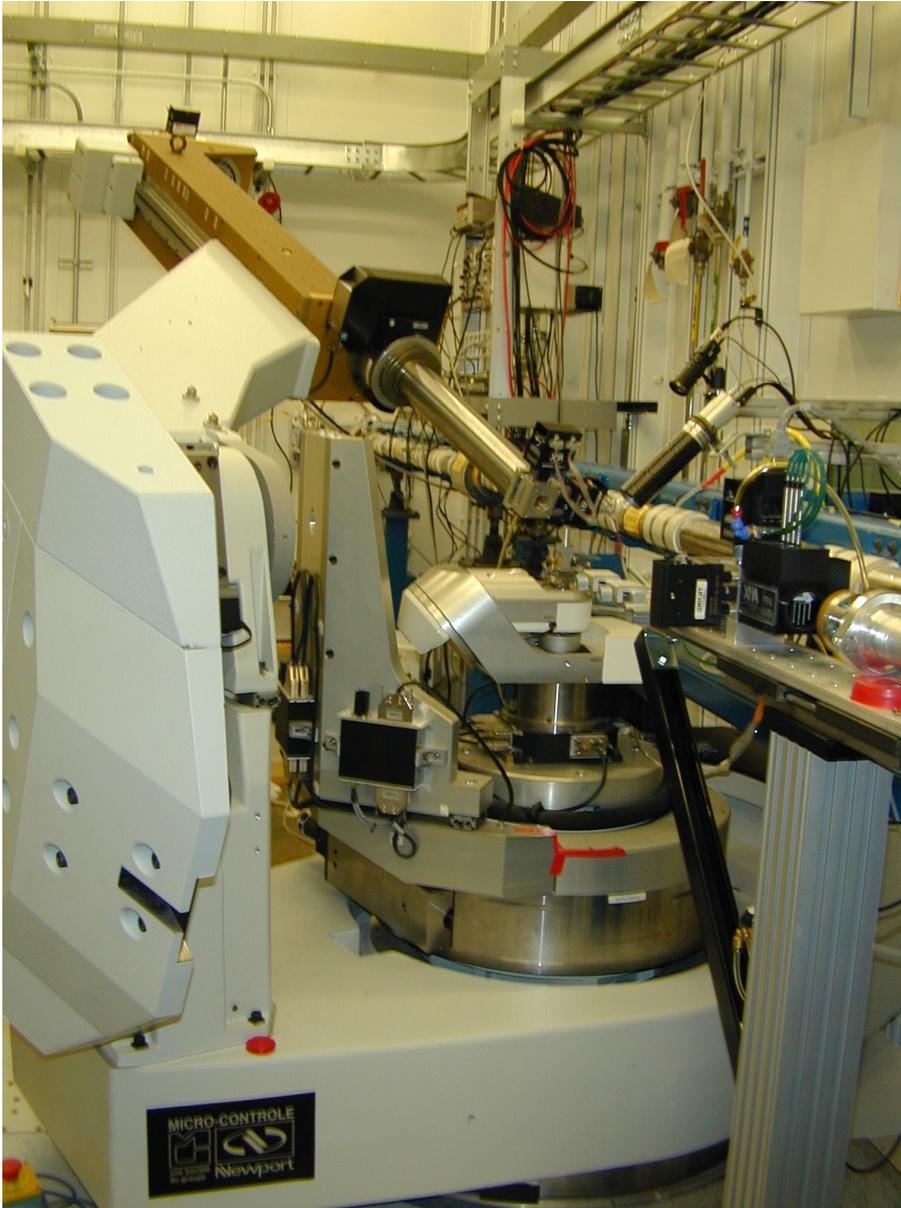


# Twinning in deformed FCC metals

J. Wulff, "Structure and Property of Materials III" (1965)

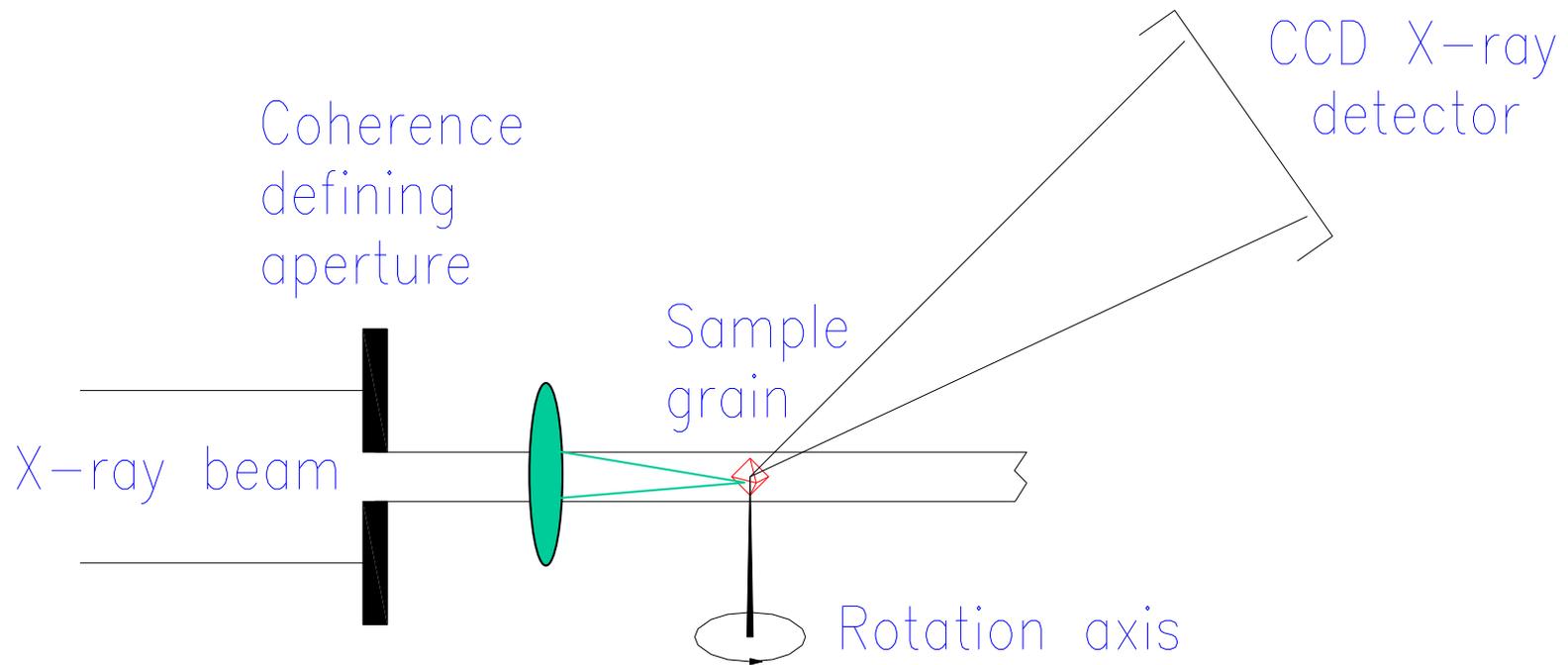


■  $\sim 10\mu\text{m}$   
Cu

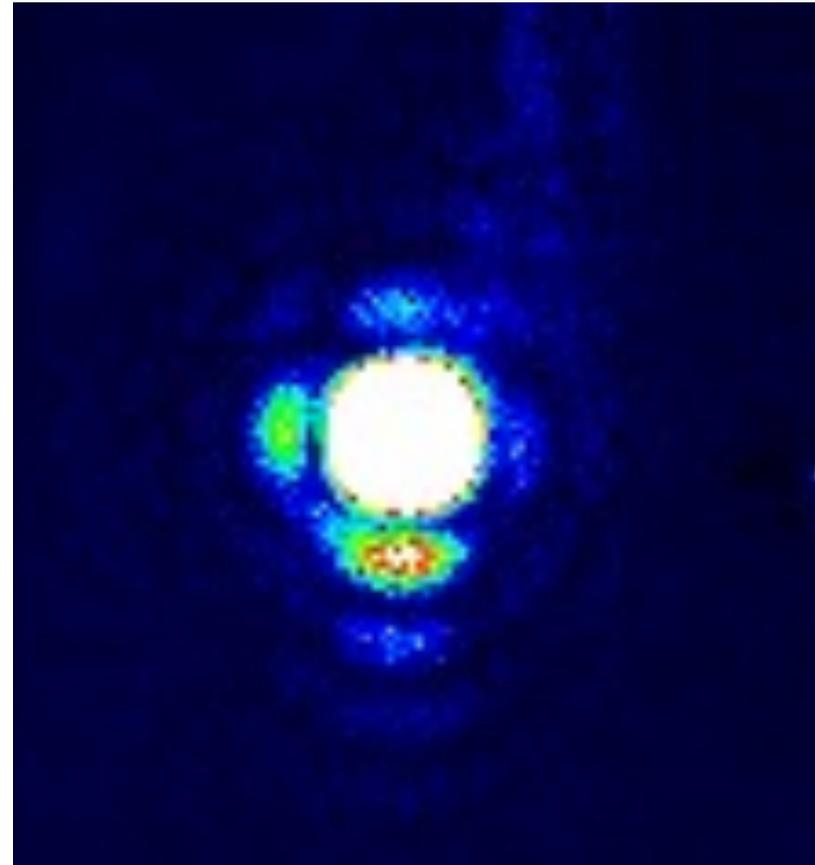
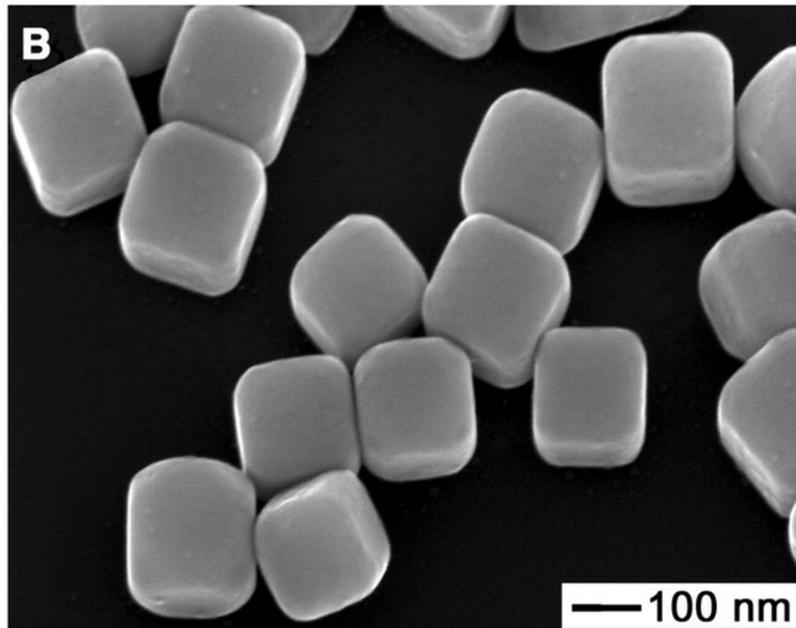


I. K. Robinson, VBL, Nagoya, Oct 2004

# Lensless X-ray Microscope

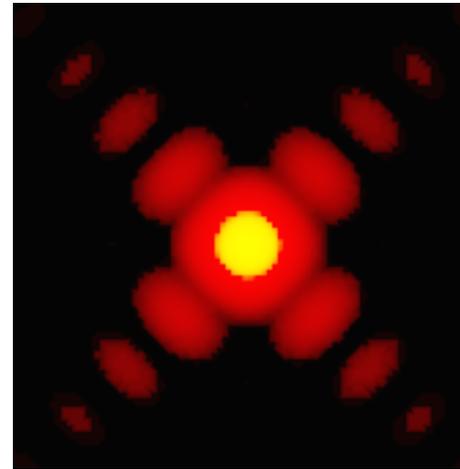
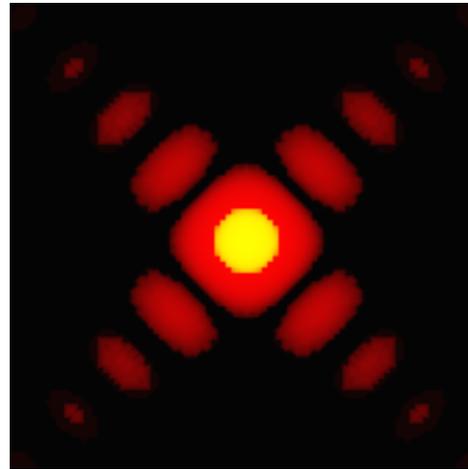


# CXD from Silver Nanocubes



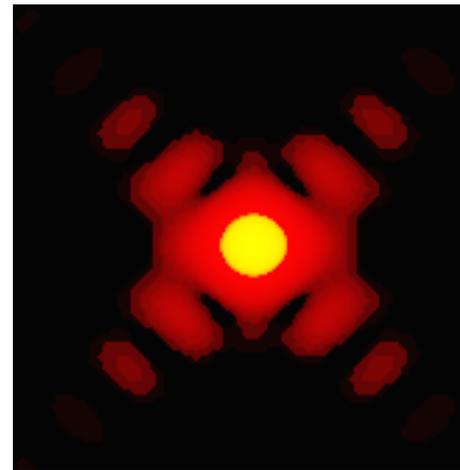
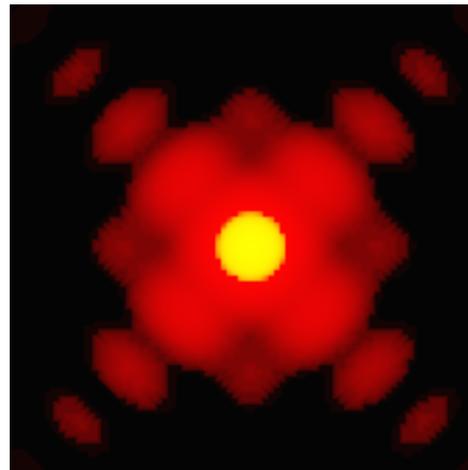
Yugang Sun and Younan Xia,  
*Science* 298 2177 (2003)

# Spherical and cylindrical waves



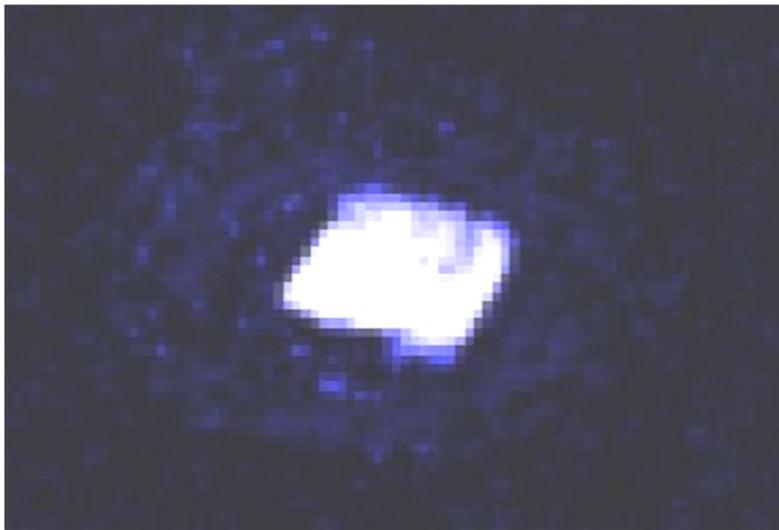
$\pi/4$

$\pi/2$

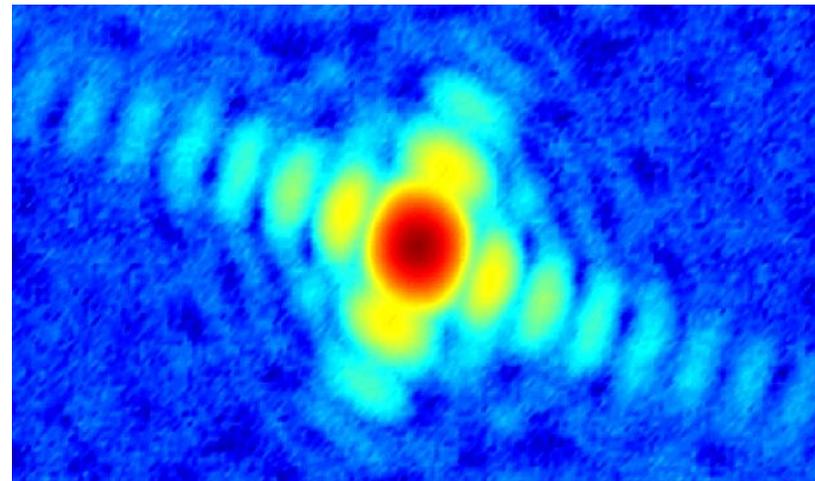
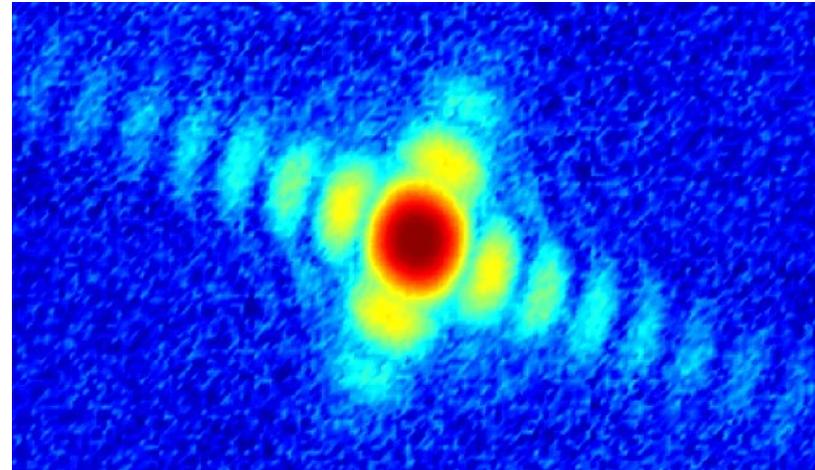


$\pi/4$  (x)

# Reconstruction of Ag Nanocrystal

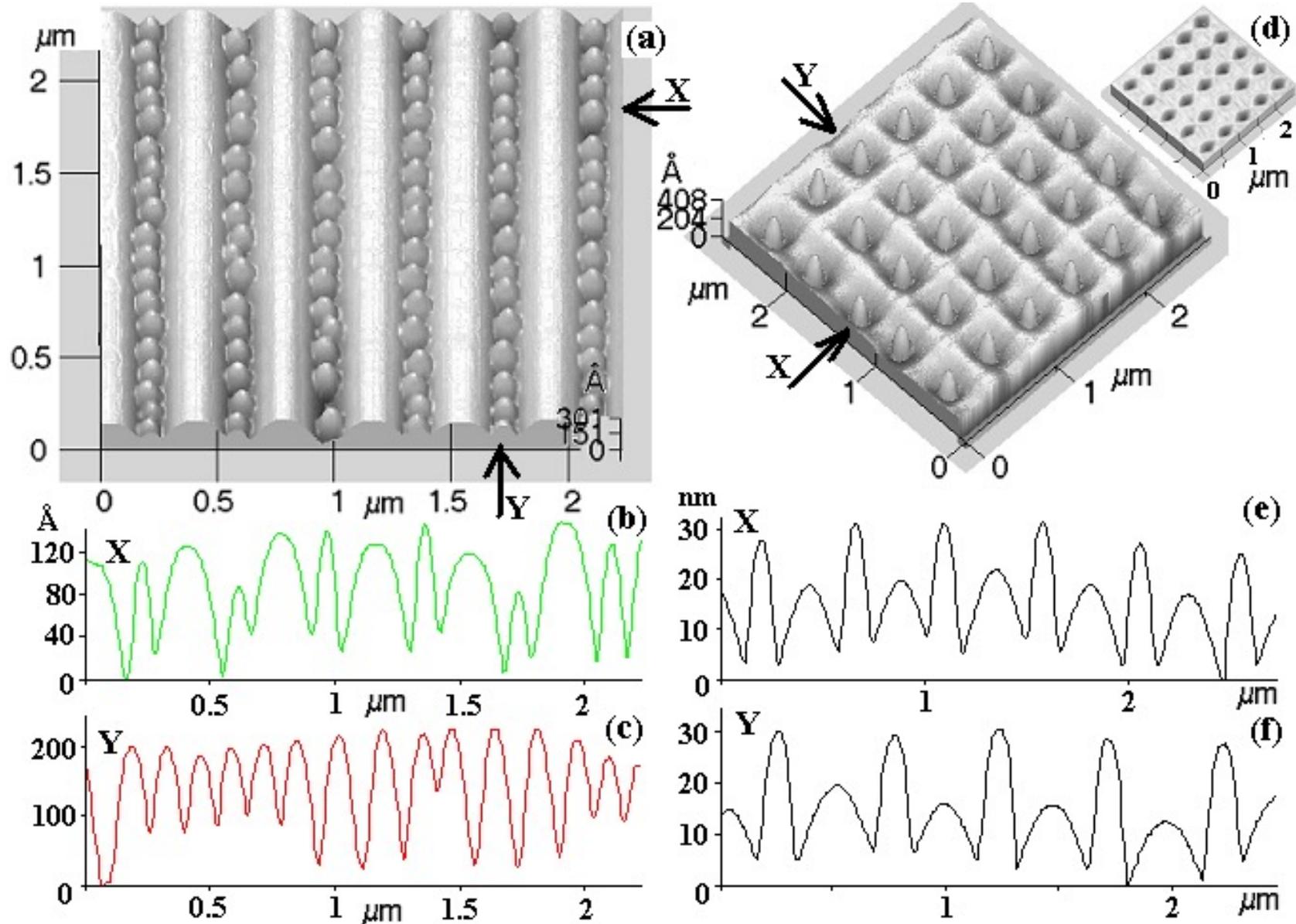


←→  
200nm



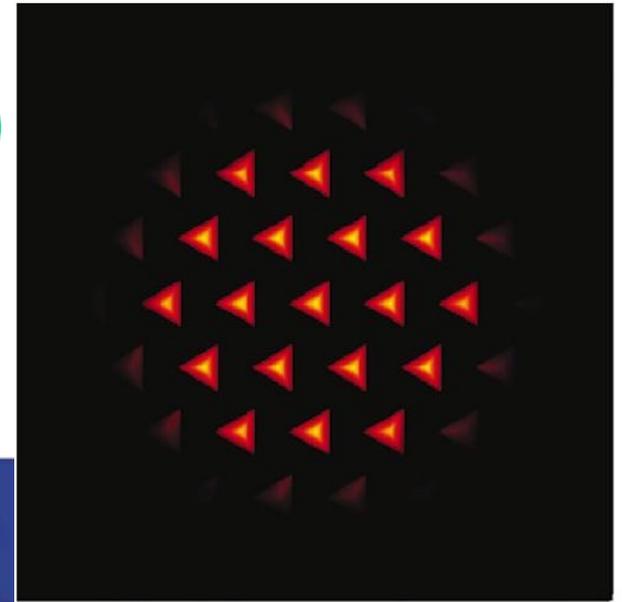
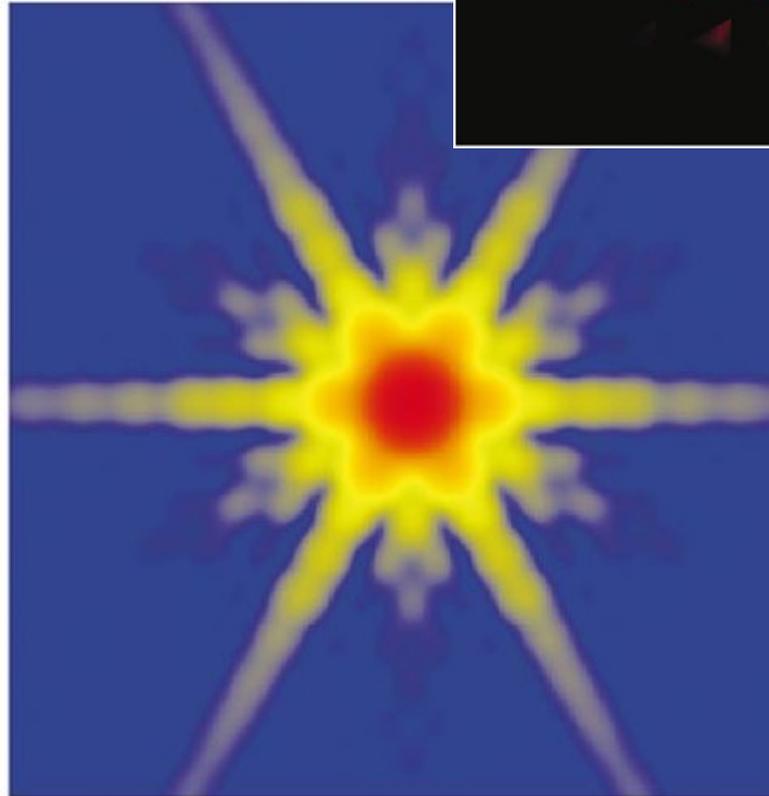
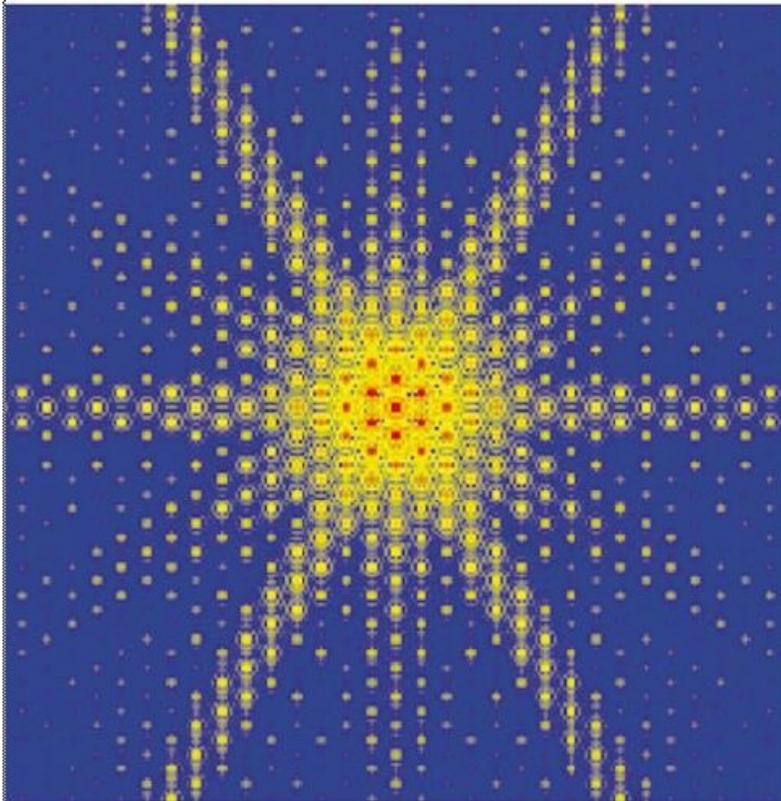
# 1D and 2D Quantum Dot Arrays

Zhenyang Zhong, G. Bauer, Johannes Kepler Universität Linz



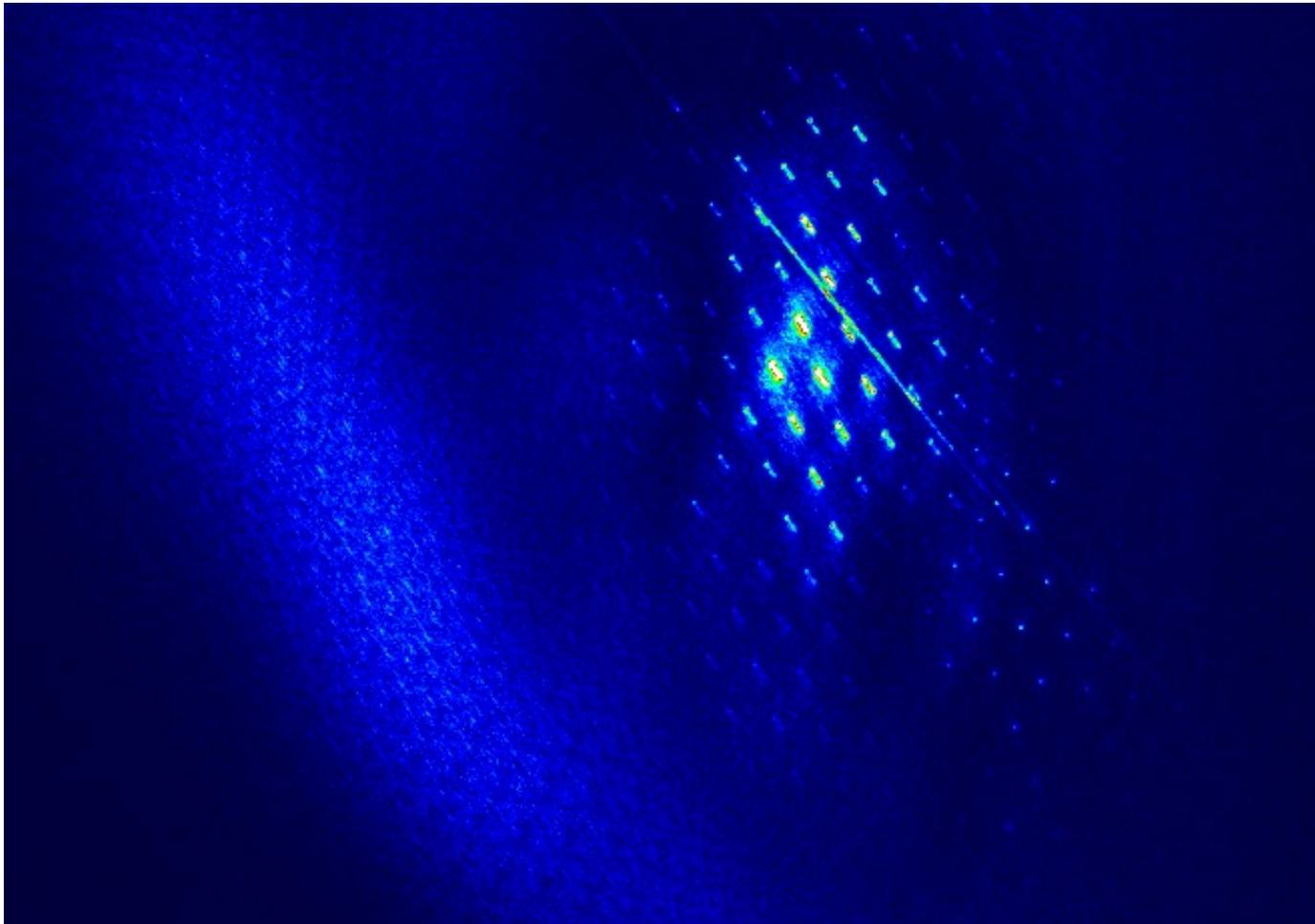
# Vary Coherence (model)

I. A. Vartanyants and I. K. Robinson,  
J. Sync. Rad. **10** 409 (2003)

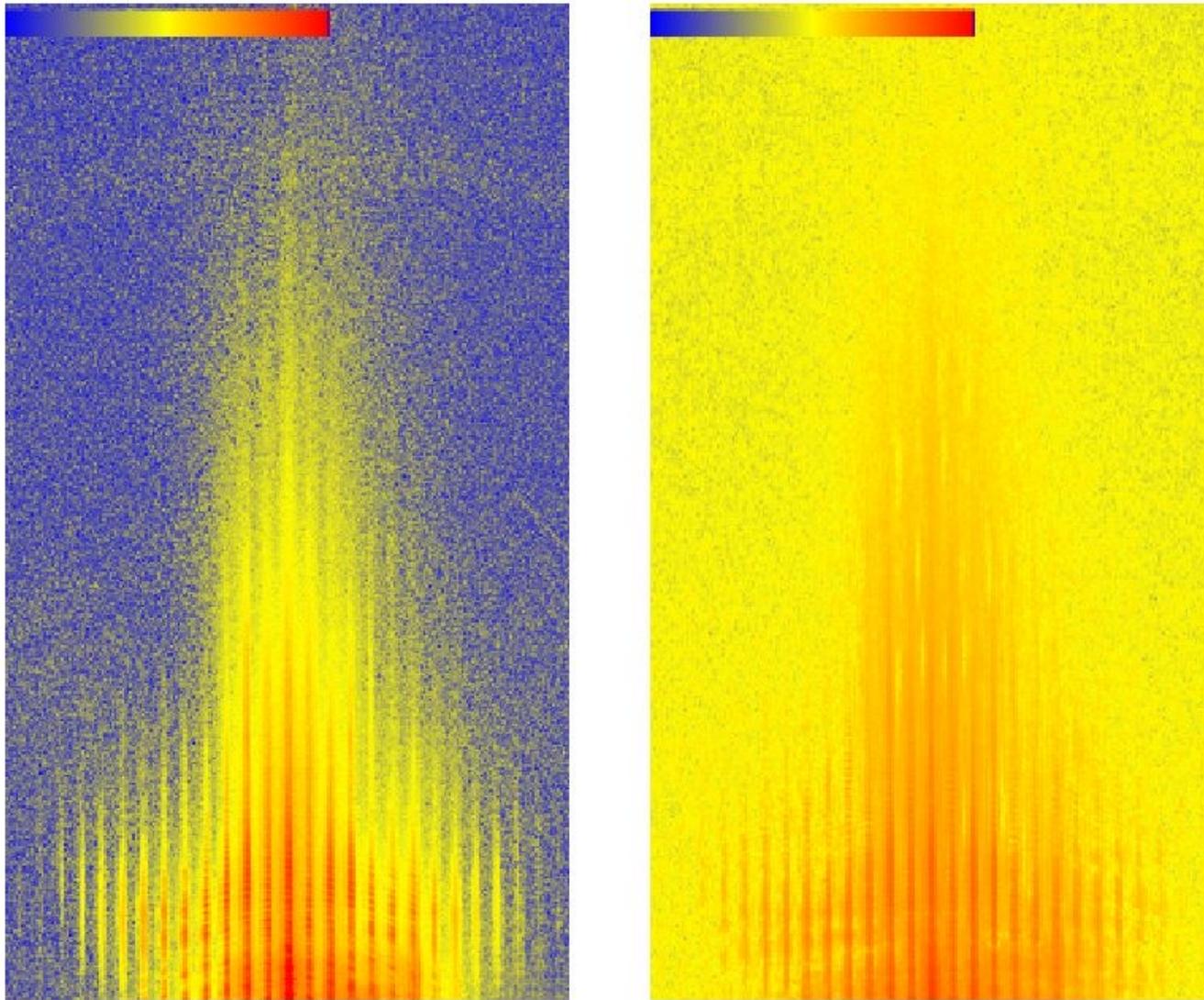


# 202 Diffraction from Ge QD array

with G. Bauer, Z. Zhong and T. H. Metzger



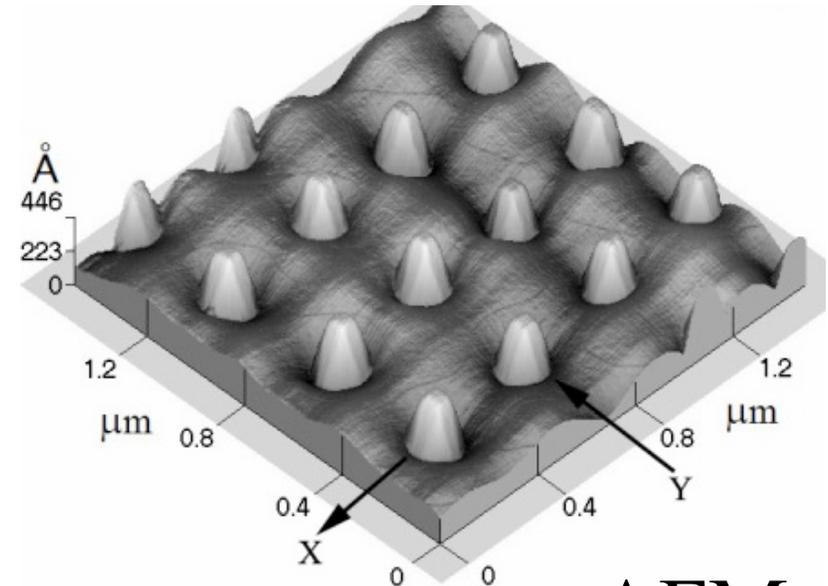
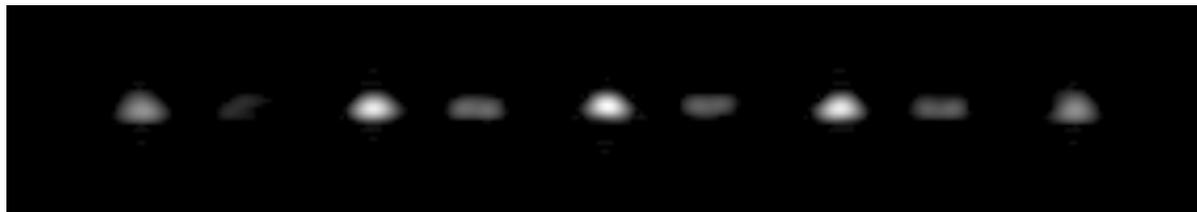
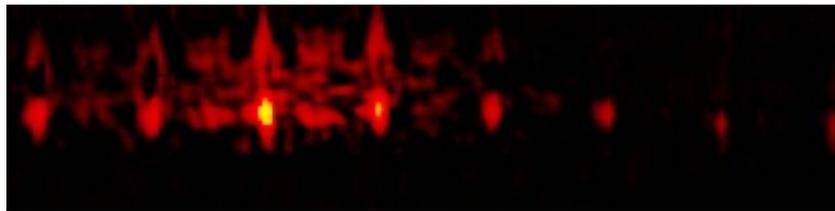
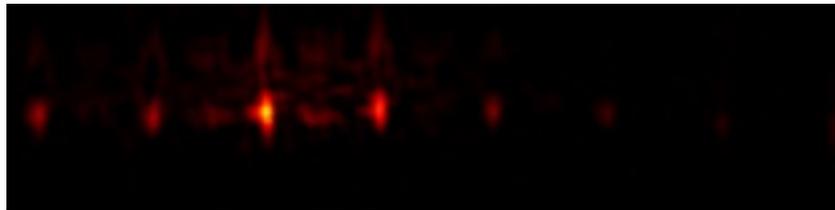
# Result of fitting GISAXS data



I. K. Robinson, VBL, Nagoya, Oct 2004

# Images from Fitting GISAXS

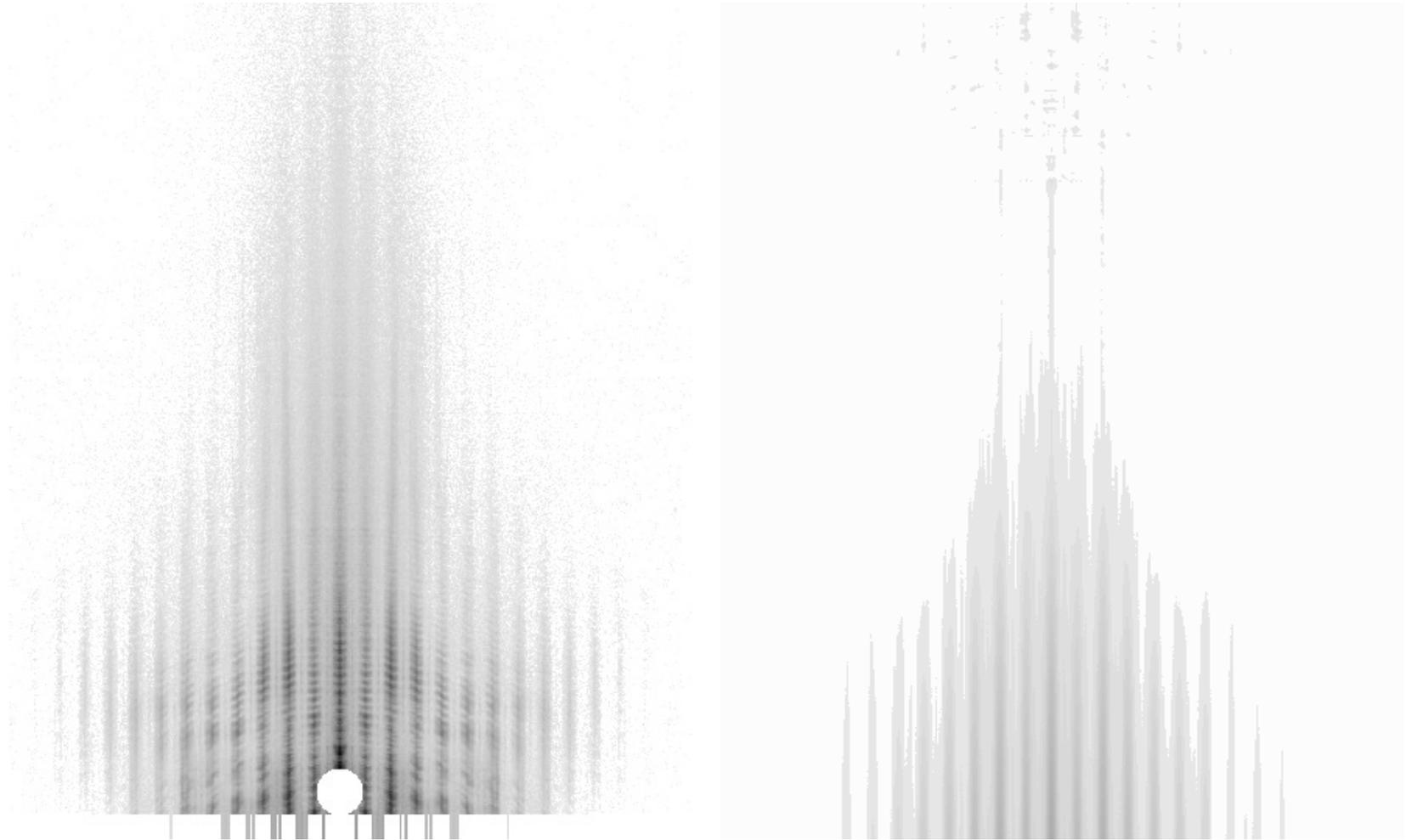
with Jeff Onken



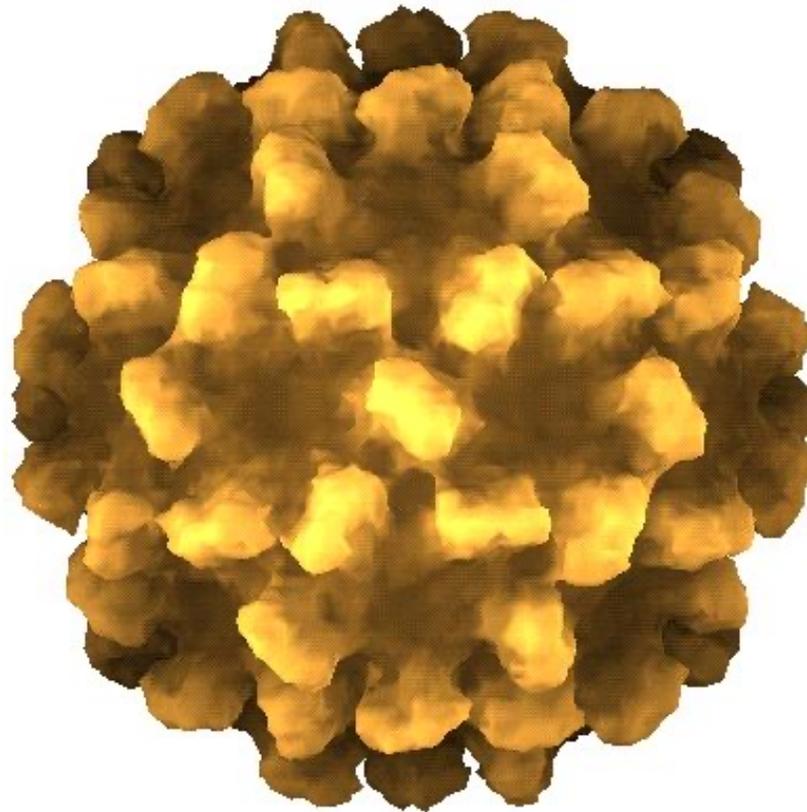
AFM

Mask used  
as support

# Diffraction pattern under constraint



# Tomato Bushy Stunt Virus 1980



# Conclusions and Outlook

- Direct inversion of CTRs for heterostructures
- Inversion of CXD demonstrated also
- Internal structure of Au Nanocrystals
- Preservation of coherence upon focussing
- Simple Quantum Dot structures possible now
- Single molecules one day