

# Coherent X-ray Diffraction imaging of strain fields in Nanocrystals

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Harwell Research Complex

East Midlands Materials Society,

Leicester, February 3, 2011

# Outline

- Coherent x-ray diffraction
- CXD can solve the **phase** problem
- Nanocrystal structures
- Crystal strain as complex density
- Nanowire structures
- Full strain tensor

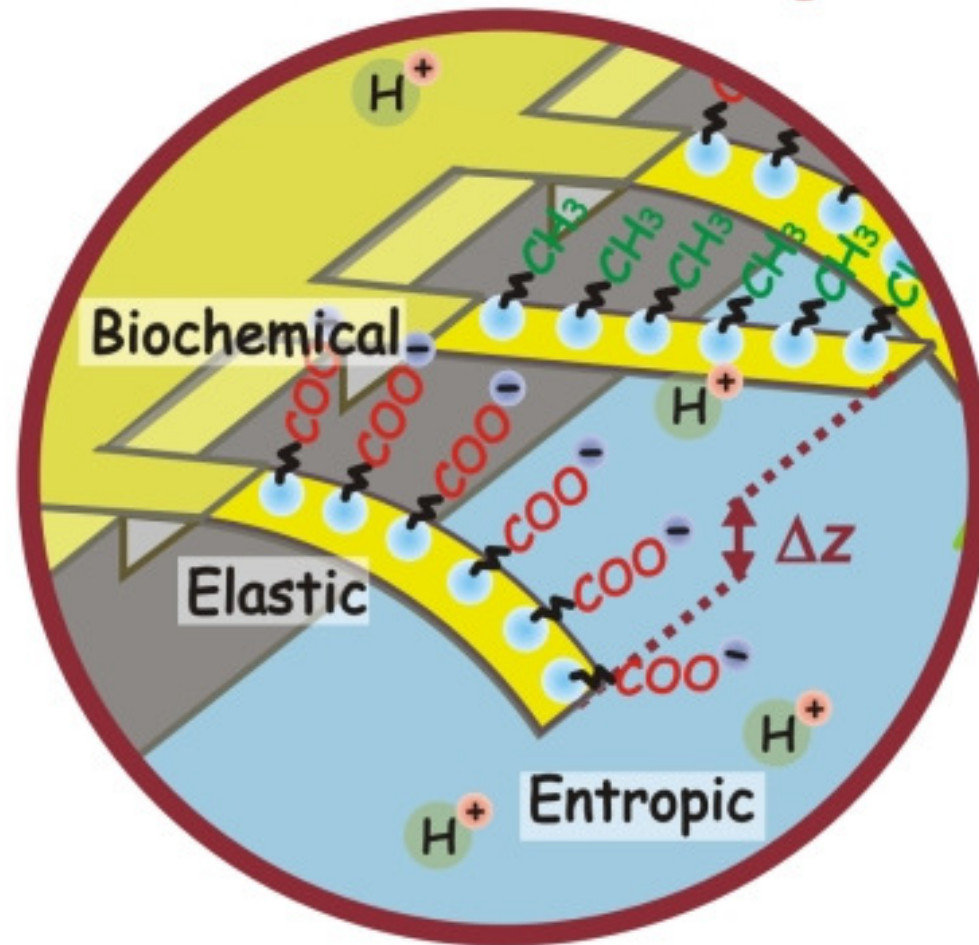
# London Centre for Nanotechnology

- Clean Rooms
- Low-T STM
- Lithography
- 3-beam FIB
- Visualisation
- CLS?



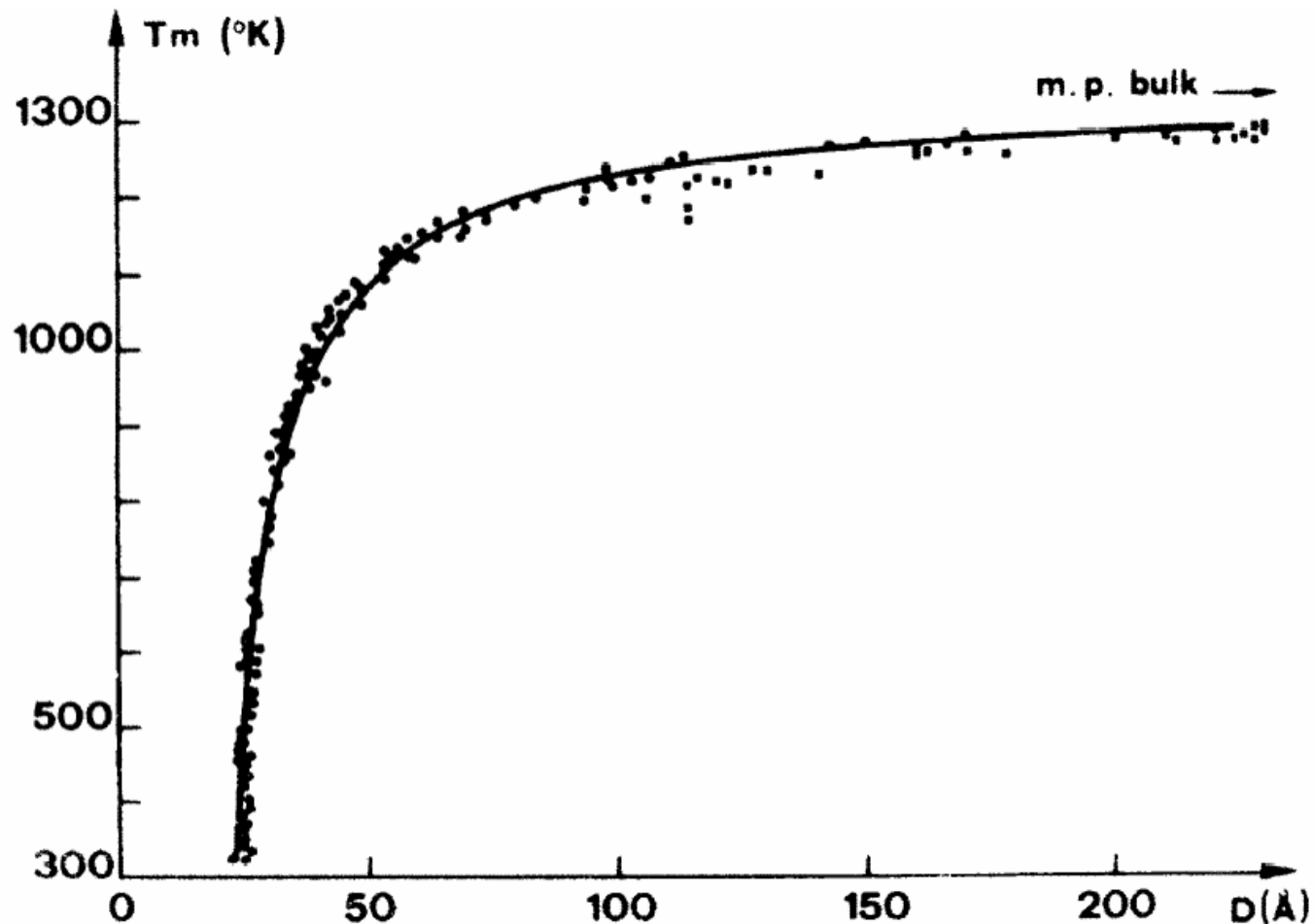
# Nanocantilevers

Dr Rachel McKendrie

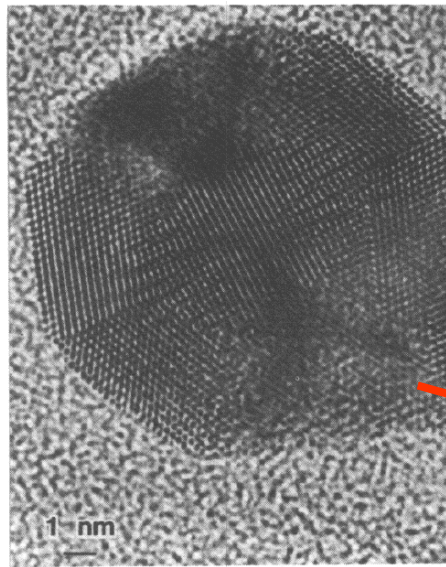


# Size-dependent Melting of Au Particles

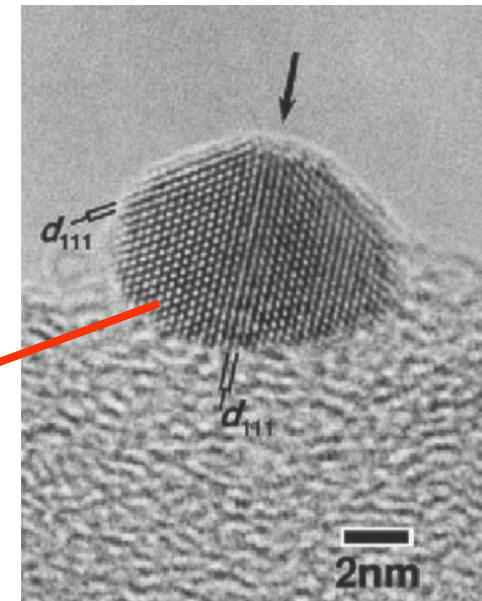
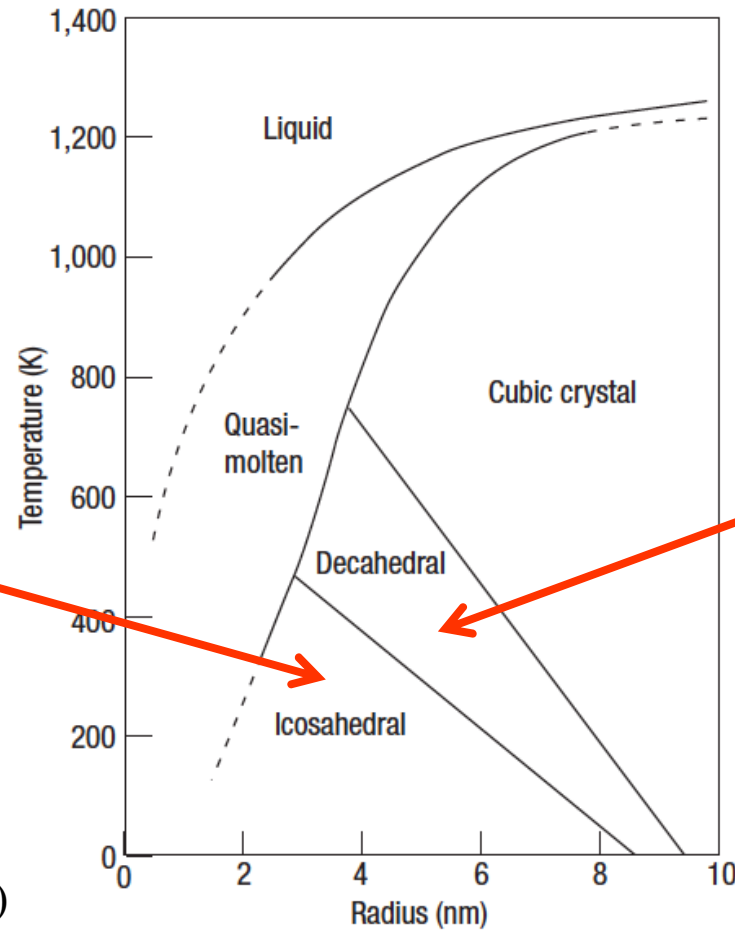
P. Buffat and J-P. Borel, Phys. Rev. A 2287-97 (1975)



# Structure of Gold vs Size

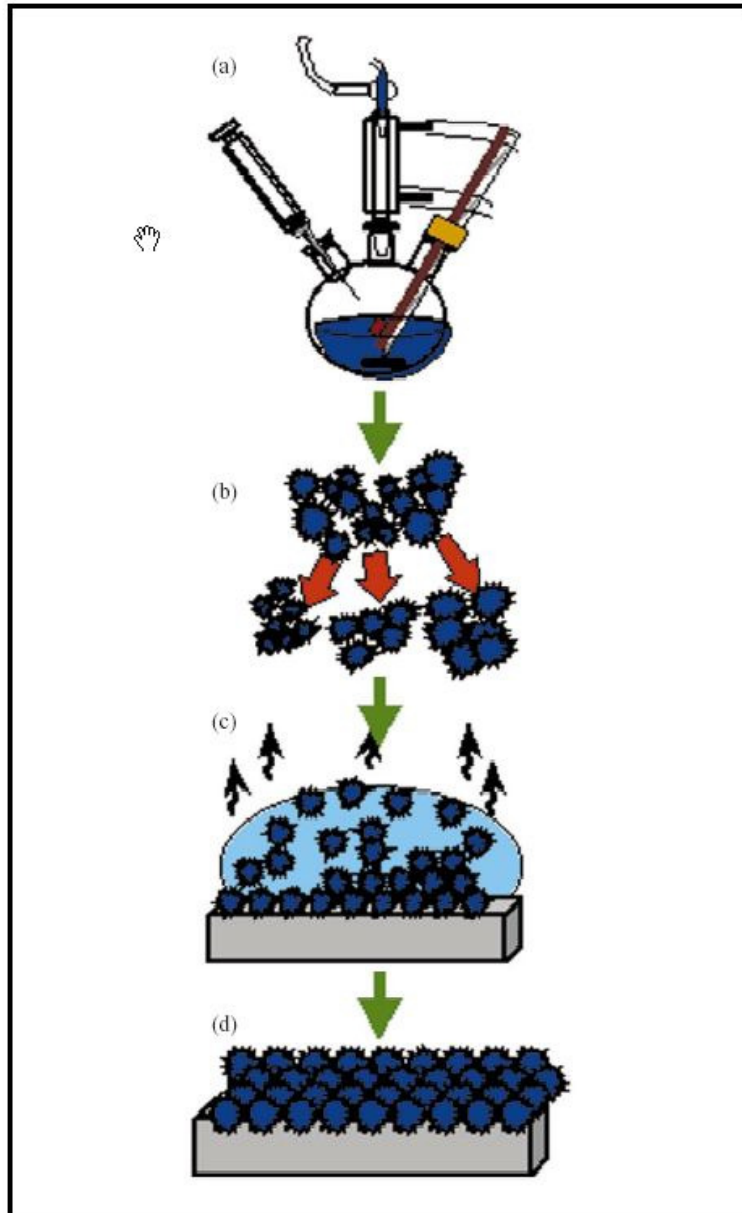


L. D. Marks, RPP (1994)



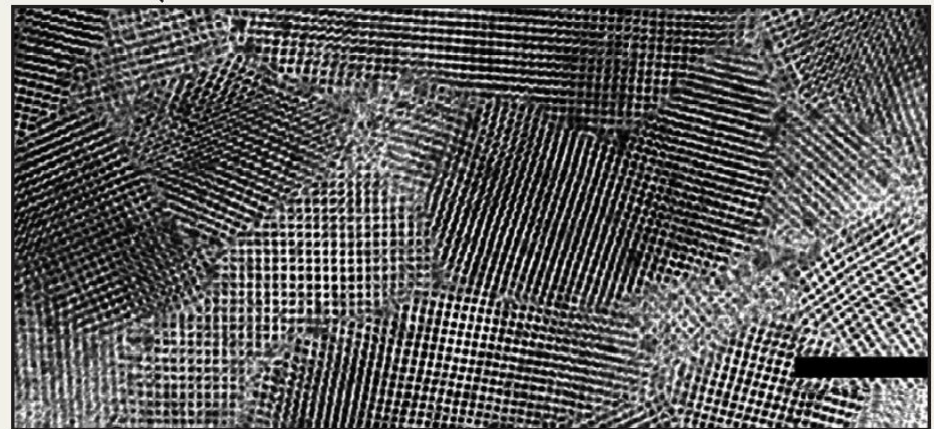
Koga and Sugawara (2003)

# Chemical Synthesis of Nanocrystals



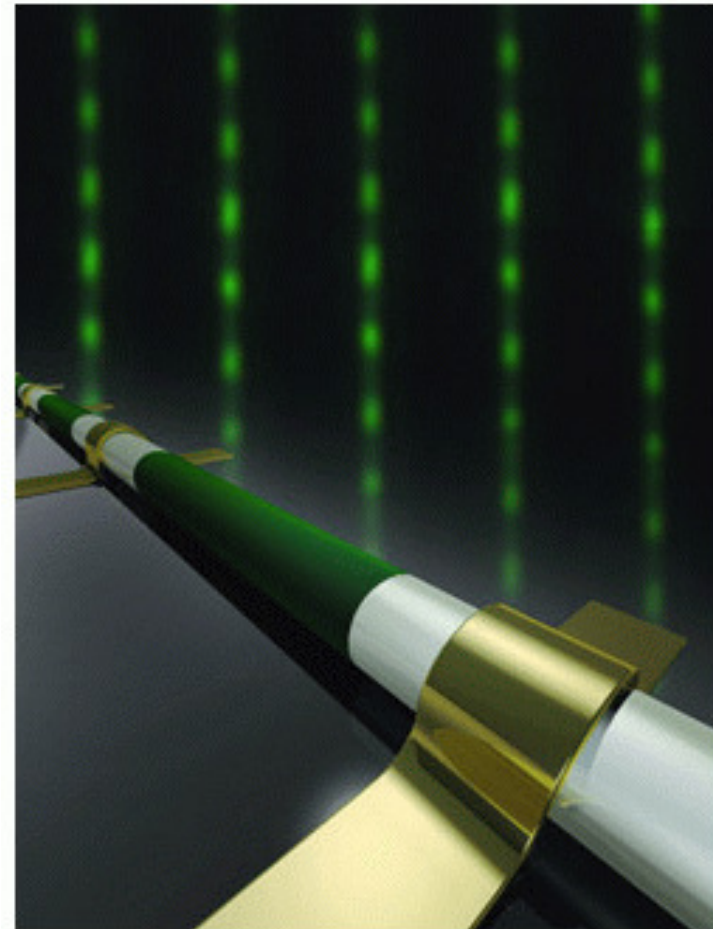
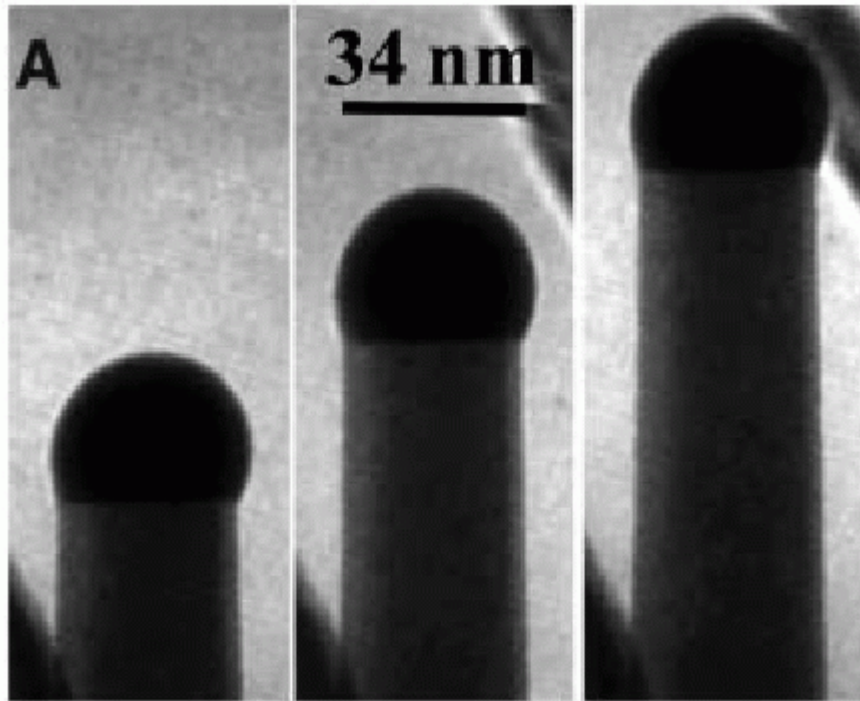
- Reactants introduced rapidly
- High temperature solvent
- Surfactant/organic capping agent
- Square superlattice (200nm scale)

C. B. Murray, IBM J. Res. & Dev.  
45 47 (2001)



# VLS growth of nanowires

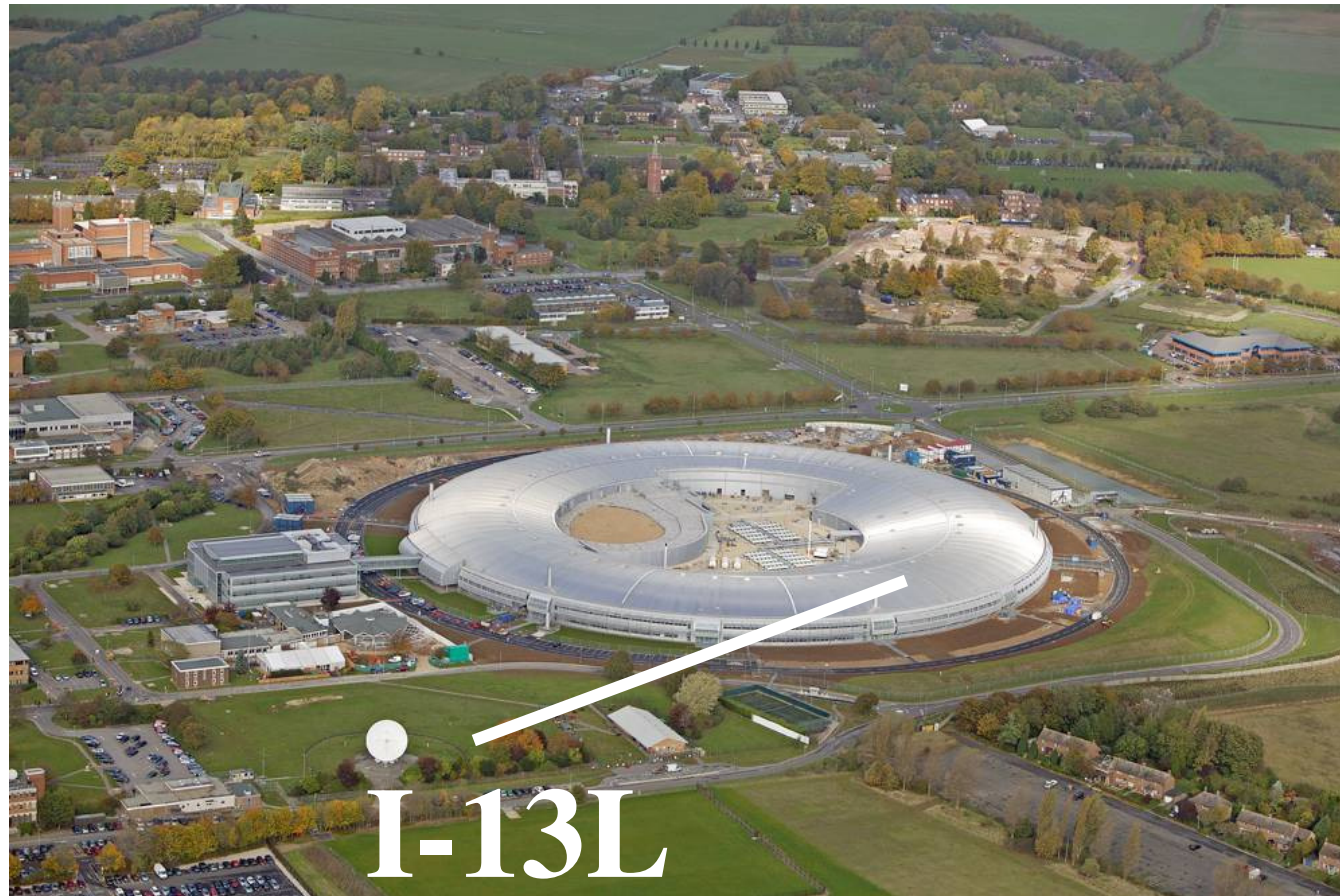
S. Kodambaka et al., *Science* 316 729 (2007)



I. K. Robinson, EMM

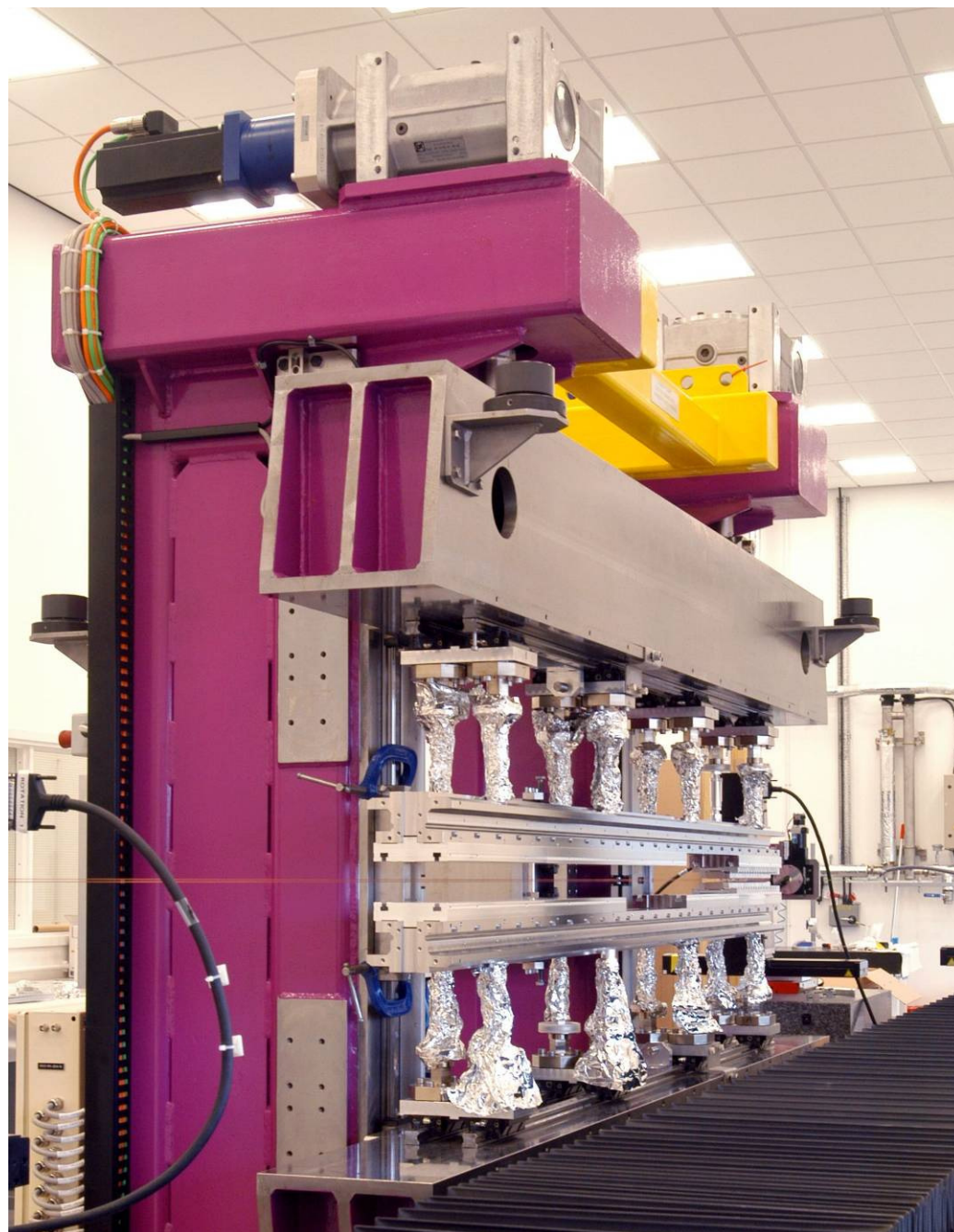
NiSi/Si nanowire heterostructure devices. *Nature* **430**, 61 (2004).

# Diamond Light Source (RAL)

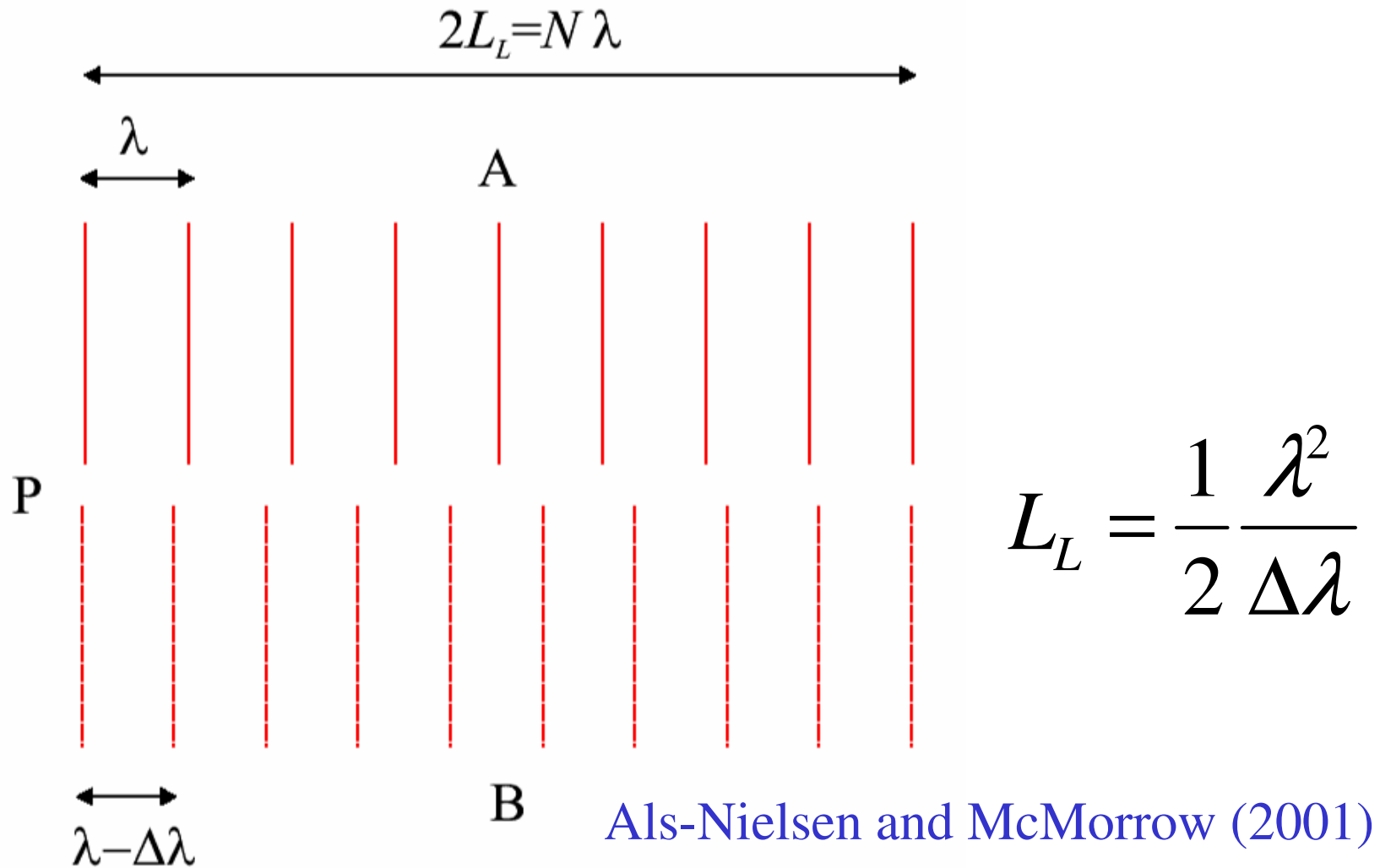


i-13L

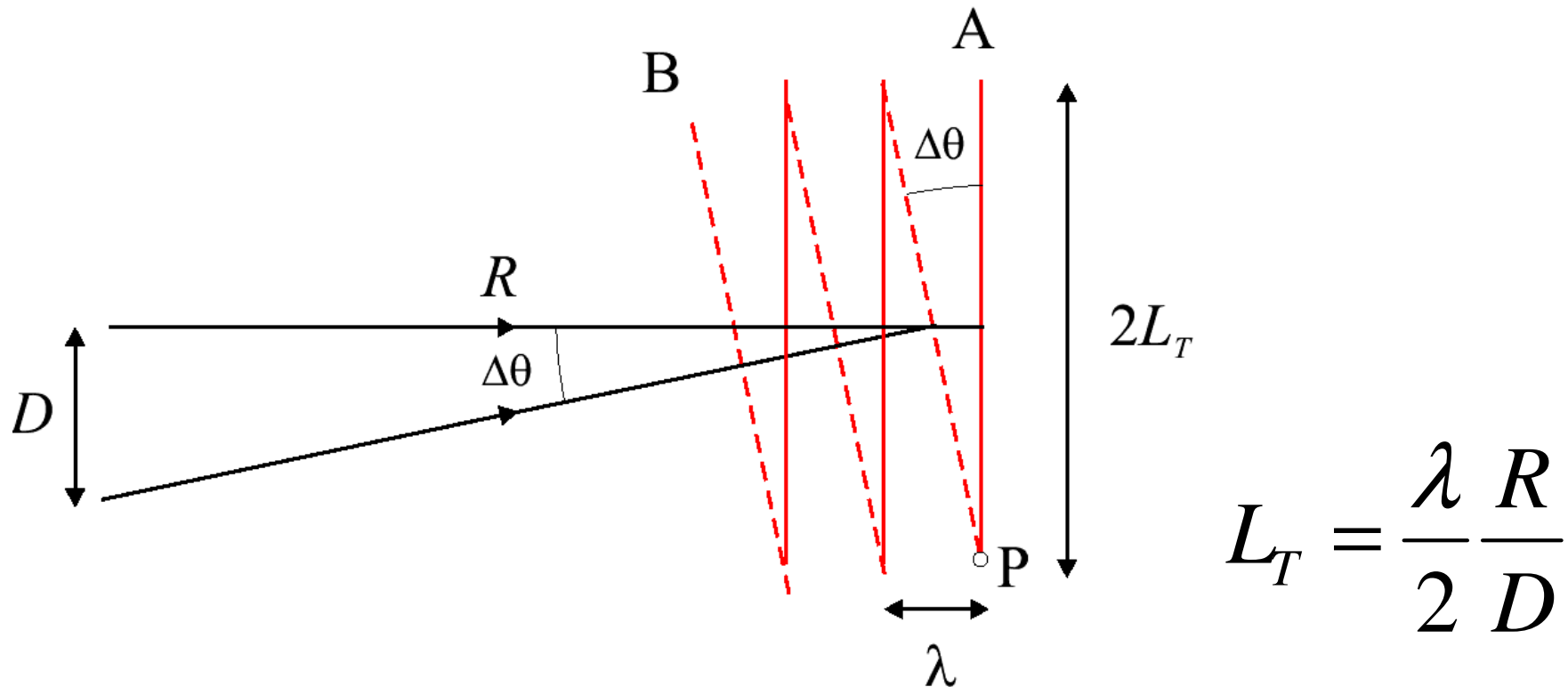
Diamond  
in-vacuum  
X-ray  
Undulator



# Longitudinal Coherence



# Lateral (Transverse) Coherence



$$L_T = \frac{\lambda R}{2 D}$$

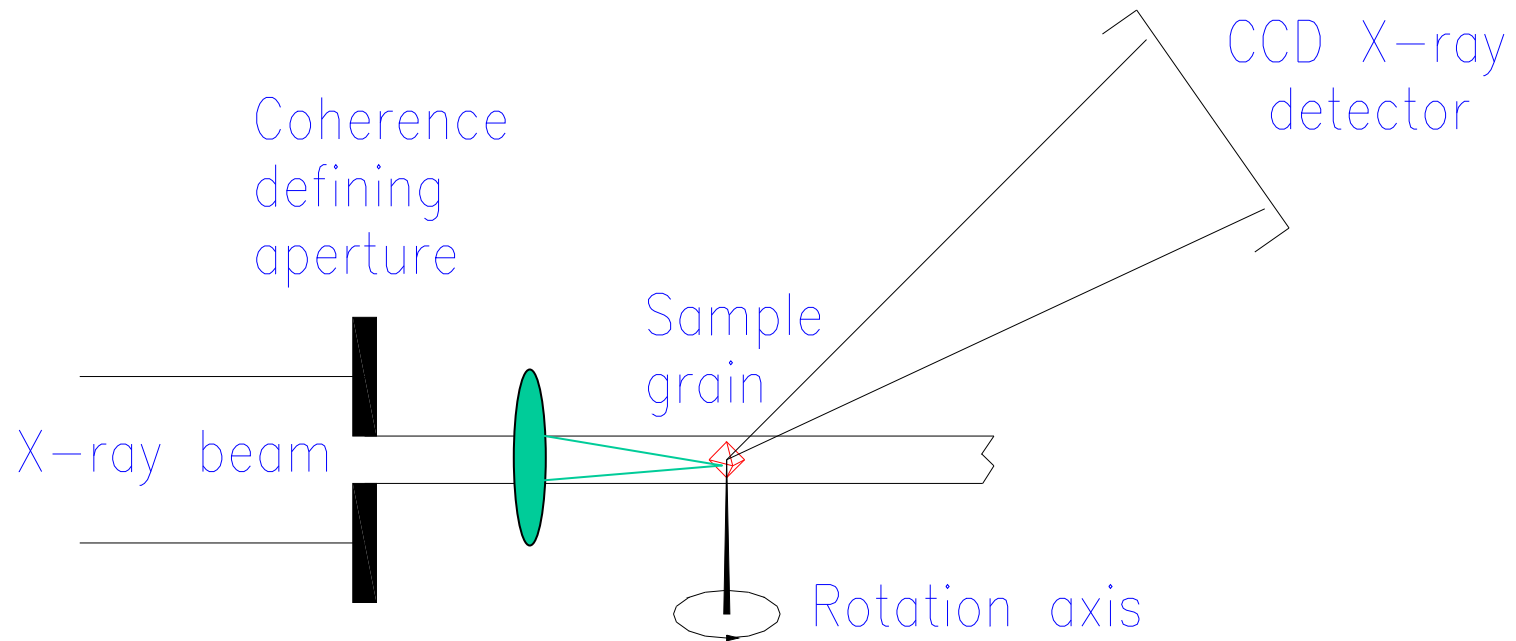
Als-Nielsen and McMorrow (2001)

# Robert Hooke's microscope, 1665

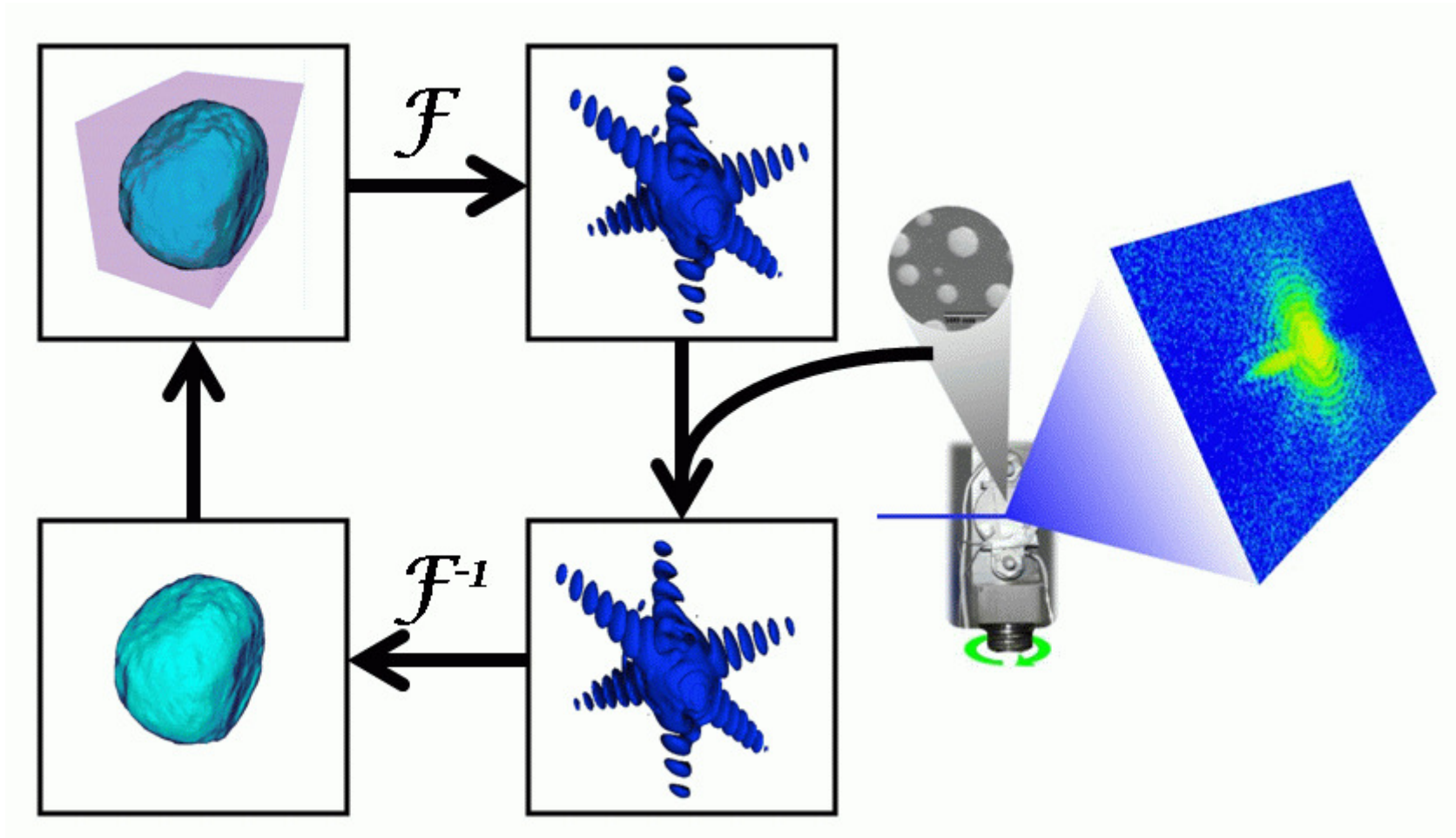
National Museum of  
Health and Medicine,  
Washington DC



# Lensless X-ray Microscope, 2003

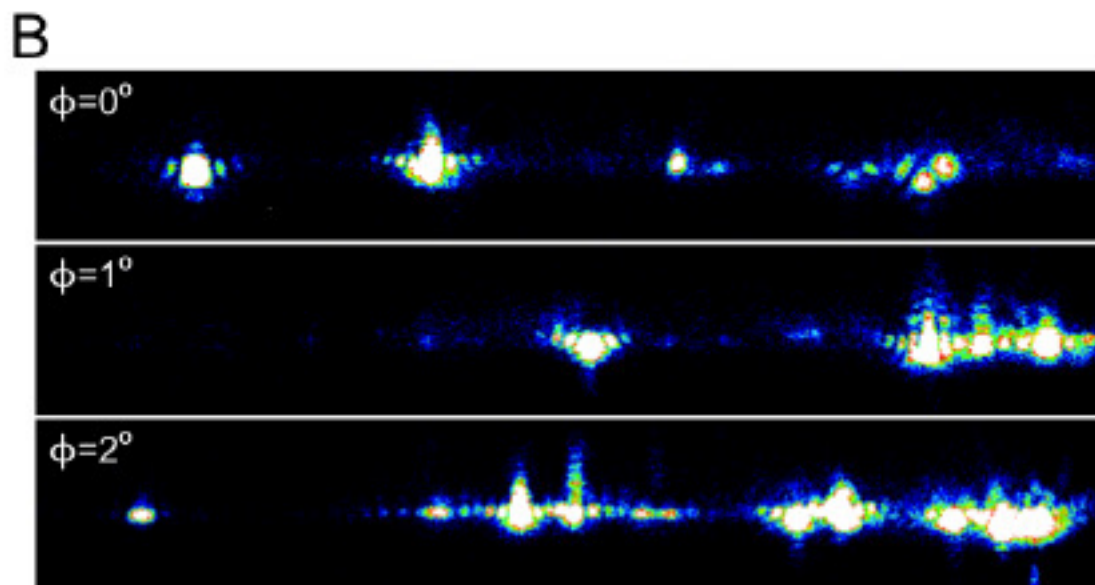
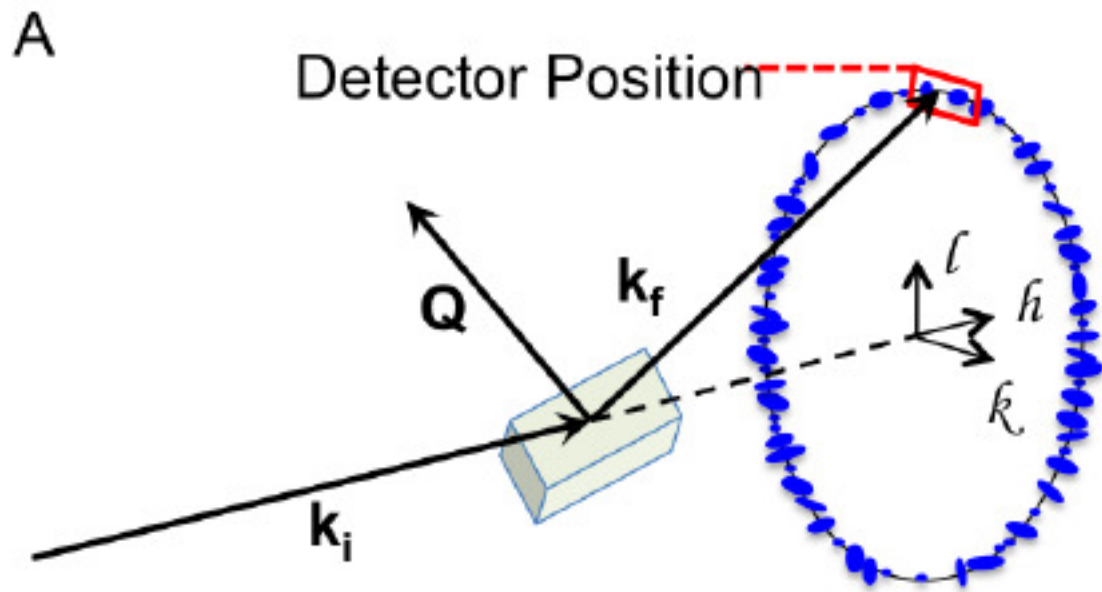


# Generic “Error Reduction” method



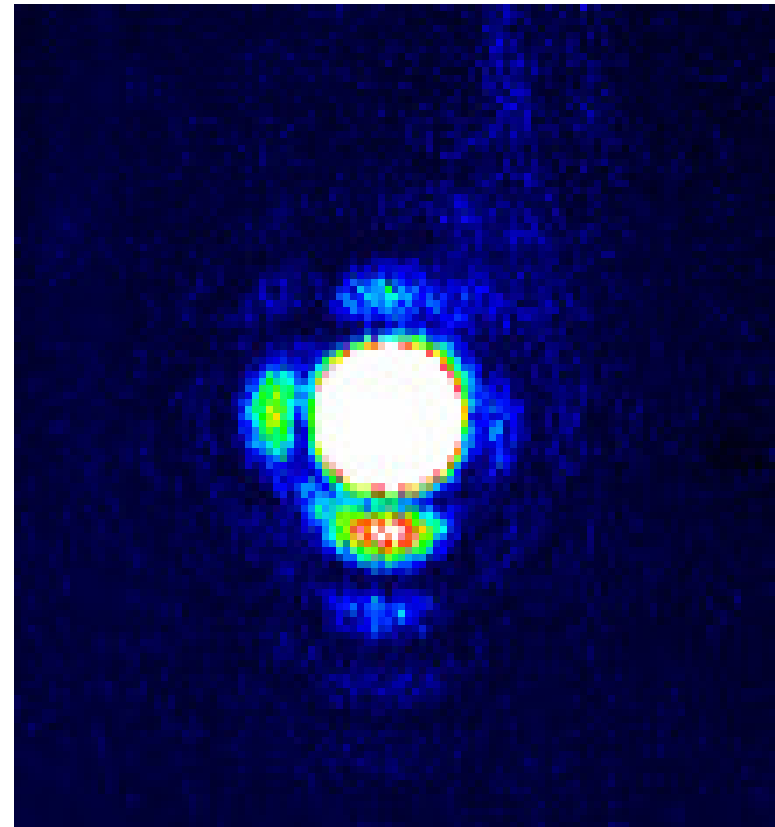
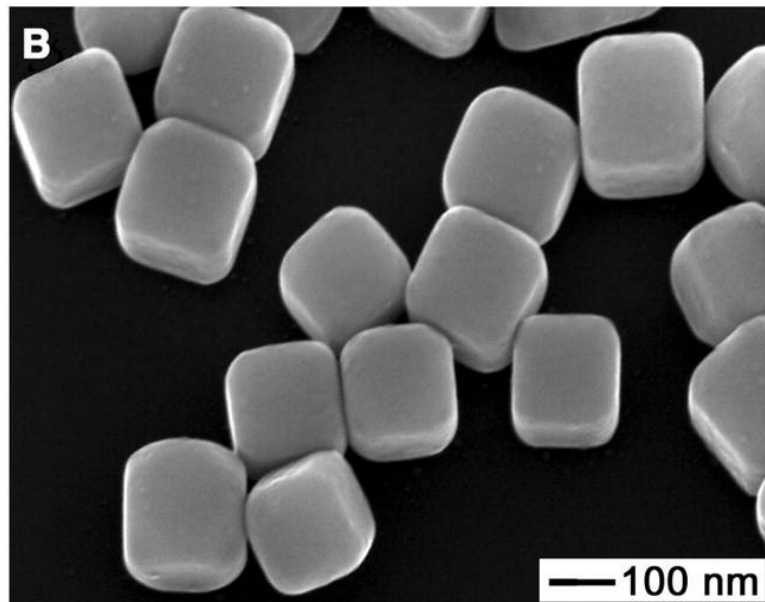
J. R. Fienup *Appl. Opt.* 21 2758 (1982)

R. W. Gerchberg and W. O. Saxton *Optik* 35 237 (1972)



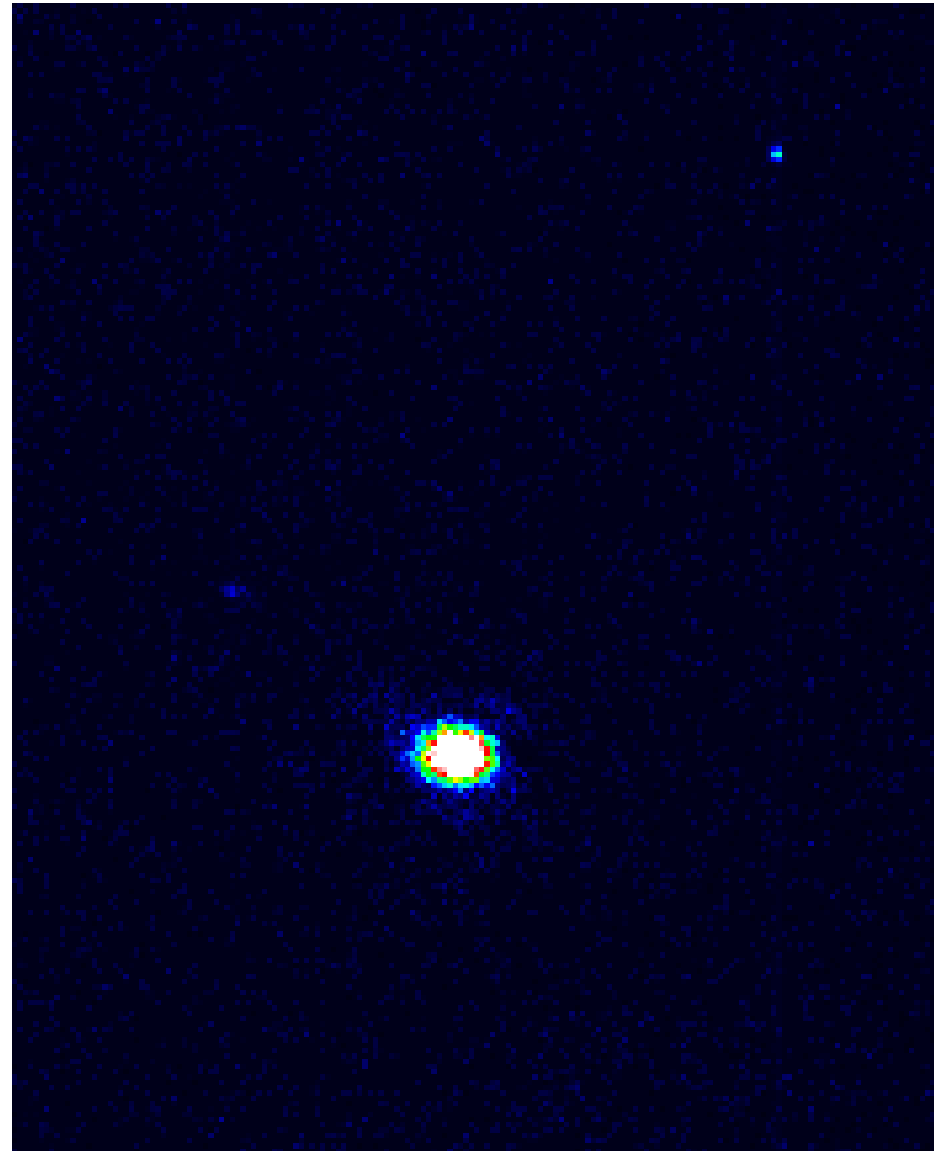
A. K. ROBINSON, PHYSICS 2011

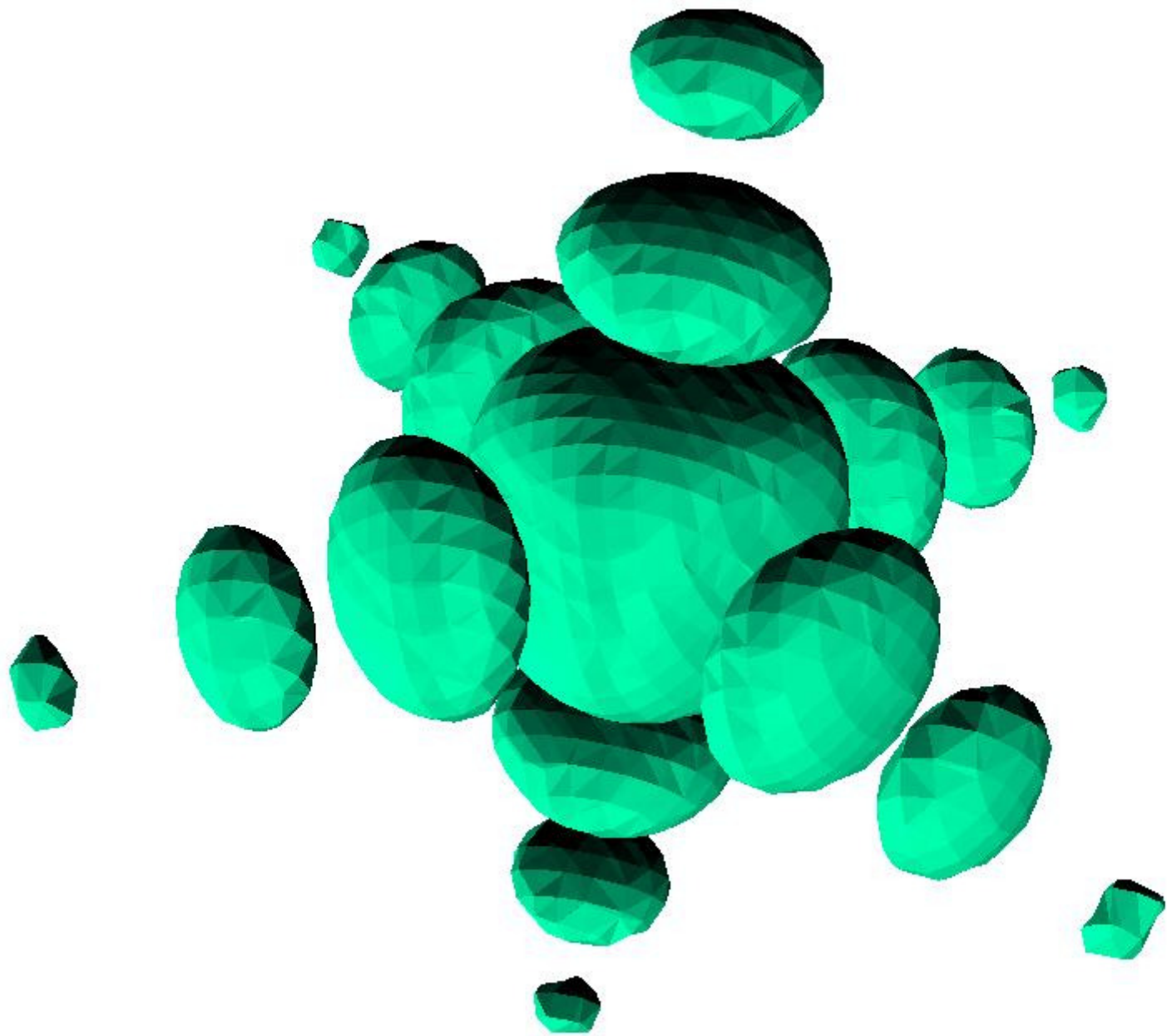
# Chemically Synthesized Silver Nanocubes

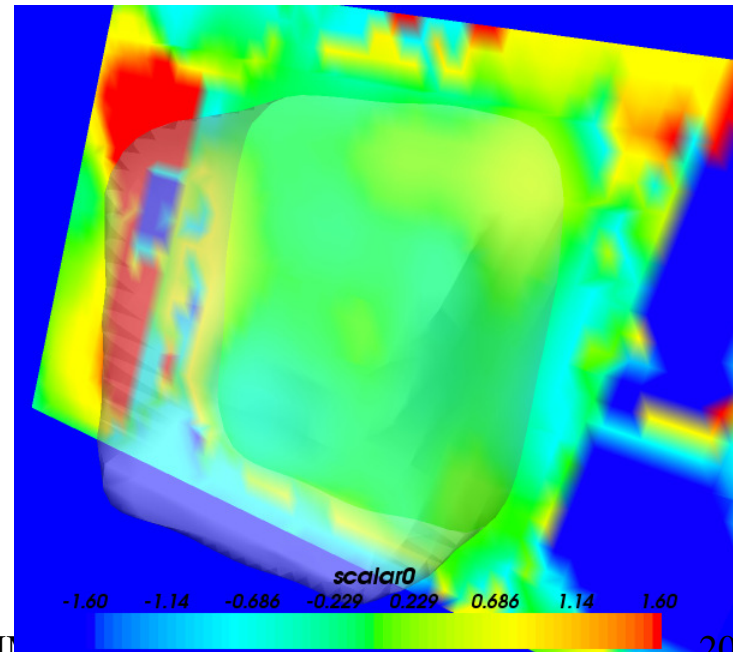
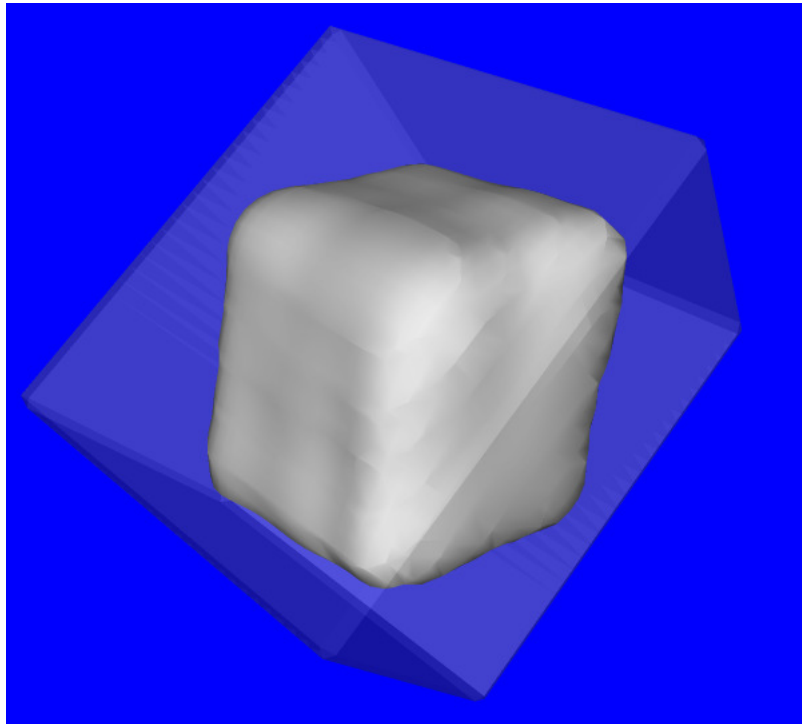
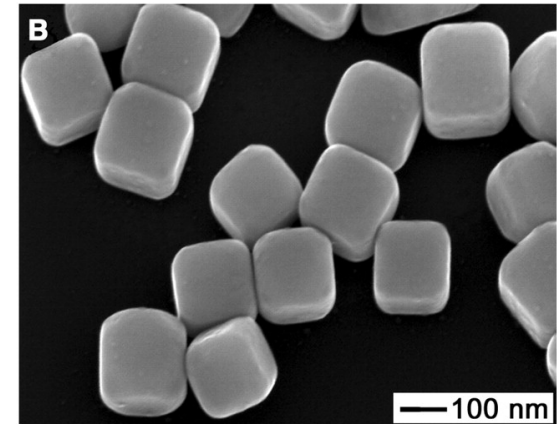
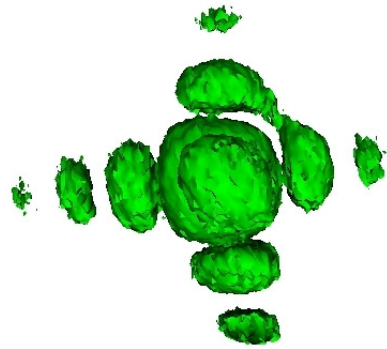
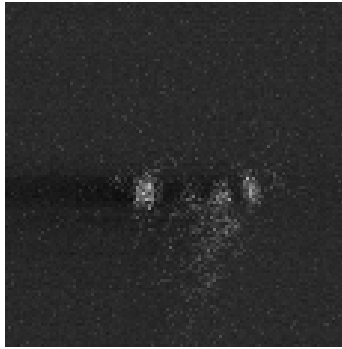


Yugang Sun and Younan Xia,  
Science 298 2177 (2003)

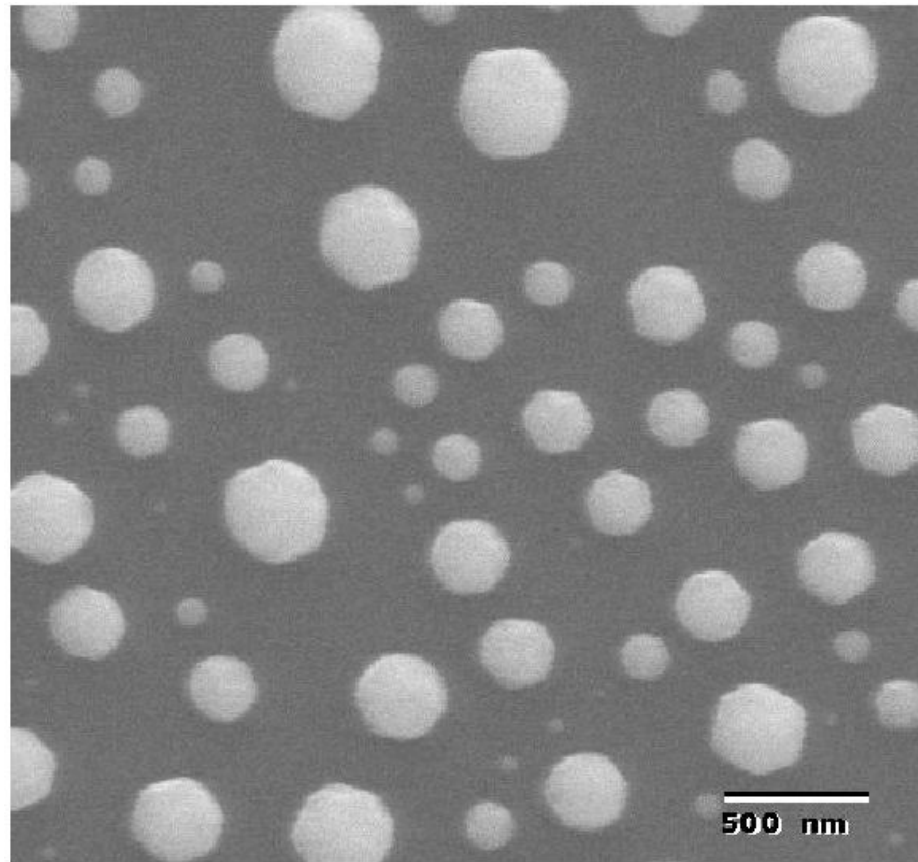
Rocking  
scan of Ag  
cubes with  
 $0.01^\circ$  steps



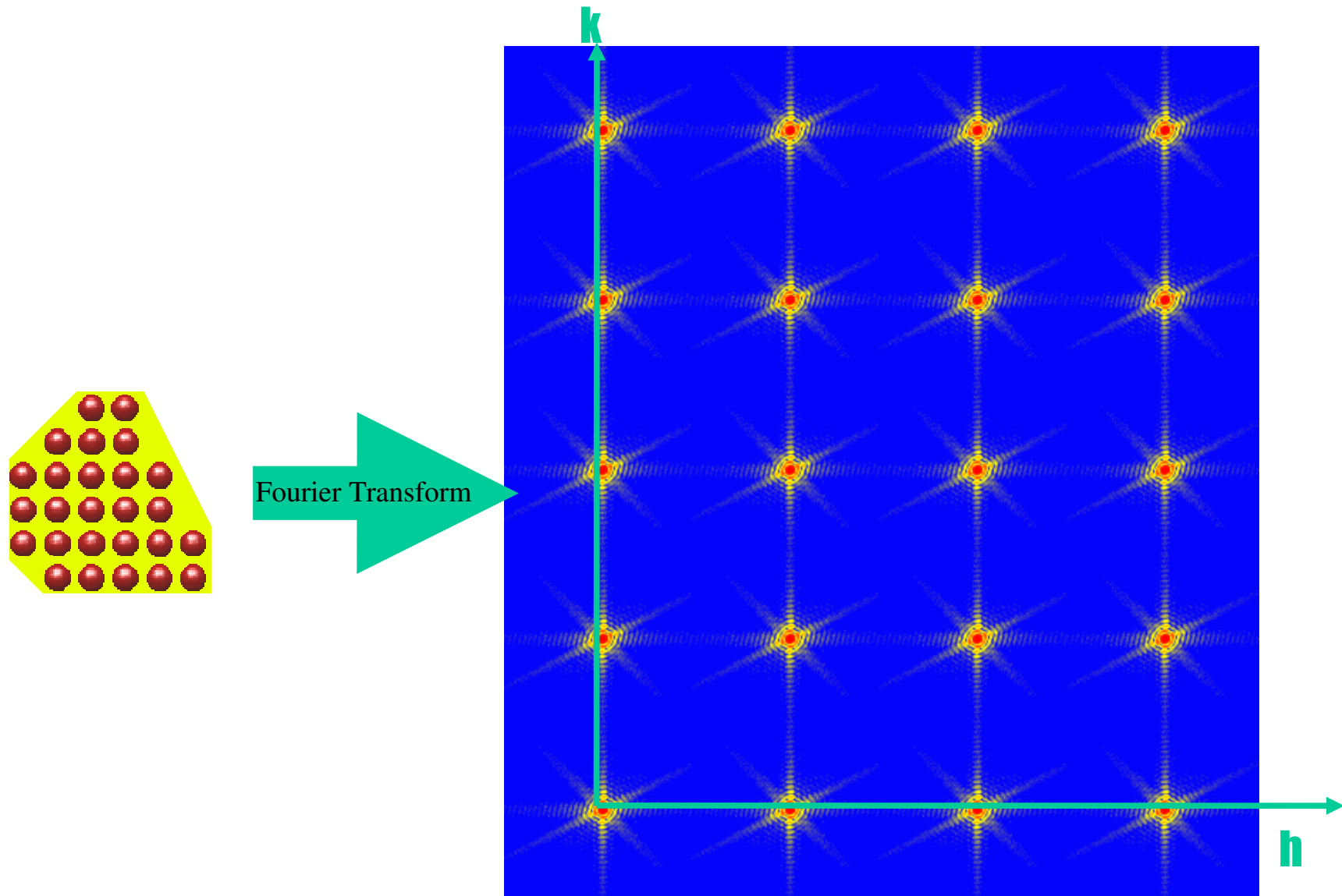




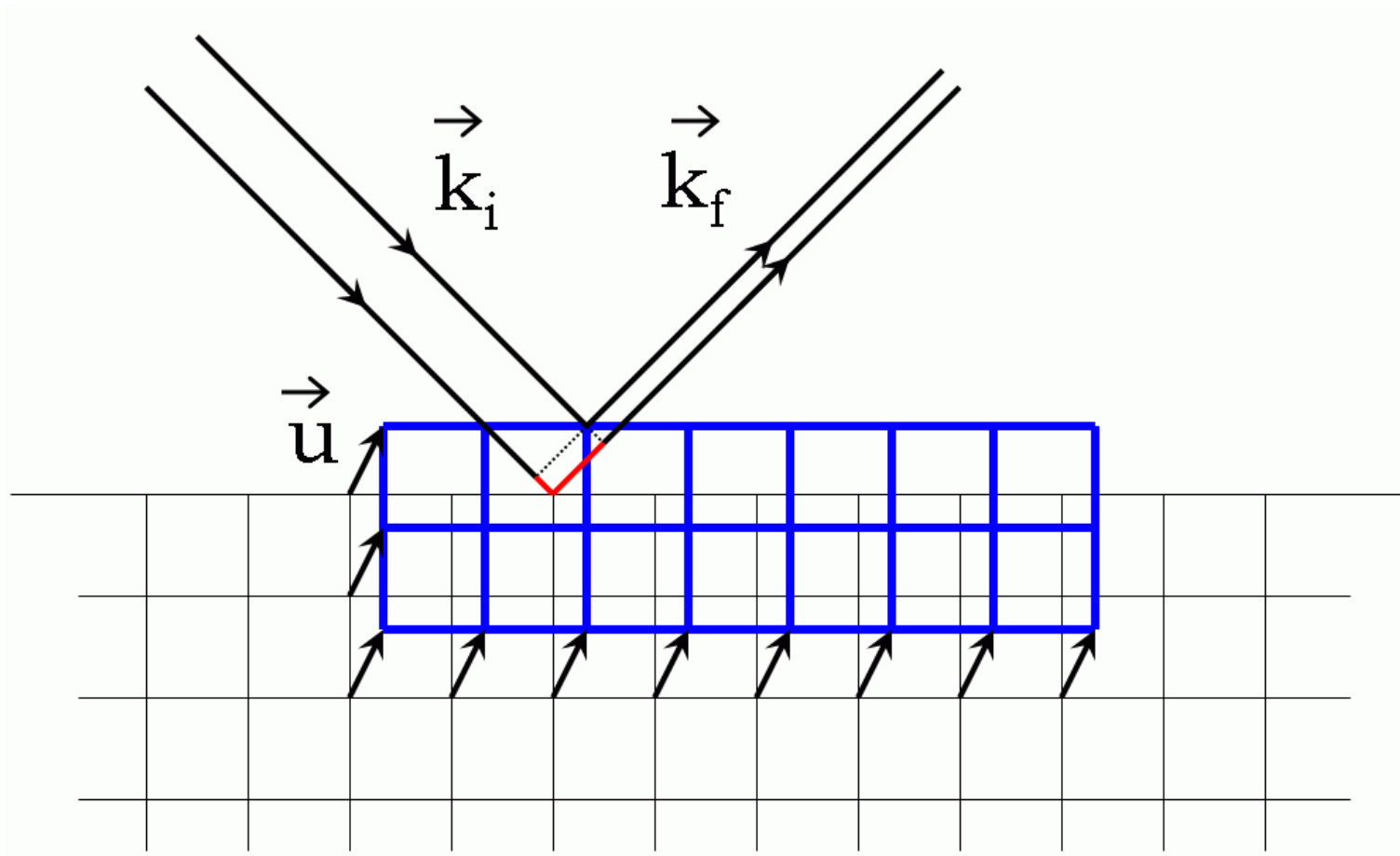
# In situ growth of Pb crystals



# Coherent Diffraction from Crystals



# Sensitivity to strain

$$\Delta\varphi = \mathbf{k}_f \cdot \mathbf{u} - \mathbf{k}_i \cdot \mathbf{u} = \mathbf{Q} \cdot \mathbf{u}$$


# Good statistics, 3D diffraction data

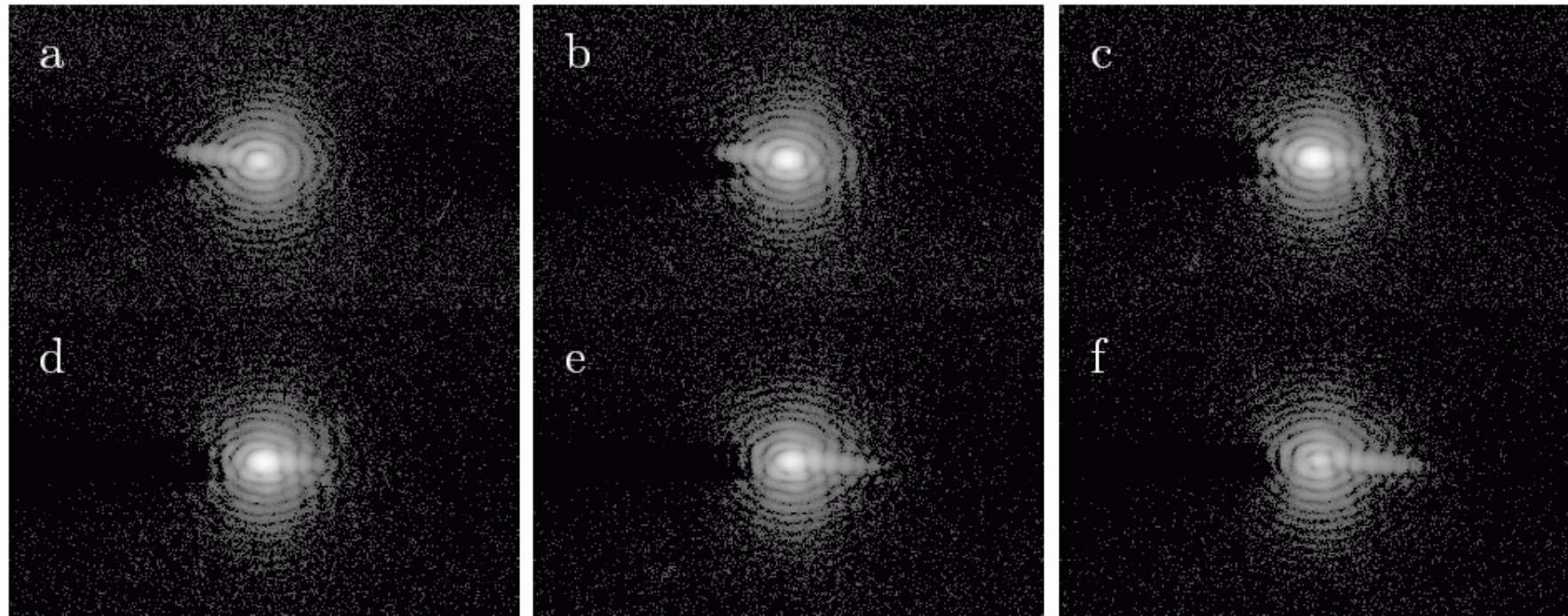
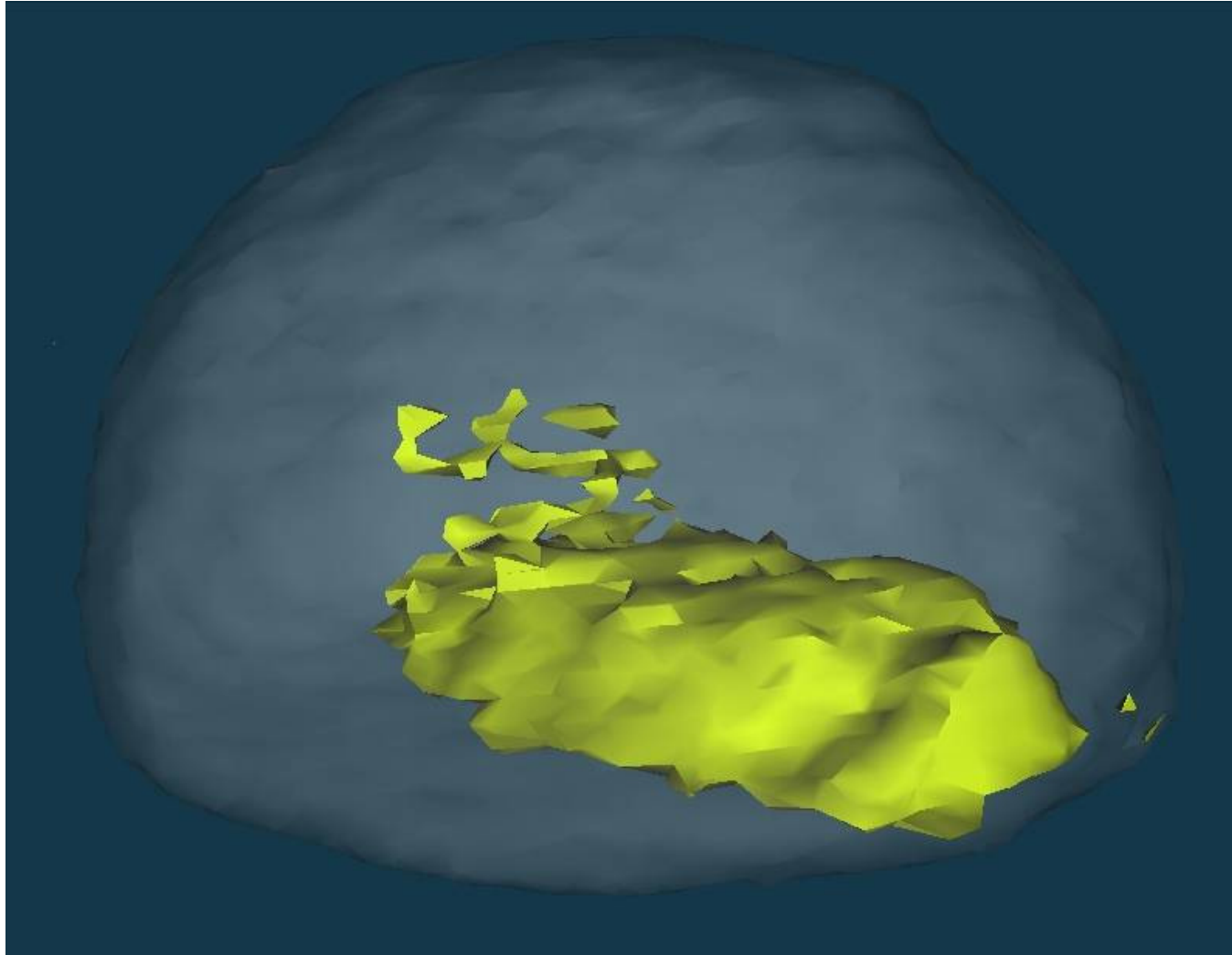


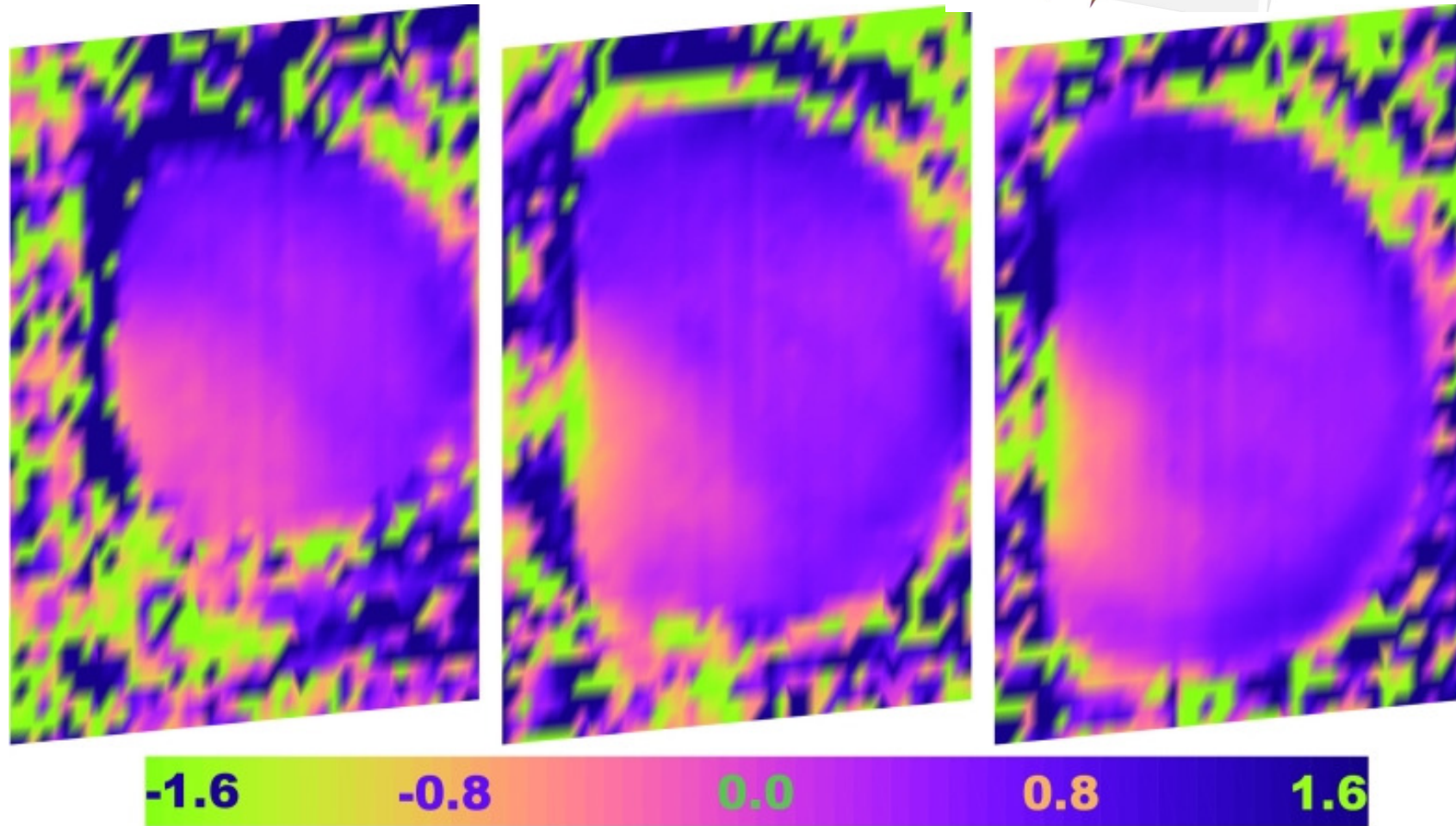
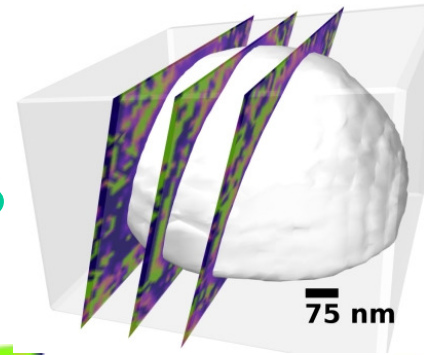
Figure 4.12: Center slices from 3D CXD pattern from Pb sample, on a log scale. Data file 296 from 10/03.

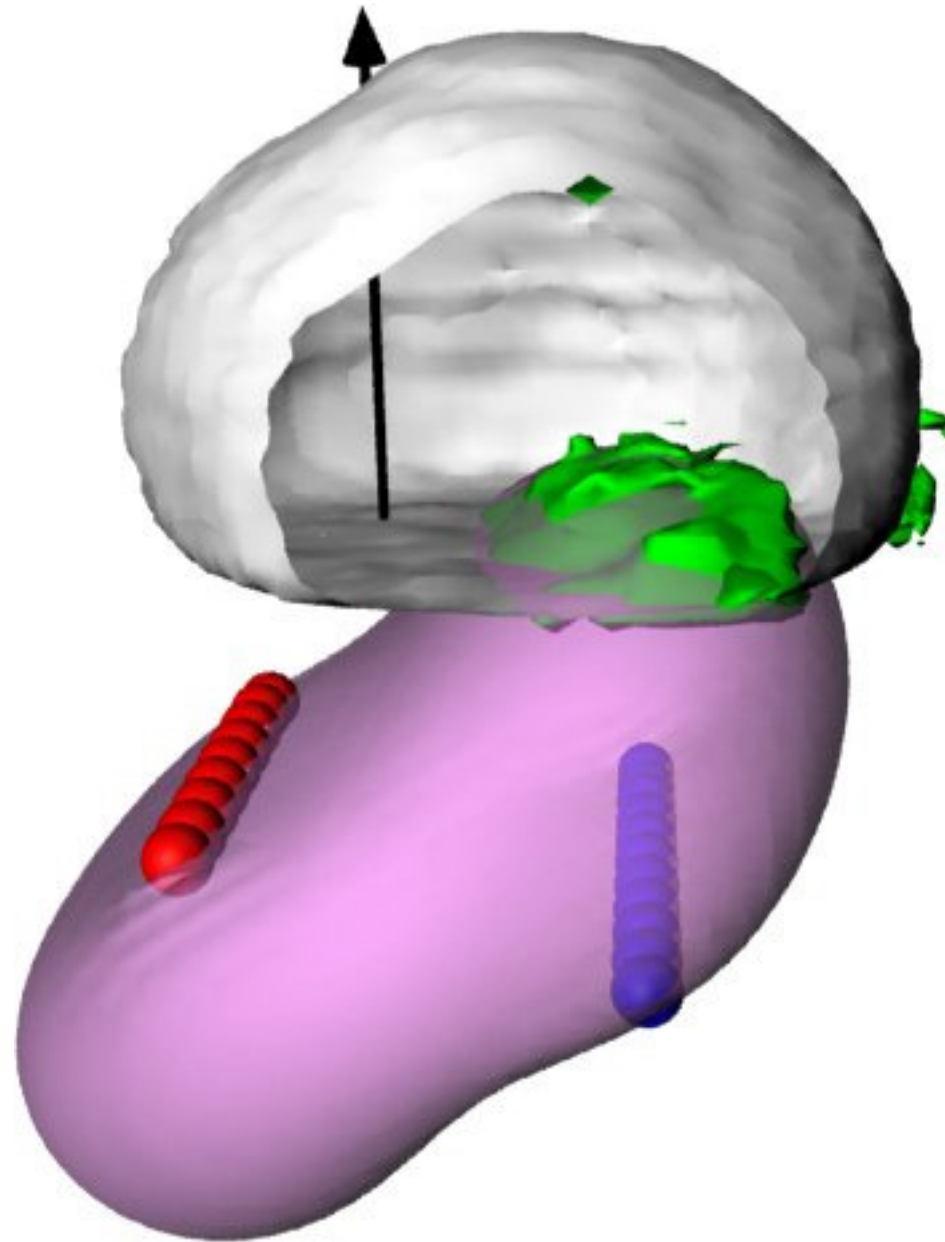
# Modeling of 3D Phase Bump



I. K. Robinson, EMMS 2011

# 3D phase map sections

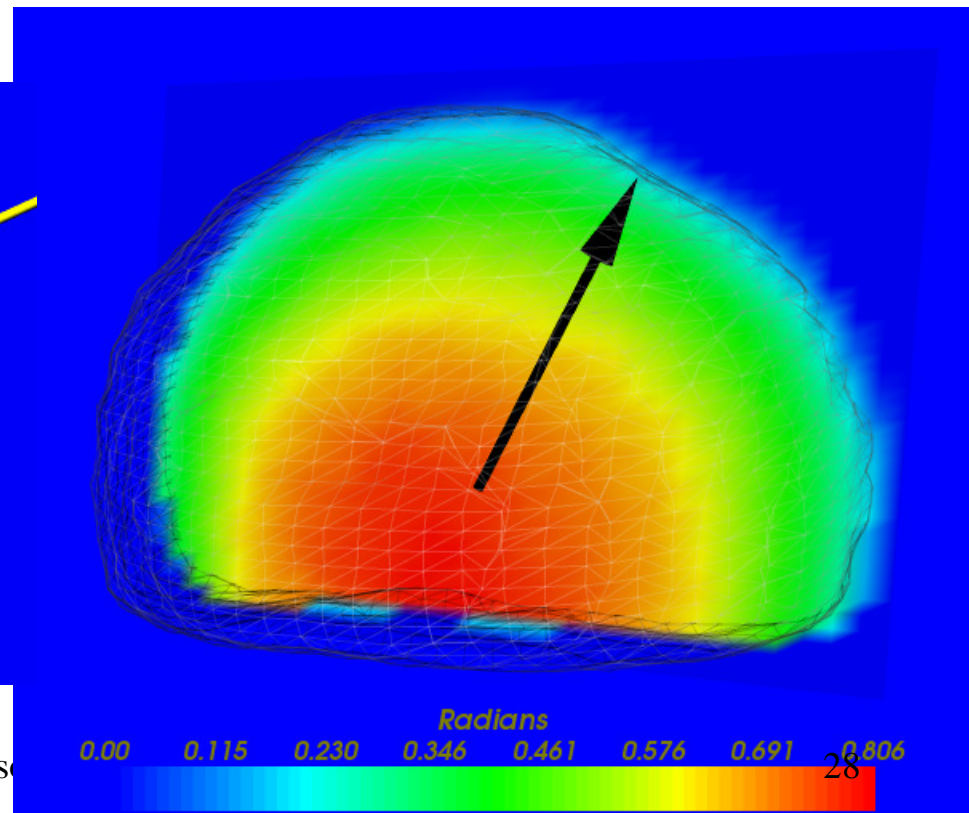
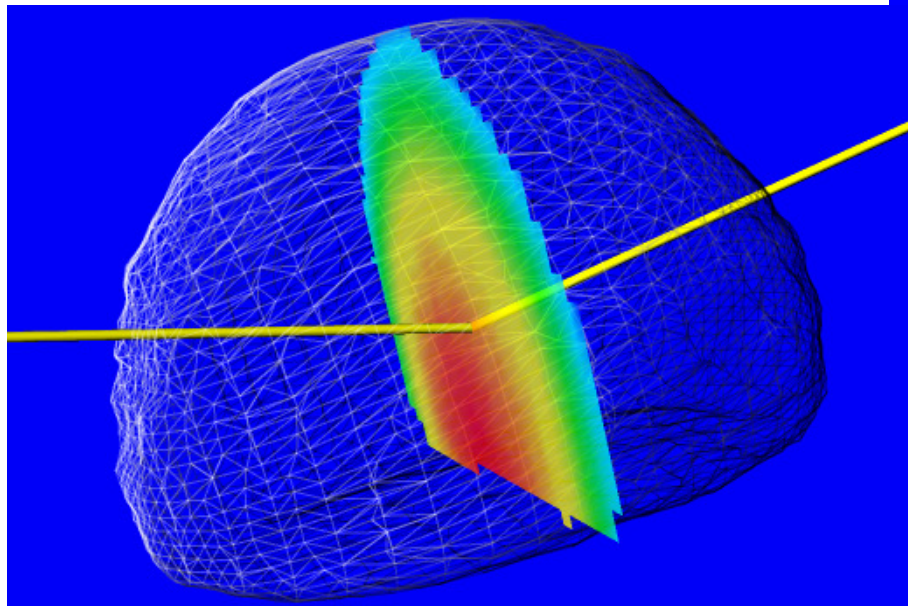




# Refraction effects in Lead at 8.9keV

Phase accumulation due to refraction along scattering path  
 $n=1-\delta+i\beta$

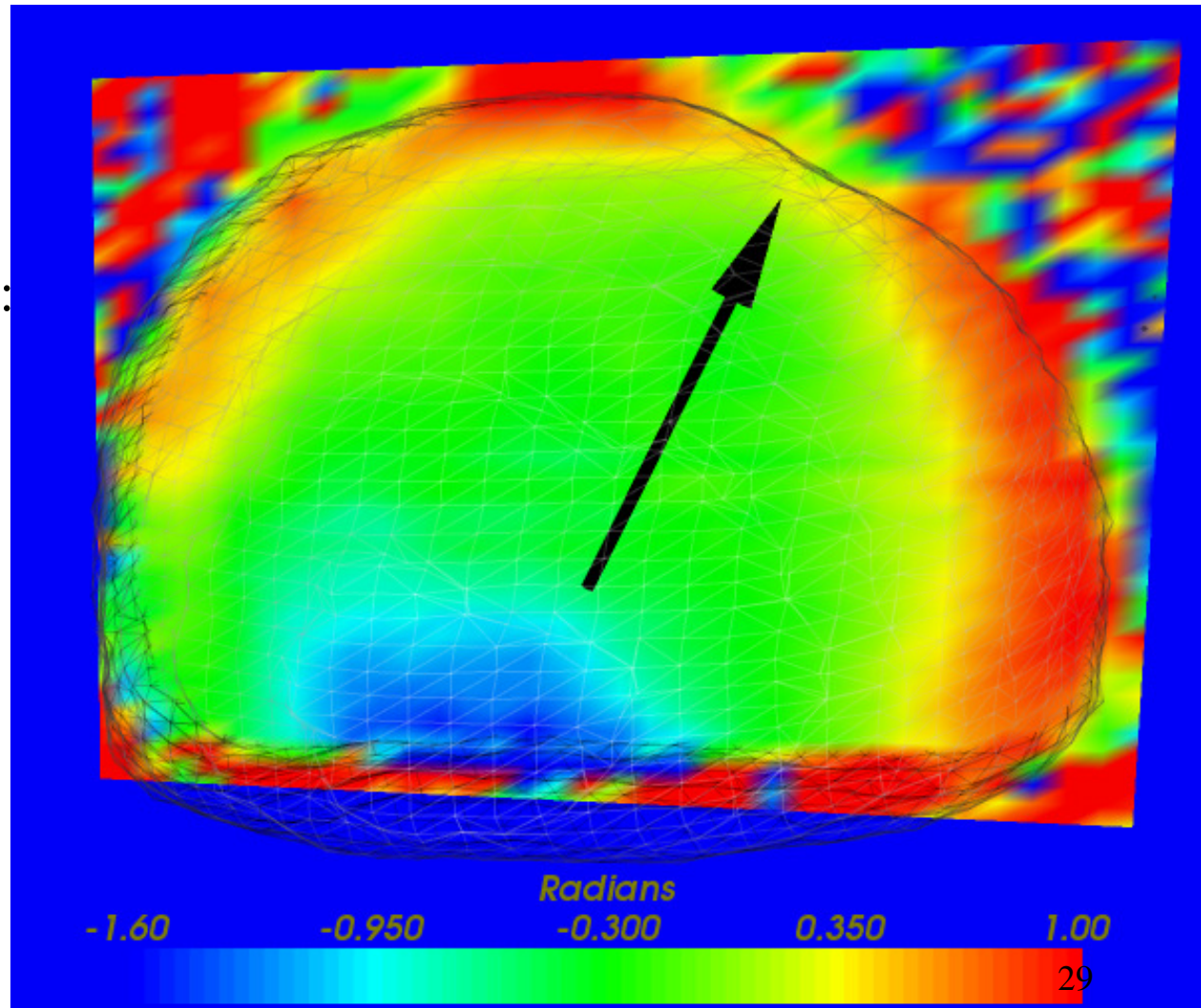
$$\delta=2.23\times 10^{-5}$$
$$\beta=2.19\times 10^{-6}$$



# Refraction corrected phase map

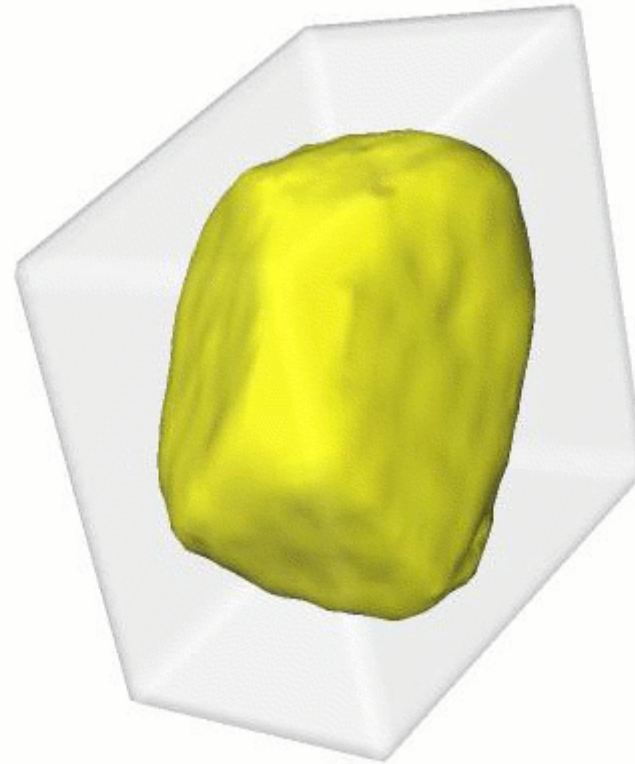
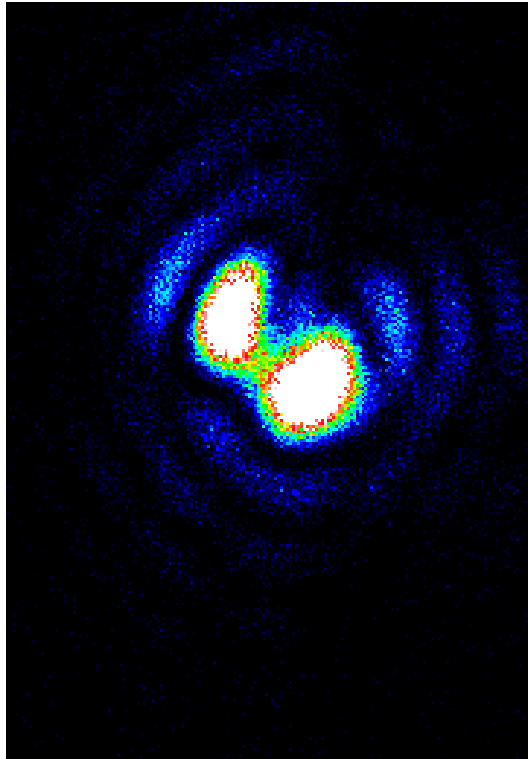
Max phase = 1.15rad  
= 0.052nm

Phase on the (111) facet:  
= 0.47 rad  
= 0.02nm

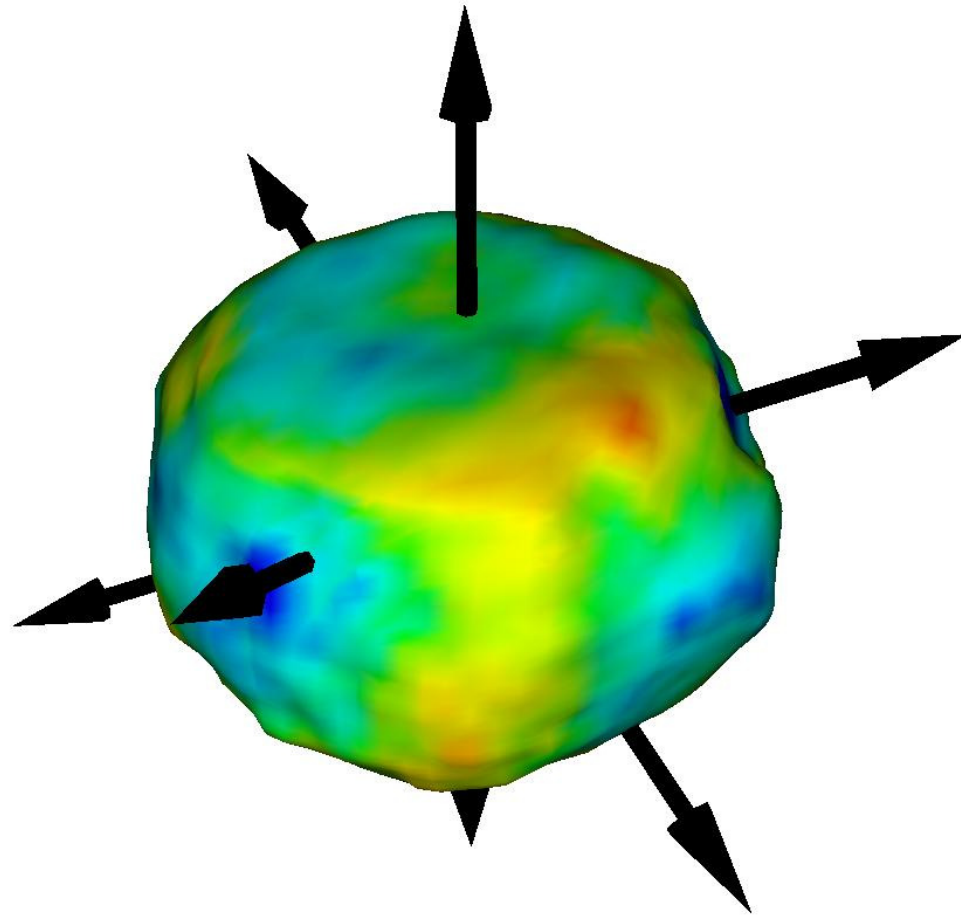


# Gold nanocrystal reconstruction

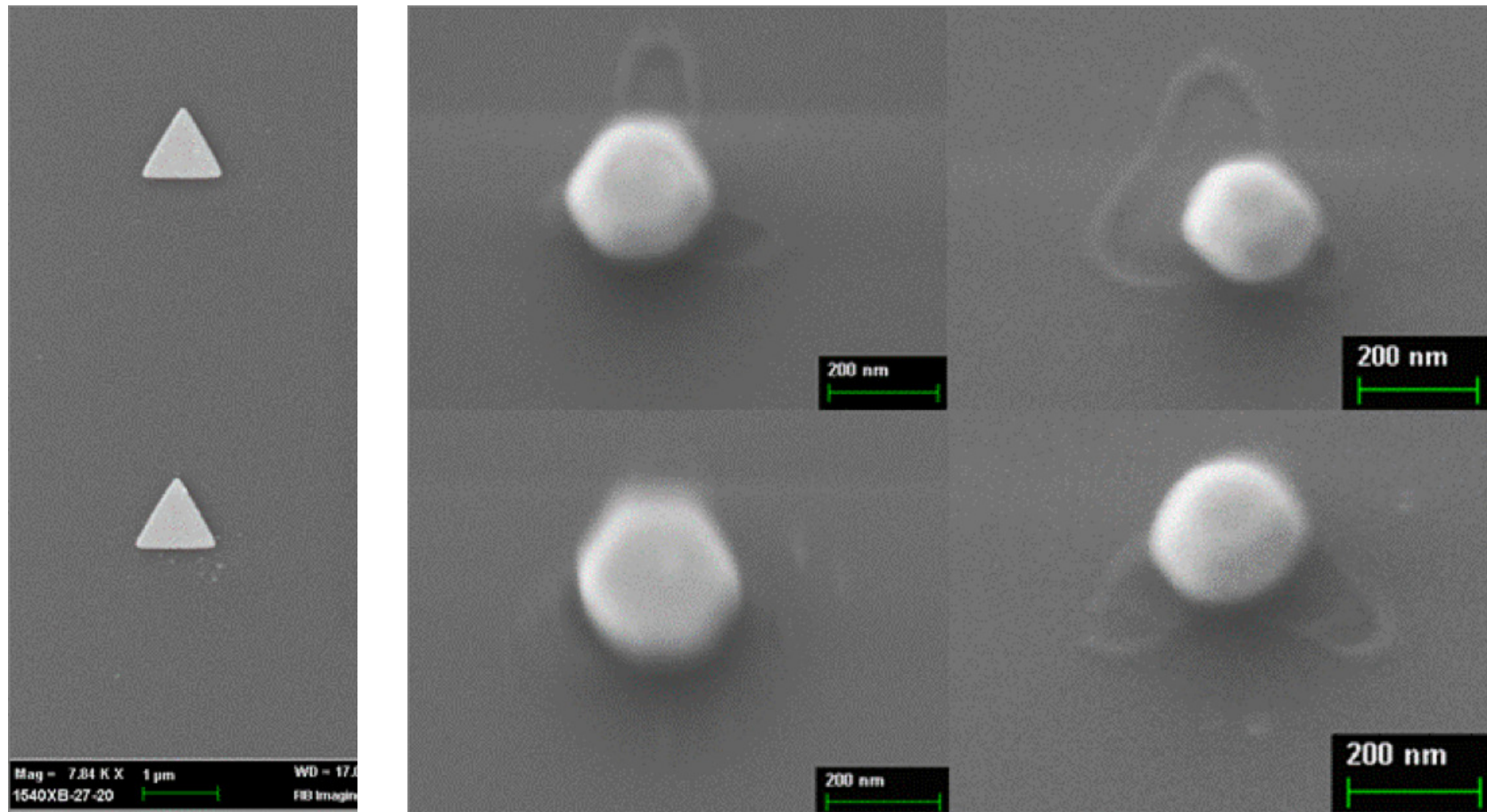
showing support used for 20 HIO followed by 10 ER



# Phase isosurface of residual strain

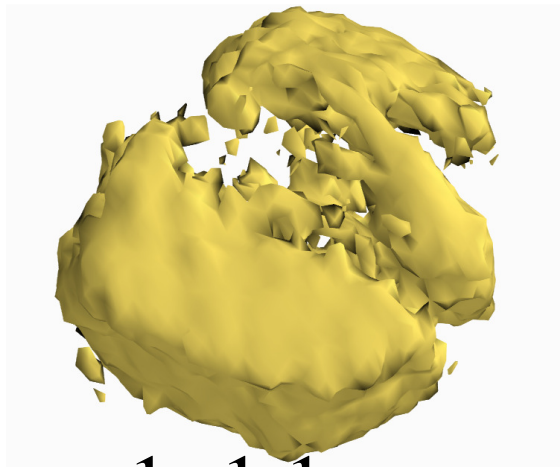


# Single Au nanocrystal synthesis

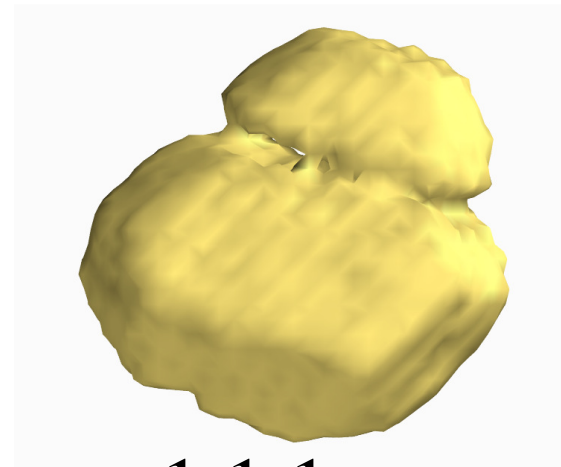




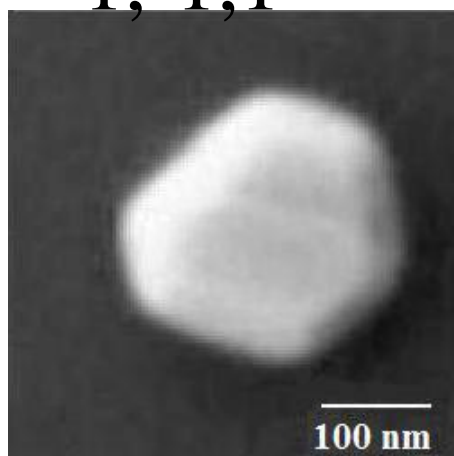
1,1,-1



1,-1,1

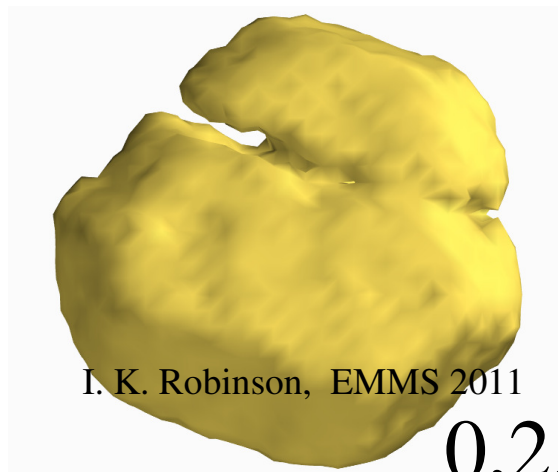
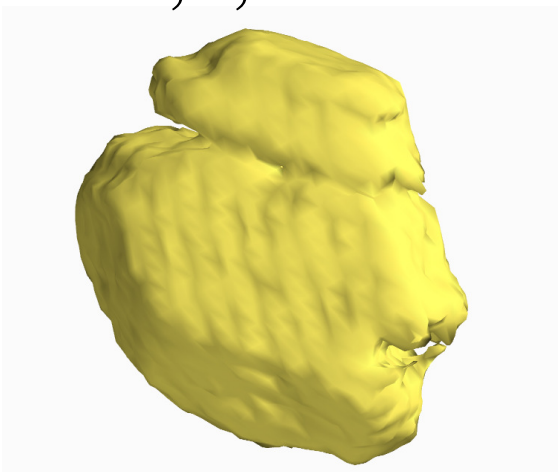


-1,1,1

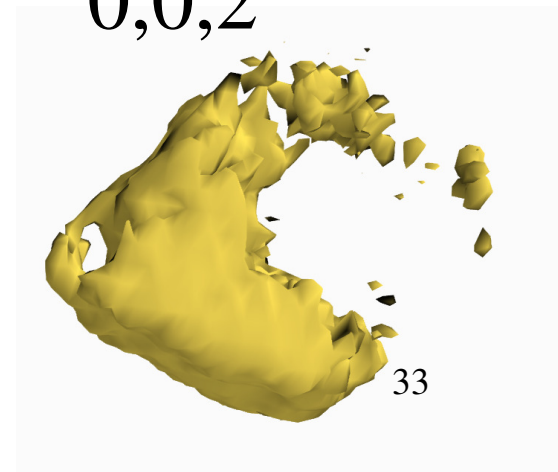


100 nm

2,0,0



0.2.0



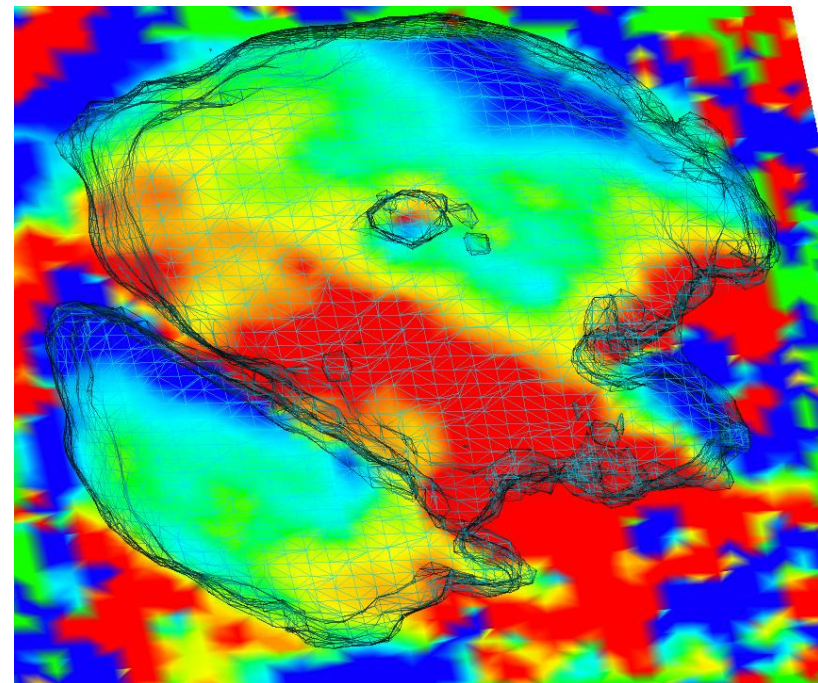
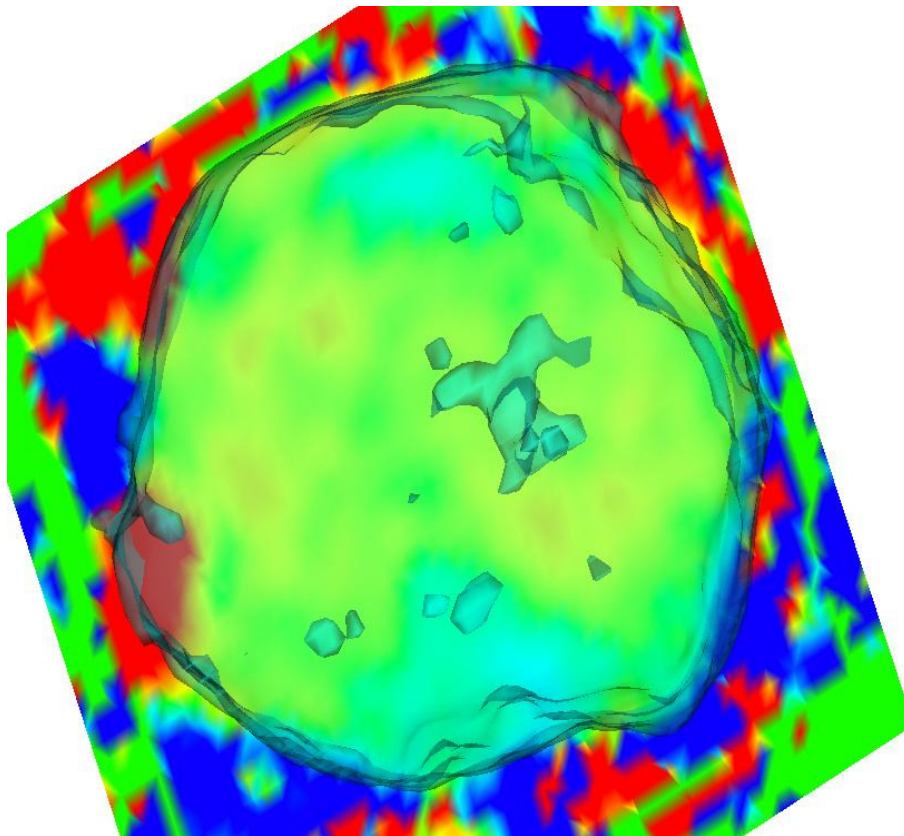
0,0,2

I. K. Robinson, EMMS 2011

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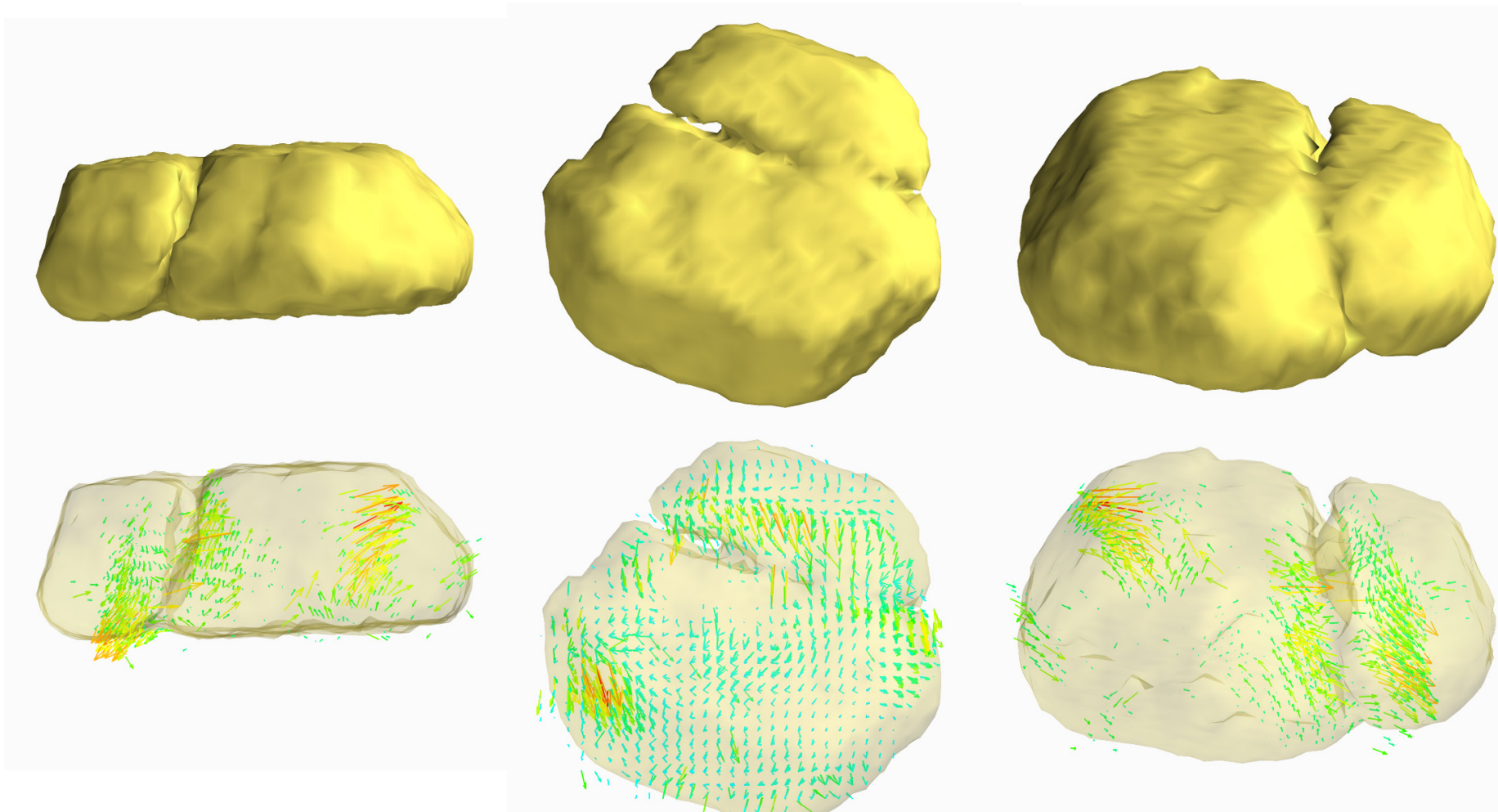
# Two views of strain in Au NC

Au409B-52 (11-1) and Au409B-60 (200)

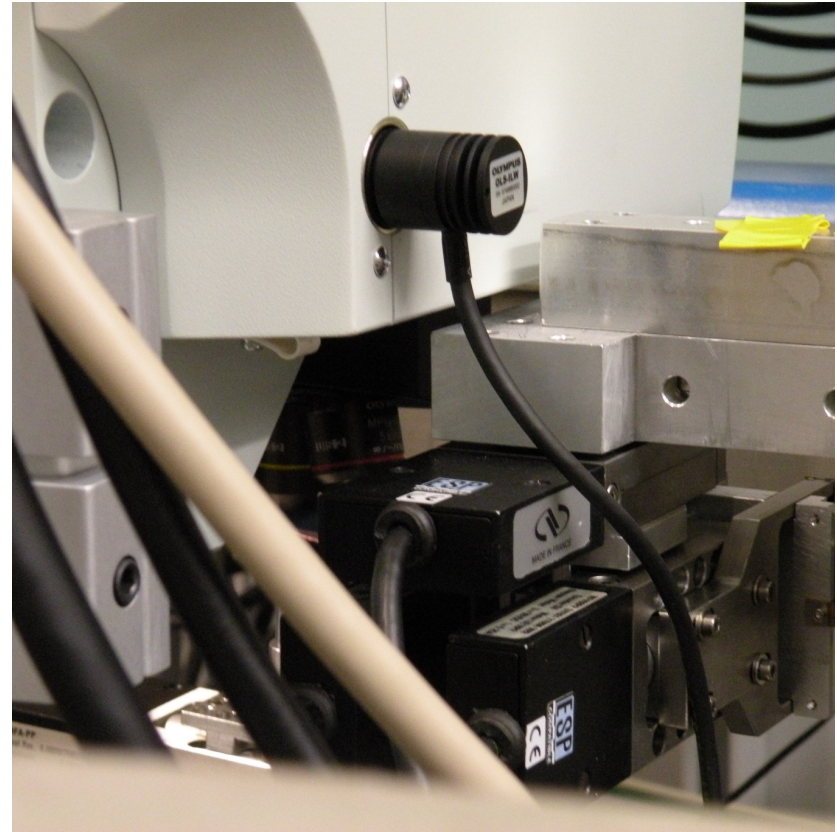
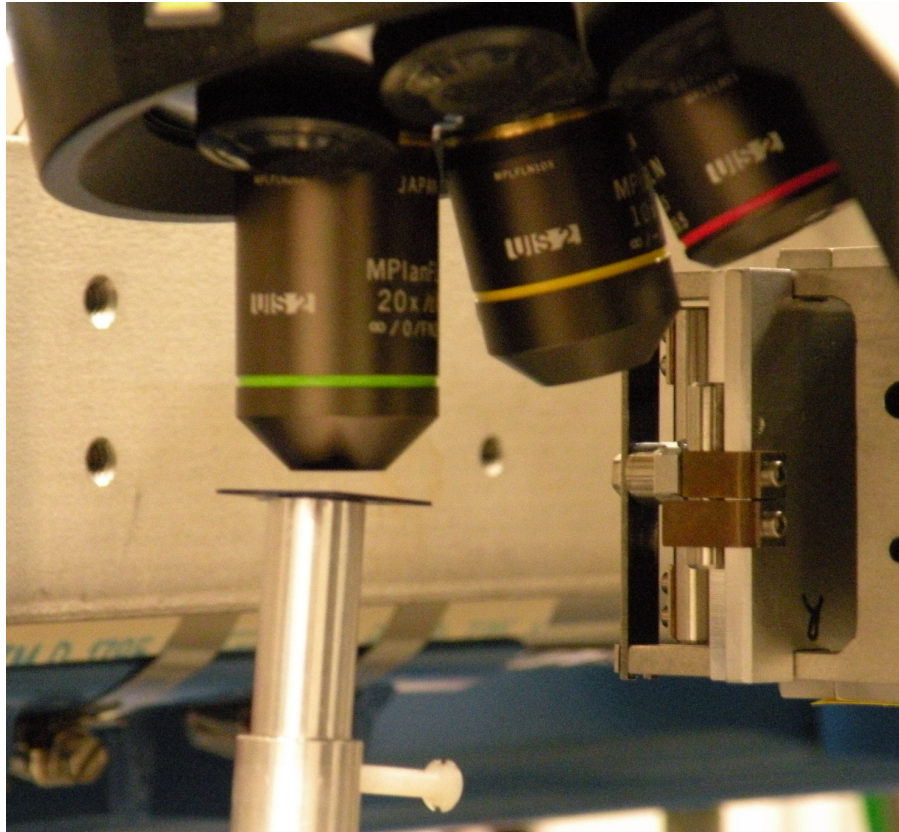


# Vector displacement field

Merged reconstructions from (11-1) (020) and (-111)

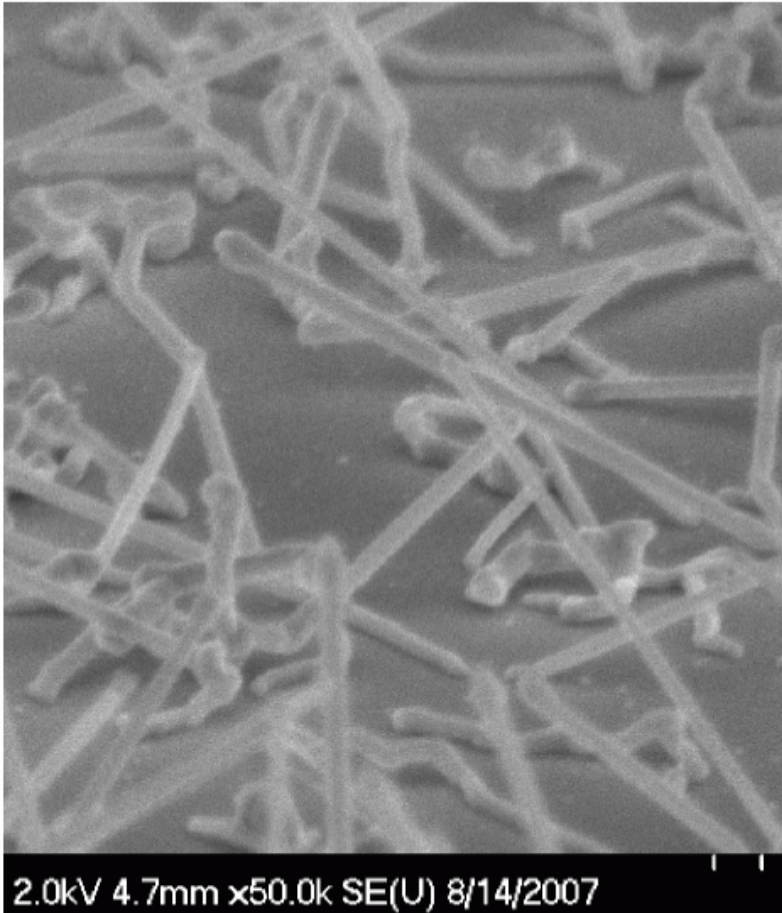


# Confocal Alignment Microscope

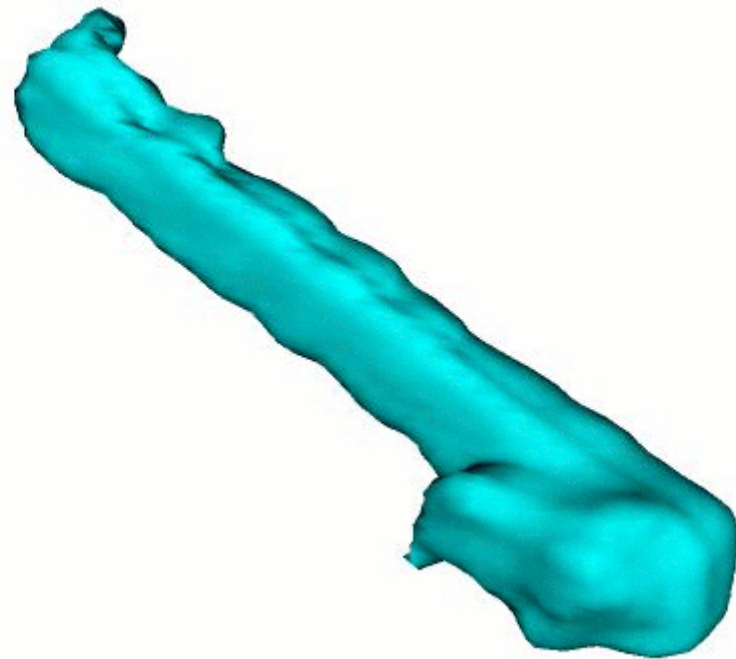


# Reconstruction of InP nanowire

CVD on Si, Suneel Kodambaka, UCLA

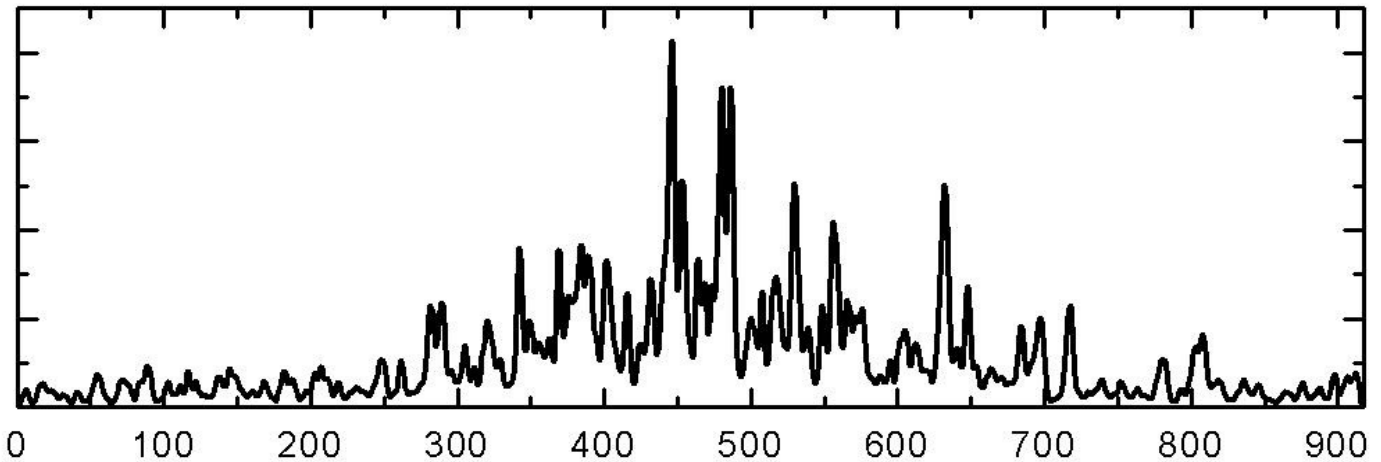
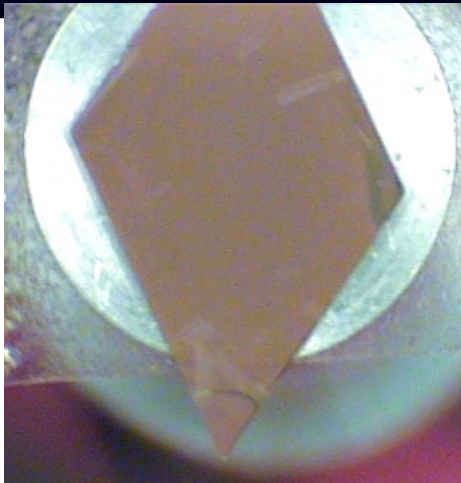
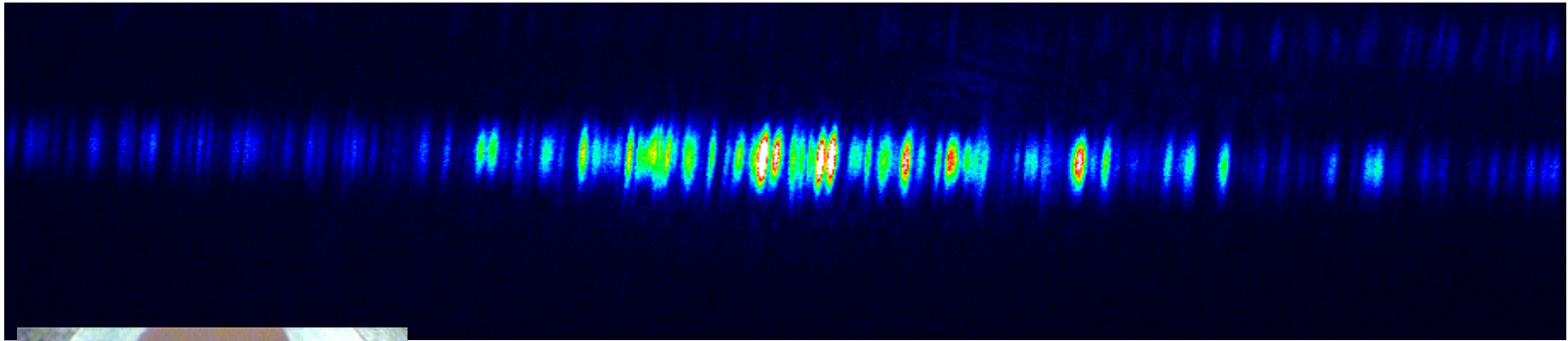


InP nanowires grown on Si (111)



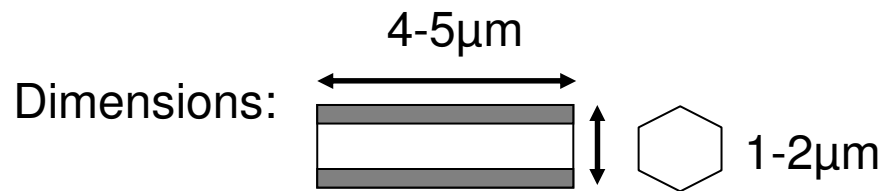
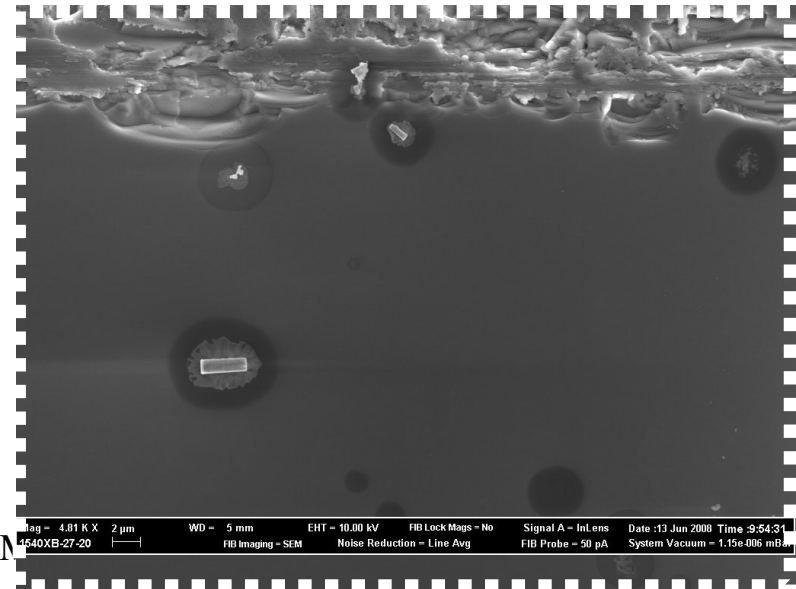
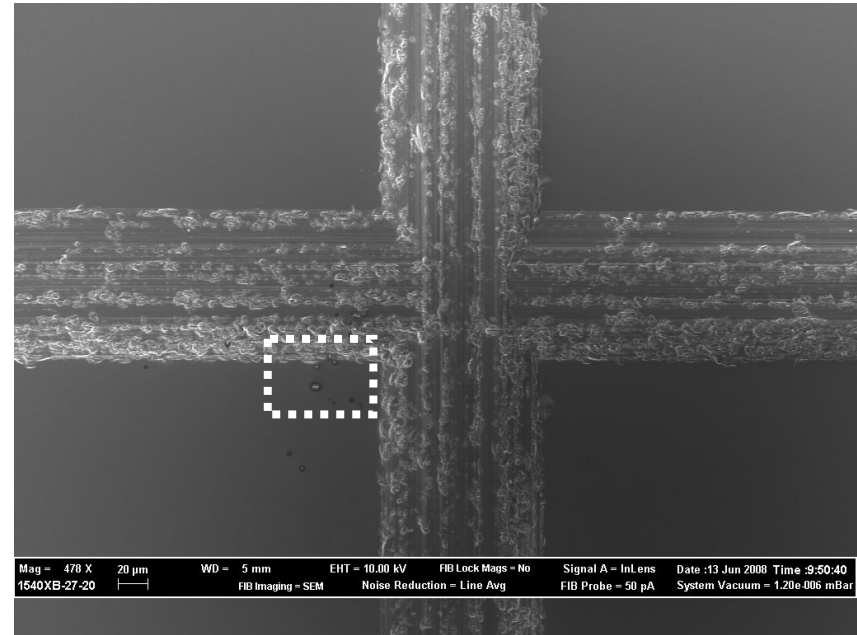
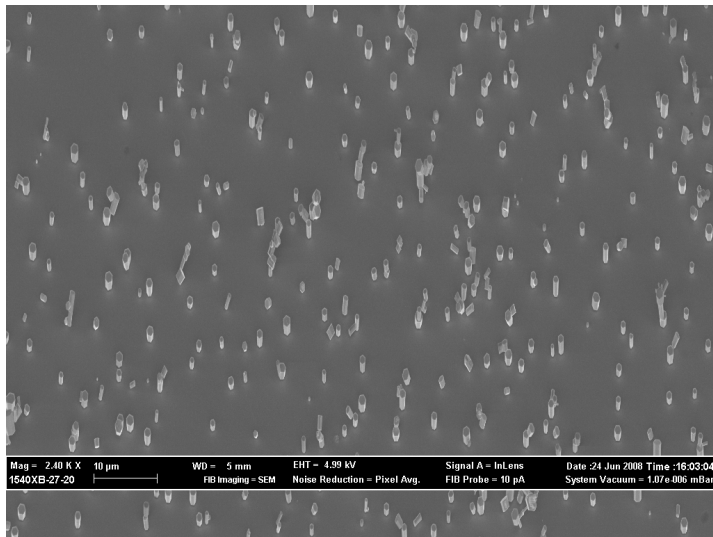
# GaAs Nanowire “Barcode”

Vincent Favre-Nicolin, Joel Eymery (CEA),  
Rienk Algra (Philips), Ross Harder



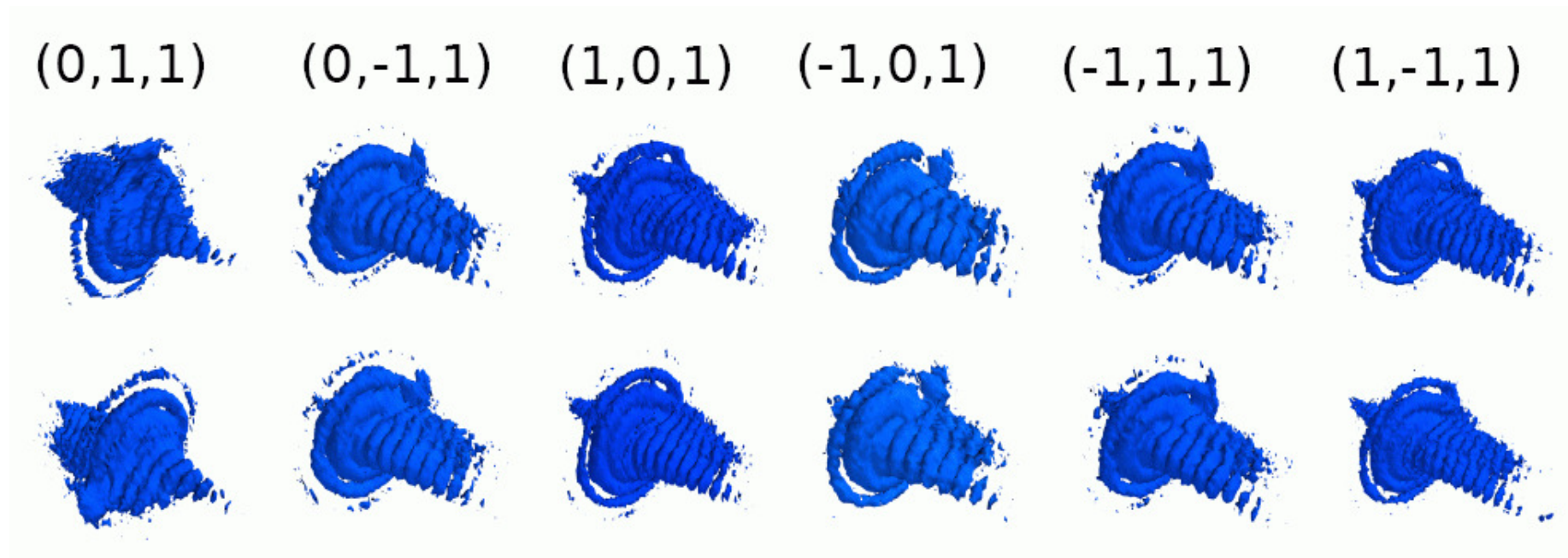
GaAsNW1106-22.spe  
B9348 from Philips

# ZnO Sample Preparation

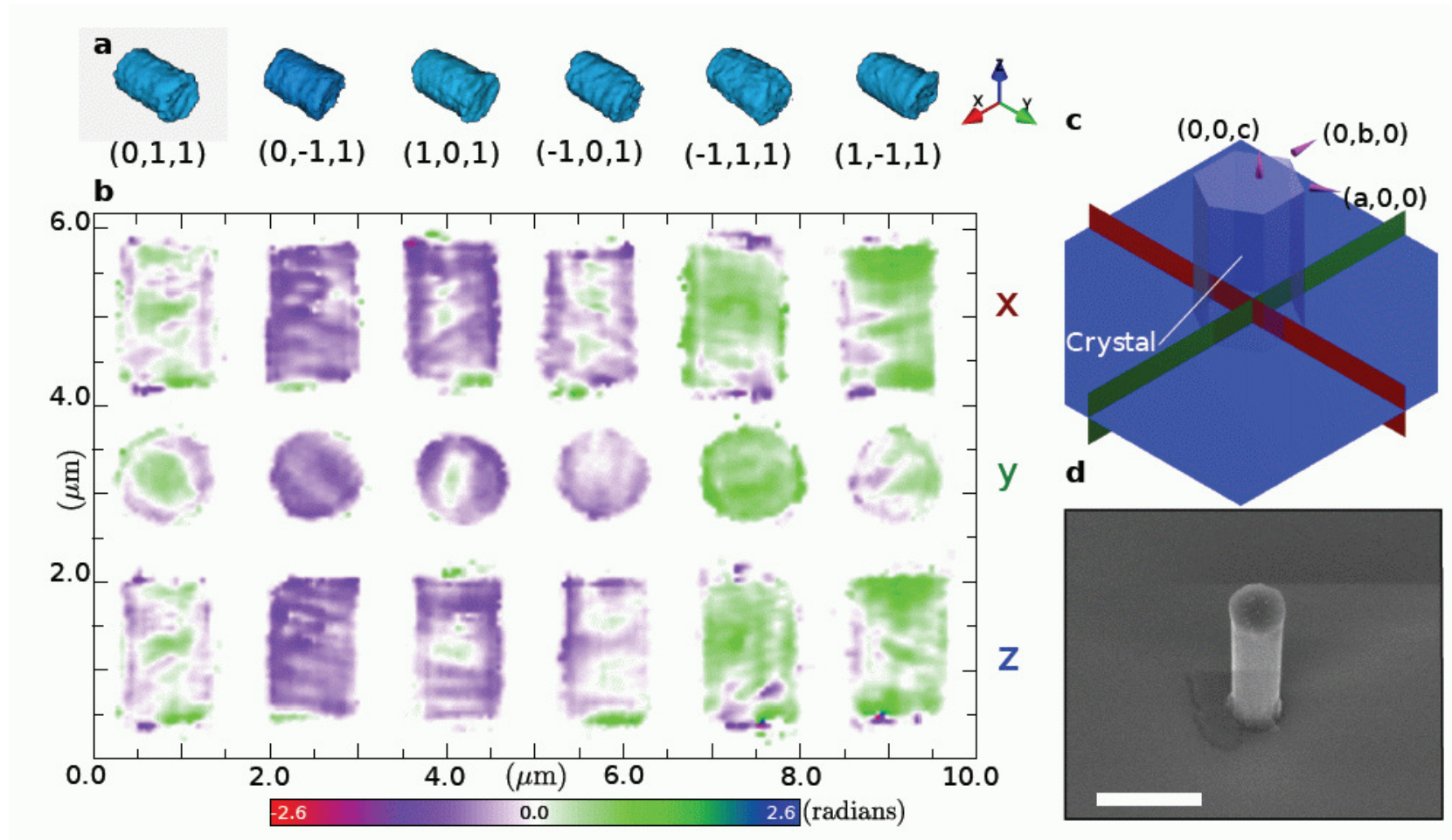


I. K. Robinson, EMM

# Six Independent Bragg Peaks

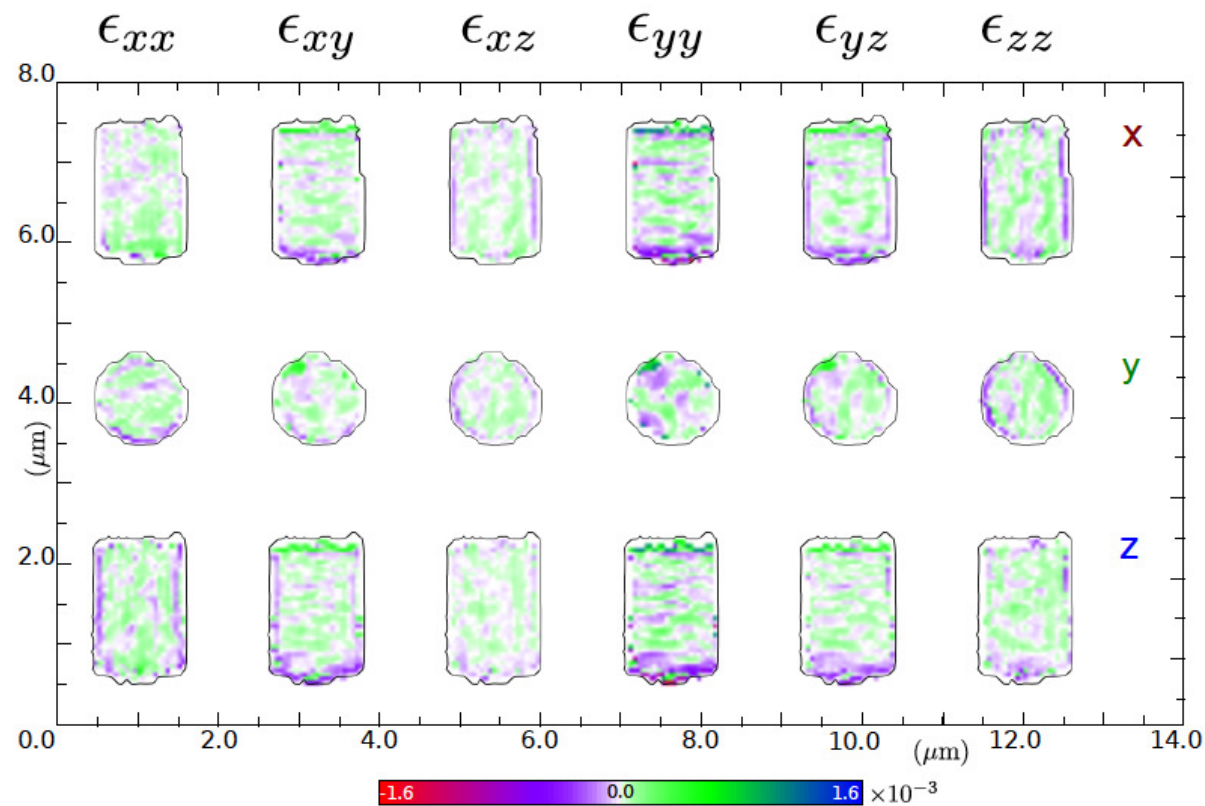


# Separate images 6 Bragg Peaks

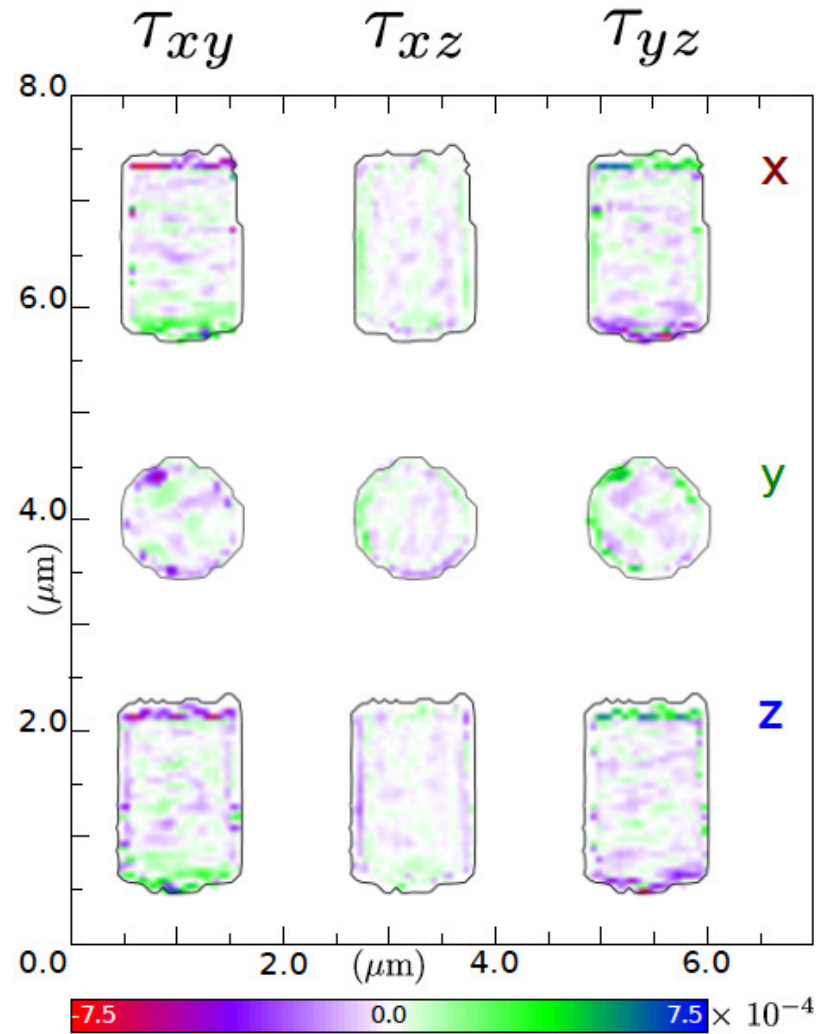


# Full Strain Tensor

$$\epsilon_{ij} = \frac{1}{2} \left( \frac{\partial u_j}{\partial x_i} + \frac{\partial u_i}{\partial x_j} \right) , \quad \tau_{ij} = \left( \frac{\partial u_j}{\partial x_i} - \frac{\partial u_i}{\partial x_j} \right)$$



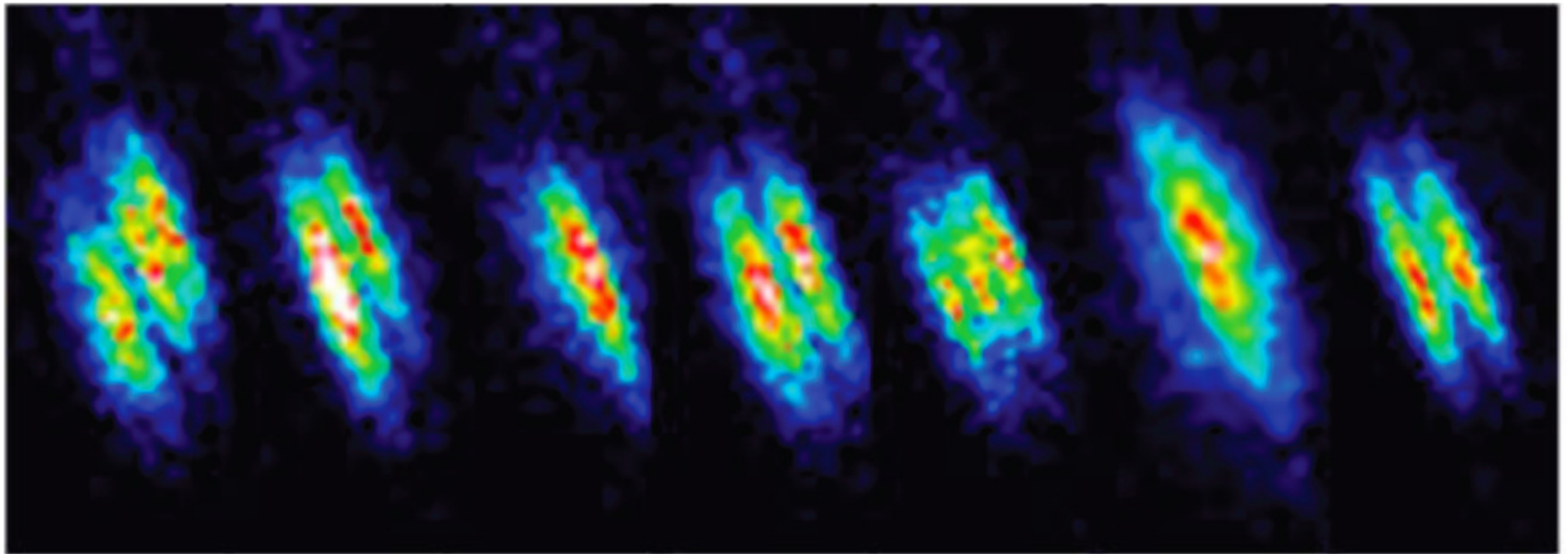
# ZnO Rigid-body Rotations



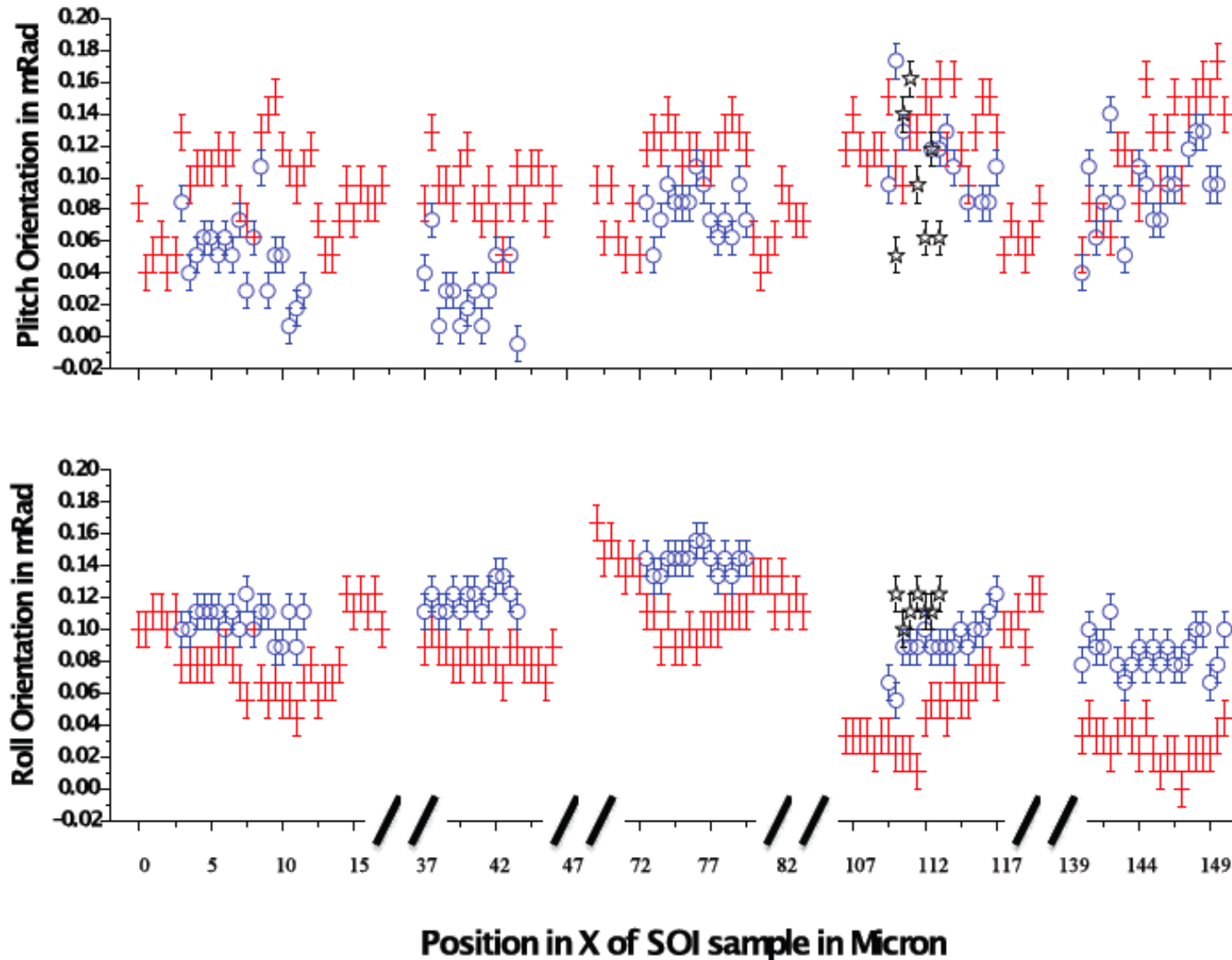
# Silicon on Insulator

Microdiffraction, 1.6 $\mu\text{m}$  beam, 9 $\mu\text{m}$  steps

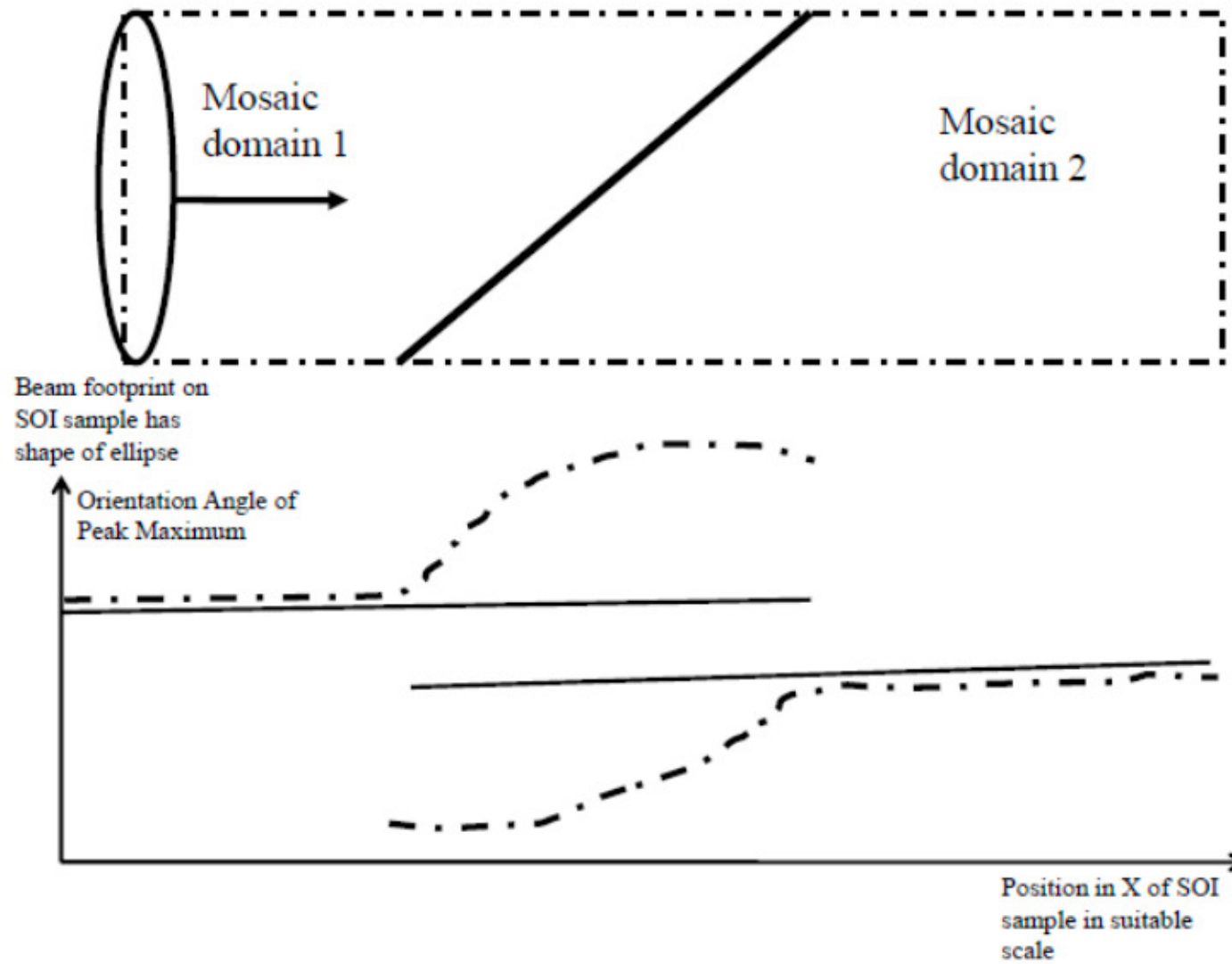
Xiaowen Shi et al, Z. Krist (2010)



# Mosaic domains on SOI film



# Coherent or incoherent effect?



# Conclusions

- CXD is a new branch of Crystallography
- 3D imaging practical for nanocrystals
- Phasing by computation instead of lens
- Strain fields imaged from asymmetric patterns
- Applications to semiconductors and metals