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Explaining the Effects of Government Spending Shocks [☆]Morten O. Ravn¹, Stephanie Schmitt-Grohé², Martín Uribe*

Abstract

Using panel structural VAR analysis and quarterly data from four industrialized countries, we document that an increase in government purchases raises output and private consumption, deteriorates the trade balance, and depreciates the real exchange rate. This pattern of comovement poses a puzzle for both neoclassical and Keynesian models. An explanation based on the deep-habit mechanism is proposed. An estimated two-country model with deep-habits is shown to replicate well the observed responses of output, consumption, and the trade balance, and the initial response of the real exchange rate to an estimated government spending shock.

Keywords: Government spending shocks, deep habits, real exchange rate. *JEL Classification:* F4, E3, E6.

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1. Introduction

Government spending is one of the main tools of macroeconomic stabilization policy. The vast fiscal stimulus packages enacted in response to the 2008 global recession exemplify the importance that policy makers place on this policy instrument. Therefore it is important to understand the macroeconomic consequences of variations in government spending and the mechanism through which they propagate. This paper presents an empirical and theoretical investigation into the effects of government spending shocks on output, consumption, the trade balance, and the real exchange rate. Our empirical analysis uses quarterly data from a panel of four industrialized countries, the United States, the United Kingdom, Canada, and Australia, over the post-Bretton Woods period and employs a structural vector autoregressive (SVAR) representation of the data. Following Blanchard and Perotti (2002), we identify government spending shocks by assuming that no innovation other than government spending shocks themselves can affect government spending within the quarter. A positive innovation in government spending is found to cause an expansion in output, an expansion in consumption, a deterioration of the trade balance, and a depreciation of the real exchange rate (that is, a decline in domestic prices relative to exchange-rate-adjusted foreign prices).

The effects of government spending shocks on domestic aggregate activity and private absorption have been extensively studied in the related empirical literature. Our finding that government spending shocks raise output and consumption is consistent with previous studies that have used identification assumptions and estimation techniques similar to those we employ in the present paper.³

By contrast, the effects of government spending shocks on the external sector of the economy, and in particular on the real exchange rate, have received considerably less attention.⁴ The empirical finding of a depreciation of the real exchange rate in response to a positive government spending shock is striking for it goes against the conventional wisdom. The standard view is that an increase in domestic absorption drives up domestic prices rendering the domestic economy relatively more expensive than the rest of the world. Contrary to this view, the data show that conditional on an unanticipated increase in government spending, the economy in which this innovation originates becomes relatively cheaper than its trading partners.

The observed responses of the real exchange rate and private consumption to innovations in government spending are hard to reconcile with the predictions of existing theoretical models of the transmission of government spending shocks. For instance, it is well known that the standard neoclassical model faces serious difficulties explaining the observed expansion in private consumption in response to a positive innovation in government spending. In this model an increase in government spending generates a negative wealth effect that causes an increase in labor supply, a decline in real wages, and a contraction in household spending.

The observed real depreciation of the exchange rate following a positive government spending shock is equally challenging for the neoclassical paradigm. In the absence of home bias, an increase in public consumption generates no changes in international relative prices. As a result the real exchange rate is unperturbed by the fiscal shock. In the presence of home bias, the relative price of domestically produced goods in terms of foreign produced goods increases, causing the neoclassical model to predict a counterfactual appreciation of the real exchange rate.

Our empirical findings pose a significant problem not only for the neoclassical model but also for models situated on the other end of the theoretical spectrum. For example, the Mundell-Flemming extension of the IS-LM model, while capturing the increase in consumption, fails to account for the observed real depreciation of the exchange rate triggered by an increase in public consumption. Within this framework, an increase in government purchases produces an expansion in aggregate demand that drives interest rates up. In turn, the elevated level of interest rates attracts foreign capital inflows, which increase the demand for domestic currency resulting in a nominal appreciation of the exchange rate. With product prices rigid in the short run, the nominal appreciation translates into a real appreciation.

Furthermore, more modern versions of the Mundell-Flemming IS-LM model with optimizing households and firms and sluggish nominal price adjustment can be shown to fail to predict a real exchange rate depreciation in response to a government spending increase. For instance, Monacelli and Perotti (2006) study the effects of government spending shocks in the context of a neo-Keynesian open-economy model with sticky

³See, for example, Rotemberg and Woodford, 1992; Blanchard and Perotti, 2002; Fatás and Mihov, 2001; Perotti, 2004, 2008; and Galí, López-Salido, and Vallés, 2007.

⁴Notable exceptions are Monacelli and Perotti (2006), Corsetti and Müller (2006), and Kim and Roubini (2008).

50 prices. These authors show that the neo-Keynesian framework is unable to generate the observed initial real
 51 depreciation in response to a positive innovation in government spending. Extensions of the neo-Keynesian
 52 open economy model that allow for rule-of-thumb consumers, while being able to explain qualitatively the
 53 rise in consumption, have also been shown to face difficulties explaining the observed initial real depreciation
 54 (see, for example, Erceg et al., 2005).

55 A central contribution of our investigation is to advance and test a theoretical explanation for the observed
 56 effects of government spending shocks based on the deep-habit mechanism developed by Ravn, Schmitt-
 57 Grohé, and Uribe (2006). To this end, we introduce deep habits into a two-country model. Under deep
 58 habits, an increase in domestic aggregate demand provides an incentive for firms selling in the domestic
 59 market to lower markups. Thus, an increase in government spending in the domestic economy leads to a
 60 decline in domestic markups relative to foreign markups. In this way, the domestic economy becomes less
 61 expensive relative to the foreign economy, or, equivalently, the real exchange rate depreciates. At the same
 62 time, a decline in domestic markups shifts the labor demand curve outward, giving rise to an increase in
 63 domestic real wages. In turn, the rise in wages induces households to substitute consumption for leisure.
 64 This substitution effect may be strong enough to offset the negative wealth effect stemming from the increase
 65 in public absorption, resulting in an equilibrium increase in private consumption.

66 The structural parameters defining the deep-habit mechanism are estimated using a limited information
 67 approach. The estimation of the model yields substantial support for the presence of deep habits in private
 68 and public consumption. The impulse responses of consumption, output, and the trade balance predicted
 69 by the deep-habit model is found to match well in size and shape their empirical counterparts. The model
 70 also matches the initial response of the real exchange rate. In particular, not only does our theoretical model
 71 predict an increase in output and a deterioration in the trade balance in response to a positive innovation in
 72 public spending, but also — and more importantly — an expansion in private consumption and an initial
 73 depreciation in the real exchange rate. While the model captures well the initial real depreciation of the
 74 exchange rate, it cannot explain its considerable persistence.

75 Section 2 estimates econometrically the effects of government spending shocks on output, consumption,
 76 the trade balance, and the real exchange rate using a panel SVAR model. The main difference between our
 77 empirical strategy and that adopted in the related literature, e.g., Monacelli and Perotti (2006), Corsetti
 78 and Müller (2006), and Kim and Roubini (2008), is our pooling of data across countries. We justify a panel
 79 analysis by observing that the identified effects of government spending shocks, particularly on consumption
 80 and the real exchange rate, whose behavior is the focus of our study, are similar across the individual countries
 81 considered.⁵ The purpose of our panel approach is to obtain an efficient estimate of a single benchmark
 82 against which to evaluate our proposed theoretical explanation of the transmission of government spending
 83 shocks. Section 3 presents a two-country model with deep habits. Section 4 explains at an intuitive level
 84 how the deep-habit mechanism affects the transmission of aggregate demand shocks. Section 5 describes the
 85 calibration of the nonestimated structural parameters of the model. Section 6 presents the estimation of the
 86 structural parameters defining the deep-habit mechanism. Section 7 compares the predicted and estimated
 87 impulse response functions. Section 8 explores the robustness of our findings to changes in key structural
 88 parameters, detrending technique, the introduction of endogenous investment, and computing predicted
 89 impulse responses by estimating SVARs on artificial data generated by the deep habit model. Section 9
 90 concludes.

91 2. The Observed Effects of Government Spending Shocks

92 The effects of government spending shocks on key macroeconomic variables are estimated using a struc-
 93 tural vector autoregression model of the form

⁵Country-by-country estimates are available in the supplementary material collected in Ravn, Schmitt-Grohé, and Uribe (2011) and posted on the website of the JME.

$$A \begin{bmatrix} \hat{g}_t \\ \hat{y}_t \\ \hat{c}_t \\ \widehat{nx}y_t \\ \hat{e}_t \end{bmatrix} = B(L) \begin{bmatrix} \hat{g}_{t-1} \\ \hat{y}_{t-1} \\ \hat{c}_{t-1} \\ \widehat{nx}y_{t-1} \\ \hat{e}_{t-1} \end{bmatrix} + \epsilon_t, \quad (1)$$

94 where g_t denotes real per capita government consumption spending deflated by the GDP deflator, y_t denotes
 95 real per capita GDP, c_t denotes real per capita private consumption of nondurables and services, $nx y_t$ denotes
 96 the net export-to-GDP ratio, and e_t denotes the real exchange rate defined as the ratio of a trade-weighted
 97 average of exchange-rate-adjusted foreign CPIs to the domestic CPI.⁶ According to this definition, an increase
 98 in e_t means that the real exchange rate of the domestic country depreciates, or that the domestic country
 99 becomes cheaper relative to its trading partners. A hat over a variable denotes the log deviation from trend,
 100 except for $nx y_t$, for which it indicates the level deviation from trend. All variables are seasonally adjusted,
 101 and detrended with a linear and quadratic trend. The variable ϵ_t is a mean-zero, serially uncorrelated vector
 102 of disturbances with diagonal variance-covariance matrix Σ_ϵ . The factor $B(L) \equiv B_0 + B_1 L + B_2 L^2 + \dots$
 103 denotes a lag polynomial, with L denoting the lag operator. The matrices of coefficients B_i and A are of
 104 size 5 by 5.

105 2.1. Identification

106 Following Blanchard and Perotti (2002), innovations to government spending are identified by assuming
 107 that government spending responds with at least a one-quarter lag to structural innovations other than
 108 innovations to government spending itself. Formally, the identification restriction requires that the first row
 109 of the matrix A contain unity in its first element and zeros in all other elements.

110 We estimate the structural VAR pooling quarterly data from Australia, Canada, the United Kingdom,
 111 and the United States. Our sample begins in the first quarter of 1975 and ends in the fourth quarter of
 112 2005. Our choice of countries is guided by our desire to limit attention to industrialized countries, and by the
 113 availability of reliable quarterly data on aggregate private consumption of nondurable goods and services and
 114 public consumption. The empirical strategy places emphasis on the availability of quarterly data, because,
 115 in our view, the validity of the Blanchard and Perotti (2002) identification strategy for government spending
 116 shocks depends crucially on the frequency at which the data are observed. With lower-than-quarterly
 117 frequency data, such as annual data, it is much less compelling to assume that within a period government
 118 spending cannot respond discretionarily to contemporaneous innovations in aggregate activity. That is, at
 119 a lower-than-quarterly frequency, one cannot be sure that the innovation to the \hat{g}_t equation is not a linear
 120 combination of all of the structural innovations of the SVAR model.

121 The rationale for pooling data is to gain efficiency and to obtain a single benchmark against which to
 122 evaluate the performance of our theoretical model to be presented in section 3. We estimate the VAR system
 123 by OLS including country dummies. A potential concern with the panel VAR is the inconsistency of the
 124 least squares parameter estimates due to the combination of fixed effects and lagged dependent variables
 125 (e.g., Nickell, 1981). However, because the time series dimension of our data is large (124 observations), the
 126 inconsistency problem is likely not to be a major concern. Monte Carlo analysis confirms that the size of the
 127 Nickell bias is small.⁷ A different potential problem is the possibility of correlated residuals across countries.
 128 To gauge the importance of this problem, impulse response functions were also computed from a feasible
 129 GLS estimation designed to correct for contemporaneous cross-country correlations in the error terms. The
 130 resulting impulse response functions (not shown) are fairly close to their OLS counterparts. Guided by the

⁶The data source for government consumption, GDP, and net exports is the OECD national accounts section. The source for the real exchange rate is the OECD Main Economic Indicators data base. And the sources for consumption of nondurables and services are the national statistical offices of each particular country. Government consumption is the sum of federal, state, and local public consumption spending.

⁷Specifically, the following experiment is carried out. Given the OLS estimates of A , the lag polynomial $B(L)$, and the country fixed effects, 10,000 artificial data series are generated by bootstrapping the estimated errors. Then the pooled fixed effects VAR is estimated by OLS on each of the artificial data series and the point estimates of the empirical impulse responses are compared with the median estimates over the 10,000 Monte Carlo experiments. The two estimates are found to be very similar.

131 likelihood ratio test proposed by Sims (1980), the SVAR specification allows for four lags.⁸

132 Our estimation procedure imposes that the matrices A and $B(L)$ are the same across the four countries
 133 from which we pool information. This simplifying assumption seems appropriate in light of the fact that
 134 estimations using individual country data yield similar results for the dynamic effects of government spending
 135 shocks on consumption and the real exchange rate. Our SVAR specification is similar to the one estimated
 136 in Monacelli and Perotti (2006). Like theirs, our specification comprises data from the US, the UK, Canada,
 137 and Australia, and applies the Blanchard and Perotti (2002) identification strategy. The main differences
 138 between our empirical approach and that of Monacelli and Perotti is that ours pools data, does not include
 139 taxes or the nominal interest rate in the SVAR specification, and that the sample considered is 16 quarters
 140 longer per country.

141 [Figure 1 about here.]

142 2.2. Estimation Results

143 Figure 1 displays with solid lines the empirical impulse response function of government spending, output,
 144 consumption, the net export-to-GDP ratio, and the real exchange rate to a unit innovation in government
 145 spending. The figure depicts with broken lines a two-standard error band on each side of the point estimate
 146 of the impulse response function computed using the delta method.⁹

147 The response of government spending is highly persistent, with a half life of about 5 quarters. A one-
 148 percent increase in government spending raises output by 0.1 percent. Assuming a government share of 19
 149 percent (the average of government spending over the sample period for the four countries in our sample),
 150 the government-spending multiplier, $\Delta y_t / \Delta g_t$, is 0.52 on impact, indicating that for each unit increase in
 151 public spending output increases by 0.52 units on impact.

152 Private consumption of nondurables and services experiences a persistent expansion following the increase
 153 in public spending. This finding is in line with many other SVAR studies on the effects of government
 154 spending. See, for example, Fatás and Mihov (2001) and Blanchard and Perotti (2002).¹⁰

155 The bottom left panel of figure 1 shows that the real exchange rate depreciates by one third of one
 156 percent when the economy is hit by a one-percent increase in government spending. That is, an expansion
 157 in public consumption causes the domestic country to become cheaper relative to its trading partners. This
 158 result is at odds with the conventional wisdom, according to which an expansion in government consumption
 159 is associated with an increase in domestic prices, that is, with an appreciation of the real exchange rate.
 160 The empirical evidence typically drawn upon to support the conventional view is based on raw correlations
 161 between government consumption and the real exchange rate. The difficulty with this type of evidence
 162 is that, in principle, movements in the real exchange rate and government spending may be driven by a
 163 multitude of shocks. By contrast, the impulse responses shown in figure 1, isolate movements in all variables
 164 driven exclusively by an innovation in government purchases. That is, the figure states that conditional on a
 165 positive innovation in government spending the real exchange rate depreciates. It follows that the evidence
 166 reported here and that emanating from the analysis of raw correlations are not necessarily contradictory. We
 167 note further that other empirical studies have also found that the real exchange rate depreciates in response
 168 to a positive government spending shock. For example, Monacelli and Perotti (2006) document this fact
 169 for each of the individual countries included in our panel. The reaction of the real exchange rate is quite

⁸The test rejects the hypothesis of one or two lags in favor of a longer lag structure. To maintain comparability with the related literature, a lag length of four quarters was adopted. The three-lag and four-lag specifications yield virtually identical impulse response functions and error bands.

⁹The results are robust to using parametric or nonparametric bootstrap methods for computing error bands.

¹⁰The finding that private consumption expands with government purchases is, however, not uncontroversial. A strand of the literature identifies innovations in government spending using the narrative approach. These studies find that in response to news about upcoming military buildups consumption fails to increase. In Ravn, Schmitt-Grohé and Uribe (2007), it is argued that the effects of government spending shocks estimated using the SVAR and narrative approaches are not at odds with each other. There the case is made that the SVAR methodology, followed here, identifies unanticipated changes in government spending, while the narrative approach identifies news (or anticipated innovations) in future expansion in public spending. Moreover, that study argues that in general these two types of shock trigger quite different impulse responses in a theoretical model of the transmission of public spending shocks. And in particular, that paper shows that in the context of the deep-habits model developed here, the theoretical impulse responses to these two types of shock are in line with their empirical counterparts.

170 persistent. The peak depreciation occurs only 10 quarters after the innovation in government spending takes
171 place.

172 The expansion in public spending results in a protracted albeit small deterioration in the trade balance.
173 Corsetti and Müller (2006) and Monacelli and Perotti, consistent with our results, also report a worsening
174 of the trade balance in response to a positive innovation in public spending.

175 Summarizing, our empirical results deliver four regularities that serve as the basis for evaluating the
176 theory presented in the next section. Namely, in response to an increase in government spending output and
177 consumption increase, the trade balance deteriorates, and the real exchange rate depreciates. These empirical
178 regularities are quite robust. They also emerge in country-by-country estimations, under specifications
179 including additional fiscal variables, such as taxes, and monetary policy variables, such as the nominal
180 interest rate (see Monacelli and Perotti, 2006), and under alternative detrending schemes (see section 8
181 below).

182 3. A Two-Country Model of Pricing to Habits

183 The model economy consists of two countries, the home country and the foreign country. Each country
184 specializes in the production of a set of differentiated goods. We denote by a the set of goods produced by
185 the home country and by b the set of goods produced by the foreign country. All goods are internationally
186 traded.

187 3.1. Households

188 Only the household's problem in the domestic economy is described. The foreign counterpart is a mirror
189 image. The domestic economy is populated by a large number of identical households with preferences
190 described by the utility function

$$E_0 \sum_{t=0}^{\infty} \beta^t U(x_t^c, h_t). \quad (2)$$

191 The variable x_t^c is a composite defined as

$$x_t^c = \chi(x_{a,t}^c, x_{b,t}^c), \quad (3)$$

192 where the aggregator function χ is assumed to be increasing and homogeneous of degree one in both ar-
193 guments. The variable $x_{a,t}^c$ is a habit-adjusted composite consumption good of varieties of goods of type
194 a .

195 3.1.1. Deep Habits

196 Following Ravn, Schmitt-Grohé, and Uribe (2006), it is assumed that habits form at the level of each
197 individual variety of goods instead of at the level of the aggregate consumption good. Further, deep habits
198 are assumed to be external to the individual household (i.e., habits are modeled as catching up with the
199 Joneses good by good). Formally, $x_{a,t}^c$ is given by

$$x_{a,t}^c = \left[\int_0^1 (c_{i,a,t} - \theta_a^c s_{i,a,t-1}^c)^{1-1/\eta} di \right]^{1/(1-1/\eta)}. \quad (4)$$

200 Here $c_{i,a,t}$ denotes consumption of variety i of goods belonging to the set a in period t . The parameter
201 $\theta_a^c \in [0, 1)$ measures the intensity of deep external habits for consumption goods of type a . When θ_a^c is equal
202 to zero, preferences for goods of type a display no deep habit formation. The parameter $\eta > 1$ represents
203 the intratemporal elasticity of substitution across varieties. The variable $s_{i,a,t}^c$ denotes the stock of external
204 habit in consumption of variety i of good a . This habit stock is assumed to evolve according to the following
205 law of motion:

$$s_{i,a,t}^c = \rho s_{i,a,t-1}^c + (1 - \rho) \tilde{c}_{i,a,t}, \quad (5)$$

206 where $\tilde{c}_{i,a,t}$ denotes the average per capita consumption of variety i of good a in the domestic country; that
 207 is, $\tilde{c}_{i,a,t}$ is the integral of $c_{i,a,t}$ over all domestic households. The parameter $1 - \rho \in (0, 1]$ denotes the rate
 208 at which the stock of external habits decays over time.

209 Similarly, $x_{b,t}^c$ is given by

$$x_{b,t}^c = \left[\int_0^1 (c_{i,b,t} - \theta_b^c s_{i,b,t-1}^c)^{1-1/\eta} di \right]^{1/(1-1/\eta)}, \quad (6)$$

210 with

$$s_{i,b,t}^c = \rho s_{i,b,t-1}^c + (1 - \rho) \tilde{c}_{i,b,t}. \quad (7)$$

211 To characterize the household's demands for varieties of type- a and type- b goods, consider a two-step
 212 problem. Suppose the household has determined its desired consumption of the aggregate goods a and b ,
 213 that is, $x_{a,t}^c$ and $x_{b,t}^c$. Then it is optimal for the household to distribute its purchases of individual varieties
 214 to minimize costs, that is,

$$\min_{c_{i,a,t}} \int_0^1 P_{i,a,t} c_{i,a,t} di \quad (8)$$

215 subject to (4). This minimization problem yields the following demand function for variety i of good a :

$$c_{i,a,t} = \left(\frac{P_{i,a,t}}{P_{a,t}} \right)^{-\eta} x_{a,t}^c + \theta_a^c s_{i,a,t-1}^c, \quad (9)$$

216 where $P_{a,t}$ denotes a price index for goods of type a given by

$$P_{a,t} = \left[\int_0^1 (P_{j,a,t})^{1-\eta} dj \right]^{1/(1-\eta)}. \quad (10)$$

217 Similarly, one can express the demand for variety i of good b as

$$c_{i,b,t} = \left(\frac{P_{i,b,t}}{P_{b,t}} \right)^{-\eta} x_{b,t}^c + \theta_b^c s_{i,b,t-1}^c, \quad (11)$$

218 where $P_{b,t}$ is a price index of goods of type b defined as

$$P_{b,t} = \left[\int_0^1 (P_{j,b,t})^{1-\eta} dj \right]^{1/(1-\eta)}. \quad (12)$$

219 Note that the demand for each variety of good a , say, is decreasing in its relative price, $P_{i,a,t}/P_{a,t}$, increasing
 220 in the level of habit-adjusted consumption of the composite good of type a , $x_{a,t}^c$, and increasing in the stock
 221 of habit of the variety in question $s_{i,a,t-1}^c$.

222 Total expenditure on goods of type a in period t is given by

$$\int_0^1 P_{i,a,t} c_{i,a,t} di = P_{a,t} x_{a,t}^c + \theta_a^c \int_0^1 P_{i,a,t} s_{i,a,t-1}^c di. \quad (13)$$

223 Let $\omega_{a,t}$ and $\omega_{b,t}$ be defined, respectively, as $\omega_{a,t} \equiv \theta_a^c \int_0^1 P_{i,a,t} s_{i,a,t-1}^c di$ and $\omega_{b,t} \equiv \theta_b^c \int_0^1 P_{i,b,t} s_{i,b,t-1}^c di$. Note
 224 that because habits are assumed to be external, the household takes both $\omega_{a,t}$ and $\omega_{b,t}$ as exogenously given.

225 It follows that total expenditure on goods of type a and b , respectively, can be written as $\int_0^1 P_{i,a,t} c_{i,a,t} di =$
 226 $P_{a,t} x_{a,t}^c + \omega_{a,t}$ and $\int_0^1 P_{i,b,t} c_{i,b,t} di = P_{b,t} x_{b,t}^c + \omega_{b,t}$.

227 3.1.2. Budget constraint and optimality conditions

228 In each period $t \geq 0$, households are assumed to have access to complete contingent claims markets. Let
 229 $r_{t,t+j}$ denote the stochastic discount factor such that $E_t r_{t,t+j} d_{t+j}$ is the period- t price of a random payment
 230 d_{t+j} of the (numeraire good) in period $t + j$. In addition, households are assumed to be entitled to the

231 receipt of pure profits from the ownership of firms, Φ_t . Households pay lump-sum taxes in the amount T_t .
 232 Then, the domestic representative household's period-by-period budget constraint can be written as

$$P_{a,t}x_{a,t}^c + \omega_{a,t} + P_{b,t}x_{b,t}^c + \omega_{b,t} + E_t r_{t,t+1} d_{t+1} + T_t = d_t + W_t h_t + \Phi_t. \quad (14)$$

233 The variable W_t denotes the wage rate. In addition, households are assumed to be subject to a borrowing
 234 constraint of the form $\lim_{j \rightarrow \infty} E_t r_{t,t+j} d_{t+j} \geq 0$, which prevents them from engaging in Ponzi games. The
 235 representative household's optimization problem consists in choosing processes $x_{a,t}^c$, $x_{b,t}^c$, h_t , and d_{t+1} to
 236 maximize the lifetime utility function (2) subject to (3), (14), and the no-Ponzi-game constraint, taking as
 237 given the processes for $\omega_{a,t}$, $\omega_{b,t}$, W_t , T_t , and Φ_t and initial asset holdings d_0 .

238 The first-order conditions of the household's optimization problem are the constraints (3) and (14), the
 239 no-Ponzi-game constraint holding with equality, and

$$\frac{\chi_a(x_{a,t}^c, x_{b,t}^c)}{\chi_b(x_{a,t}^c, x_{b,t}^c)} = \frac{P_{a,t}}{P_{b,t}}, \quad (15)$$

$$-\frac{U_h(x_t^c, h_t)}{U_x(x_t^c, h_t) \chi_a(x_{a,t}^c, x_{b,t}^c)} = \frac{W_t}{P_{a,t}}, \quad (16)$$

240 and

$$\frac{U_x(x_t^c, h_t) \chi_a(x_{a,t}^c, x_{b,t}^c)}{P_{a,t}} r_{t,t+1} = \beta \frac{U_x(x_{t+1}^c, h_{t+1}) \chi_a(x_{a,t+1}^c, x_{b,t+1}^c)}{P_{a,t+1}}. \quad (17)$$

241 The first equation states that the marginal rate of substitution between the composite goods a and b must
 242 equal their relative price. The second equation implicitly defines the supply of labor. It equates the real
 243 domestic product wage to the marginal rate of substitution between leisure and consumption of composite
 244 good a . The last equation is a standard asset pricing relation equating the price of contingent claims to the
 245 intertemporal marginal rate of substitution.

246 3.2. The Government

247 Like households, the government is assumed to form habits on consumption of individual varieties of
 248 goods. This assumption is important for understanding the transmission of government purchases shocks in
 249 the context of our model. The deep-habit formulation in public spending can be interpreted as private house-
 250 holds valuing public goods in a way that is separable from private consumption and leisure and households
 251 deriving external habits from consumption of government-provided goods. By good-specific external habit
 252 formation in the consumption of public goods we mean situations in which the provision of public services
 253 in one community—such as street lighting, traffic signals, yard-waste collection—creates the desire in other
 254 communities to have access to the same type of service. Alternatively, one can assume that the government
 255 forms procurement relationships that create a tendency for it to favor transactions with sellers that supplied
 256 public goods in the past.

257 Government habits are assumed to be external. Conceivably, government habits could be treated as
 258 internal to the government even if they are external to their beneficiaries, namely households. This alternative
 259 is, however, less tractable, and is therefore not pursued here. In the econometric estimation of the model,
 260 presented later in the paper, we let the data tell how much habit formation there is in public spending.

261 The government is assumed to aggregate individual varieties of domestic and foreign goods to produce
 262 two intermediate composite goods denoted $x_{a,t}^g$ and $x_{b,t}^g$, using the same aggregator function as the private
 263 sector:¹¹

$$x_{a,t}^g = \left[\int_0^1 (g_{i,a,t} - \theta_a^g s_{i,a,t-1}^g)^{1-1/\eta} di \right]^{1/(1-1/\eta)} \quad (18)$$

264 and

¹¹A more general formulation would allow for the government and consumers to absorb different subsets of goods.

$$x_{b,t}^g = \left[\int_0^1 (g_{i,b,t} - \theta_b^g s_{i,b,t-1}^g)^{1-1/\eta} di \right]^{1/(1-1/\eta)}. \quad (19)$$

265 The parameters $\theta_a^g, \theta_b^g \in [0, 1]$ measure the degree of habit formation in government consumption of domestic
 266 and foreign goods, respectively. The variables $s_{i,a,t}^g$ and $s_{i,b,t}^g$ denote the government's stocks of habit in
 267 variety i of goods a and b , respectively, and are assumed to evolve over time as

$$s_{i,a,t}^g = \rho s_{i,a,t-1}^g + (1 - \rho)g_{i,a,t} \quad (20)$$

268 and

$$s_{i,b,t}^g = \rho s_{i,b,t-1}^g + (1 - \rho)g_{i,b,t}, \quad (21)$$

269 where $1 - \rho \in (0, 1]$ denotes the rate of depreciation of the stocks of habit. The government combines the
 270 intermediate goods $x_{a,t}^g$ and $x_{b,t}^g$ to produce a final, public good x_t^g according to the relationship

$$x_t^g = \chi(x_{a,t}^g, x_{b,t}^g). \quad (22)$$

271 Note that the aggregator function χ is the same as the one used by private consumers.

272 As in the empirical SVAR model of section 2, let g_t denote total real government spending expressed in
 273 units of domestic GDP (i.e., nominal government spending divided by the GDP deflator). Then, letting P_t^y
 274 denote the GDP deflator, to be defined later, one obtains

$$g_t \equiv \frac{\int_0^1 (P_{i,a,t}g_{i,a,t} + P_{i,b,t}g_{i,b,t}) di}{P_t^y}. \quad (23)$$

275 3.2.1. Government spending process

276 To allow for the empirical and the theoretical models to feature the same feedback mechanism and driving
 277 process for total government purchases, we assume that fiscal policy takes the form of a feedback rule given
 278 by the first equation of the SVAR system given in equation (1). Formally, g_t satisfies

$$\hat{g}_t = B^1(L) \begin{bmatrix} \hat{g}_{t-1} \\ \hat{y}_{t-1} \\ \hat{c}_{t-1} \\ \widehat{nx}_{t-1} \\ \hat{c}_{t-1} \end{bmatrix} + \epsilon_t^1, \quad (24)$$

279 where $B^1(L)$ denotes the first row of $B(L)$ and ϵ_t^1 denotes the first element of the vector of innovations ϵ_t .
 280 Here, hatted variables denote log-deviations from deterministic steady-state values, except for the variable
 281 \widehat{nx}_{t-1} , for which a hat indicates the level deviation of nx_{t-1} from its deterministic steady state. Note that
 282 the values assigned to $B^1(L)$ are those estimated in section 2. However, the behavior of the endogenous
 283 variables appearing in the above law of motion for g_t is dictated by the dynamics of the theoretical model.
 284 For this reason, the theoretical and empirical impulse responses of g_t to an innovation in ϵ_t^1 will in general
 285 not coincide. Government spending is assumed to be financed by lump-sum taxes.

286 The government's problem consists in choosing $g_{i,a,t}$ and $g_{i,b,t}$, $i \in [0, 1]$, to maximize x_t^g subject to
 287 (18)-(23), taking as given $g_t, P_t^y, P_{i,a,t}, P_{i,b,t}, s_{i,a,t-1}^g$, and $s_{i,b,t-1}^g$ for all $i \in [0, 1]$ and $t \geq 0$.

288 The government's problem implies demand functions for individual varieties of goods a and b of the form

$$g_{i,a,t} = \left(\frac{P_{i,a,t}}{P_{a,t}} \right)^{-\eta} x_{a,t}^g + \theta_a^g s_{i,a,t-1}^g \quad (25)$$

289 and

$$g_{i,b,t} = \left(\frac{P_{i,b,t}}{P_{b,t}} \right)^{-\eta} x_{b,t}^g + \theta_b^g s_{i,b,t-1}^g. \quad (26)$$

290 3.3. Firms

291 Goods of type a are produced exclusively in the domestic country, and goods of type b are produced
 292 exclusively abroad. Each individual variety of good of type a or b is assumed to be produced by a monopolist.
 293 Each good $i \in [0, 1]$ is manufactured using labor as the sole input with a linear production technology.
 294 Specifically domestic output of variety i of type a , denoted $y_{i,a,t}$, is produced according to the relationship

$$y_{i,a,t} = h_{i,a,t}, \quad (27)$$

295 where $h_{i,a,t}$ denotes labor input in producing variety i of good a .

296 The producer of variety i of good a faces demands from the private and public sectors in the domestic
 297 and foreign countries. The private and public domestic demand functions are given by

$$c_{i,a,t} = \left(\frac{P_{i,a,t}}{P_{a,t}} \right)^{-\eta} x_{a,t}^c + \theta_a^c s_{i,a,t-1}^c \quad (28)$$

298 and

$$g_{i,a,t} = \left(\frac{P_{i,a,t}}{P_{a,t}} \right)^{-\eta} x_{a,t}^g + \theta_a^g s_{i,a,t-1}^g. \quad (29)$$

299 Letting an asterisk denote a foreign variable or parameter, the foreign private and public components of
 300 demand for variety i of type a goods are given by

$$c_{i,a,t}^* = \left(\frac{P_{i,a,t}^*}{P_{a,t}^*} \right)^{-\eta} x_{a,t}^{c*} + \theta_a^{c*} s_{i,a,t-1}^{c*} \quad (30)$$

301 and

$$g_{i,a,t}^* = \left(\frac{P_{i,a,t}^*}{P_{a,t}^*} \right)^{-\eta} x_{a,t}^{g*} + \theta_a^{g*} s_{i,a,t-1}^{g*}. \quad (31)$$

302 Implicit in the above demand functions are the assumptions that firms can price discriminate between the
 303 domestic and foreign markets but not between the government and households residing in the same country.

304 A number of important implications for the model's predictions regarding deviations from the law of one
 305 price, and hence movements in the real exchange rate, are evident from inspection of the above demand
 306 functions. First, each demand function for an individual variety of goods is of the form $d_t = p_t^{-\eta} x_t + \theta s_{t-1}$.
 307 That is, each demand function is the sum of a price-elastic component, $p_t^{-\eta} x_t$, and a price inelastic component,
 308 θs_{t-1} . The price elastic component has price elasticity η and is proportional to a measure of current aggregate
 309 demand, x_t . The price inelastic term is purely habitual in nature. It follows that the price elasticity of each
 310 demand function is a weighted average of η and 0, with the weight on η given by the relative importance
 311 of the price-elastic, nonhabitual demand component in total demand. An increase in aggregate demand
 312 enlarges the importance of the price elastic component of demand increasing the price elasticity. In other
 313 words, the price elasticity of each demand function is procyclical. Second, the fact that the price elasticity
 314 is procyclical opens the possibility for markups to move countercyclically in equilibrium. Third, in spite of
 315 the fact that the elasticity of the price elastic component of demand, η , is assumed to be identical across
 316 countries, the price elasticity of demand can in principle be different across countries. This is because the
 317 aggregate demand, x_t , or the stocks of habit, s_{t-1} , themselves can vary across countries. This implies that
 318 firms have an incentive to charge different markups domestically and abroad. We refer to this incentive
 319 for price discrimination as 'pricing to habits' as it originates from the presence of a habitual demand for
 320 individual varieties of goods. More importantly, pricing to habits gives rise to deviations from the law of one
 321 price over the business cycle at the level of individual goods traded across borders. Finally, because firms
 322 understand that the stock of habit is a weighted average of all past sales, their profit-maximization problem
 323 is dynamic in nature. Thus, customer-market and brand-switching cost considerations in the spirit of Phelps
 324 and Winter (1970) and Froot and Klemperer (1989) will endogenously emerge in the pricing behavior of
 325 firms, affecting the size and persistence of deviations from the law of one price and movements in the real
 326 exchange rate.

3.3.1. The price setting problem

The firm's problem consists in choosing processes $\{P_{i,a,t}, P_{i,a,t}^*, c_{i,a,t}, g_{i,a,t}, c_{i,a,t}^*, g_{i,a,t}^*, s_{i,a,t}^c, s_{i,a,t}^g, s_{i,a,t}^{c*}, s_{i,a,t}^{g*}, h_{i,a,t}\}_{t=0}^{\infty}$ to maximize

$$E_0 \sum_{t=0}^{\infty} r_{0,t} [P_{i,a,t}(c_{i,a,t} + g_{i,a,t}) + P_{i,a,t}^*(c_{i,a,t}^* + g_{i,a,t}^*) - W_t h_{i,a,t}] \quad (32)$$

subject to

$$c_{i,a,t} + g_{i,a,t} + c_{i,a,t}^* + g_{i,a,t}^* = h_{i,a,t}, \quad (33)$$

$$c_{i,a,t} = \left(\frac{P_{i,a,t}}{P_{a,t}}\right)^{-\eta} x_{a,t}^c + \theta_a^c s_{i,a,t-1}^c, \quad (34)$$

$$g_{i,a,t} = \left(\frac{P_{i,a,t}}{P_{a,t}}\right)^{-\eta} x_{a,t}^g + \theta_a^g s_{i,a,t-1}^g, \quad (35)$$

$$c_{i,a,t}^* = \left(\frac{P_{i,a,t}^*}{P_{a,t}^*}\right)^{-\eta} x_{a,t}^{c*} + \theta_a^{c*} s_{i,a,t-1}^{c*}, \quad (36)$$

$$g_{i,a,t}^* = \left(\frac{P_{i,a,t}^*}{P_{a,t}^*}\right)^{-\eta} x_{a,t}^{g*} + \theta_a^{g*} s_{i,a,t-1}^{g*}, \quad (37)$$

$$s_{i,a,t}^c = \rho s_{i,a,t-1}^c + (1 - \rho)c_{i,a,t}, \quad (38)$$

$$s_{i,a,t}^g = \rho s_{i,a,t-1}^g + (1 - \rho)g_{i,a,t}, \quad (39)$$

$$s_{i,a,t}^{c*} = \rho s_{i,a,t-1}^{c*} + (1 - \rho)c_{i,a,t}^*, \quad (40)$$

and

$$s_{i,a,t}^{g*} = \rho s_{i,a,t-1}^{g*} + (1 - \rho)g_{i,a,t}^*, \quad (41)$$

taking as given the processes $r_{0,t}, W_t, P_{a,t}, P_{a,t}^*, x_{a,t}^c, x_{a,t}^g, x_{a,t}^{c*}, x_{a,t}^{g*}$, and the initial conditions $s_{i,a,-1}^c, s_{i,a,-1}^g, s_{i,a,-1}^{c*}, s_{i,a,-1}^{g*}$. The associated optimality conditions are presented in Ravn, Schmitt-Grohé, and Uribe (2011). Foreign firms face a similar optimization problem.

3.4. Symmetric Equilibrium

We assume that given the type of good (a or b), the type of consumer (private or public), and the location of the consumer (domestic market or foreign market), initial habit stocks are identical across different varieties. Then, in a symmetric equilibrium, all firms producing varieties of good a for the domestic market will charge the same price. That is, $P_{i,a,t} = P_{a,t}$ for all i . Similarly, all firms producing varieties of good a for the foreign market will charge the same price, or $P_{i,a,t}^* = P_{a,t}^*$ for all i . The same symmetry applies to the foreign produced goods (type b), that is, $P_{i,b,t} = P_{b,t}$ and $P_{i,b,t}^* = P_{b,t}^*$ for all i . It follows from these assumptions that equilibrium consumption will be the same across varieties as well, that is, $c_{i,a,t} = c_{a,t}$, $g_{i,a,t} = g_{a,t}$, $c_{i,b,t} = c_{b,t}$, $g_{i,b,t} = g_{b,t}$, $c_{i,a,t}^* = c_{a,t}^*$, $g_{i,a,t}^* = g_{a,t}^*$, $c_{i,b,t}^* = c_{b,t}^*$, and $g_{i,b,t}^* = g_{b,t}^*$, for all i .

3.5. Asset Market Structure

We close the model by assuming that financial markets are complete and that financial capital can flow freely across countries. This means that domestic and foreign households face the same contingent-claim prices $r_{t,t+1}$. Combining the domestic Euler equation (17) with its foreign counterpart to eliminate $r_{t,t+1}$ yields $\left[U_x(x_{t+1}^c, h_{t+1}) \chi_a(x_{a,t+1}^c, x_{b,t+1}^c) P_{a,t} \right] / \left[U_x(x_t^c, h_t) \chi_a(x_{a,t}^c, x_{b,t}^c) P_{a,t+1} \right] = \left[U_{x^*}(x_{t+1}^{c*}, h_{t+1}^*) \chi_a^*(x_{a,t+1}^{c*}, x_{b,t+1}^{c*}) P_{a,t}^* \right] / \left[U_{x^*}(x_t^{c*}, h_t^*) \chi_a^*(x_{a,t}^{c*}, x_{b,t}^{c*}) P_{a,t+1}^* \right]$. Because this expression holds in every date and every state, it follows that $\frac{U_x(x_t^c, h_t) \chi_a(x_{a,t}^c, x_{b,t}^c)}{P_{a,t}}$ must be proportional to $\frac{U_{x^*}(x_t^{c*}, h_t^*) \chi_a^*(x_{a,t}^{c*}, x_{b,t}^{c*})}{P_{a,t}^*}$. The factor of proportionality is

determined by the relative wealth of the two countries. We consider a case in which both countries are equally wealthy so that the factor of proportionality is unity. It follows that

$$\frac{P_{a,t}^*}{P_{a,t}} = \frac{U_{x^*}(x_t^{c^*}, h_t^*) \chi_a^*(x_{a,t}^{c^*}, x_{b,t}^{c^*})}{U_x(x_t^c, h_t) \chi_a(x_{a,t}^c, x_{b,t}^c)}. \quad (42)$$

The complete set of equilibrium conditions is given in Ravn, Schmitt-Grohé, and Uribe (2011).

3.6. Theoretical Counterparts of Variables Included in the SVAR

Two good-specific real exchange rates are defined. One is the relative price of good a abroad in terms of units of good a at home, which is denoted by $e_{a,t}$. The second is the relative price of good b abroad in terms of units of good b in the home market, denoted $e_{b,t}$. Formally, the real exchange rates for goods a and b , respectively, are given by $e_{a,t} = \frac{P_{a,t}^*}{P_{a,t}}$ and $e_{b,t} = \frac{P_{b,t}^*}{P_{b,t}}$. Because firms can price discriminate across domestic and foreign markets, good-specific real exchange rates need not be unity. When the real exchange rate for a particular good is different from one, we say that the law of one price for that good is violated.

At a more aggregate level, the real exchange rate, denoted e_t , is defined as the relative price of foreign consumption in terms of domestic consumption, or

$$e_t \equiv \frac{P_t^*}{P_t}, \quad (43)$$

where P_t and P_t^* denote, respectively, the domestic and foreign consumer price indices. In the model economy under study, however, the presence of habit formation at a good-by-good level implies that there is no natural concept of either an aggregate consumption price index or even aggregate consumption. We therefore define the consumption price index as an expenditure weighted average of the price of final goods: $P_t = \gamma P_{a,t} + (1-\gamma)P_{b,t}$, where γ is a fixed weight defined as $\gamma = (P_a(c_a + g_a)) / (P_a(c_a + g_a) + P_b(c_b + g_b))$, where variables without a time subscript represent the deterministic steady state value of their time-subscripted counterparts.

We adopt a fixed-weight price index to mimic a common practice in developed countries, whereby consumer price indices take the Laspeyres form. This definition of the consumer price index takes an arithmetic mean of prices in the broad categories a and b . Within each of these two categories, price indices are constructed as geometric means of individual prices. This convention is in line with the construction of the consumer price index in the United States where, since January 1999, a geometric mean formula has been used to average prices within item categories, while an arithmetic mean formula has been used to average prices across item categories. The consumer price index in the foreign country is defined in a similar fashion:

$$P_t^* = \gamma^* P_{a,t}^* + (1-\gamma^*) P_{b,t}^*, \quad \text{with } \gamma^* = \frac{P_a^*(c_a^* + g_a^*)}{P_a^*(c_a^* + g_a^*) + P_b^*(c_b^* + g_b^*)}.$$

Let τ_t denote the domestic relative price of imported goods in terms of domestically produced goods. That is, $\tau_t \equiv \frac{P_{b,t}}{P_{a,t}}$. One can then express the real exchange rate in terms of this relative price and the good-specific real exchange rates:

$$e_t = \frac{\gamma^* e_{a,t} + (1-\gamma^*) e_{b,t} \tau_t}{\gamma + (1-\gamma) \tau_t}. \quad (44)$$

Define aggregate domestic consumption as $c_t = (P_{a,t} c_{a,t} + P_{b,t} c_{b,t}) / P_t$, or $c_t = \frac{c_{a,t} + \tau_t c_{b,t}}{\gamma + (1-\gamma) \tau_t}$. Similarly, define foreign aggregate consumption as $c_t^* = (P_{a,t}^* c_{a,t}^* + P_{b,t}^* c_{b,t}^*) / P_t^*$, or $c_t^* = \frac{e_{a,t} c_{a,t}^* + e_{b,t} \tau_t c_{b,t}^*}{\gamma^* e_{a,t} + (1-\gamma^*) e_{b,t} \tau_t}$.

Define real GDP as follows. Pick steady-state prices as the base-year prices. Recalling that in the steady state all varieties of goods of type a are sold at the same price domestically and abroad (i.e., $P_{i,a} = P_{i,a}^* = P_a$ for all i), normalizing the steady-state price of the domestic good at unity ($P_a = 1$), and taking into account the linearity of the production technology, real GDP at base-year prices, denoted y_t , is given by $y_t = h_t$.

Market clearing for domestically produced goods requires that $y_t = c_{a,t} + g_{a,t} + c_{a,t}^* + g_{a,t}^*$. The GDP deflator P_t^y is defined as the ratio of nominal GDP to real GDP. Nominal GDP is given by $P_{a,t}(c_{a,t} + g_{a,t}) + P_{a,t}^*(c_{a,t}^* + g_{a,t}^*)$. Then, the GDP deflator is given by $P_t^y = [P_{a,t}(c_{a,t} + g_{a,t}) + P_{a,t}^*(c_{a,t}^* + g_{a,t}^*)] / h_t$.

The nominal trade balance is the difference between nominal exports, given by $P_{a,t}^*(c_{a,t}^* + g_{a,t}^*)$, and nominal imports, given by $P_{b,t}(c_{b,t} + g_{b,t})$. The trade balance-to-GDP ratio, nxy_t , can then be written as

$$nxy_t = \left[e_{a,t}(c_{a,t}^* + g_{a,t}^*) - \tau_t(c_{b,t} + g_{b,t}) \right] / \left[(c_{a,t} + g_{a,t}) + e_{a,t}(c_{a,t}^* + g_{a,t}^*) \right].$$

The variables g_t , y_t , c_t , nxy_t , and e_t are conceptually consistent with the homonymous variables used in the empirical analysis of section 2.

4. How the Pricing-To-Habits Mechanism Works

We now discuss at an intuitive level the potential of the pricing-to-habits mechanism to predict a depreciation of the real exchange rate and an expansion in private consumption in response to an increase in domestic government spending. To simplify the exposition, in this section, we consider the special case in which all stocks of habit depreciate completely after one period ($\rho = 0$) and the degrees of habit formation in private and public consumption are the same domestically and abroad ($\theta_a^c = \theta_a^g = \theta_a^{c*} = \theta_a^{g*} = \theta$). In this case, one can show that the equilibrium markup of price over marginal cost charged on varieties of good a in the domestic market, denoted $\mu_{a,t} \equiv P_{a,t}/W_t$, must satisfy

$$\mu_{a,t} = \left[1 - \frac{1}{\eta(1 - \theta d_{a,t-1}/d_{a,t})} + \theta \Omega_{a,t} \right]^{-1}, \quad (45)$$

where $d_{a,t} \equiv c_{a,t} + g_{a,t}$ denotes aggregate domestic demand for good a and $\Omega_{a,t}$ denotes the present discounted value of a sale in the domestic market in period $t + 1$. Note that in the absence of deep habits ($\theta = 0$), the markup is constant and equal to $1/(1 - 1/\eta)$. The above expression shows that under deep habits, the markup falls in response to expansions in domestic aggregate demand for good a , that is, when $d_{a,t}$ increases. We refer to this effect as the price elasticity effect of deep habits. It originates from the fact that when demand increases, the relative importance of the price-inelastic (or habitual) component of demand falls. In addition, the markup is decreasing in the present discounted value of a future sale, $\Omega_{a,t}$. We refer to this effect as the intertemporal effect of deep habits. This effect arises because when the present value of a future sale increases, it pays for the firm to invest in market share today by lowering current markups.

In the foreign market for good a , domestic firms charge a markup $\mu_{a,t}^*$ given by

$$\mu_{a,t}^* = \left[1 - \frac{1}{\eta(1 - \theta d_{a,t-1}^*/d_{a,t}^*)} + \theta \Omega_{a,t}^* \right]^{-1}. \quad (46)$$

Suppose now that domestic government expenditure increases. This shock increases domestic aggregate demand relative to foreign aggregate demand. By the price elasticity effect of deep habits, firms will lower domestic markups relative to foreign markups. That is, good a will become relatively cheaper in the domestic country than in the foreign country. Similarly, the increase in government spending leads to an increase in domestic demand for good b , inducing foreign firms to lower domestic markups relative to foreign markups. That is, the price of good b falls domestically relative to the rest of the world. The fact that all goods in the domestic economy (a and b) become cheaper relative to the foreign economy implies that the real exchange rate of the country experiencing the increase in government purchases depreciates.

The decline in markups brought about by the expansion in government spending, is key for the deep-habit model to predict an increase in private consumption. To see this, note first that the increase in government spending produces a negative wealth effect on households, which, all other things equal, induces households to reduce consumption and increase labor effort. In turn, the expansion in the labor supply schedule tends to depress real wages. This is the basic mechanism at work in the standard neoclassical model. Under deep habits, however, the decline in markups that takes place following the government spending shock acts as a positive productivity shock that shifts the labor demand upward. This expansion in the demand for labor can be strong enough to cause the real wage to increase. In turn, higher real wages produce a substitution effect whereby households increase consumption and reduce the demand for leisure. This substitution effect may be strong enough to offset the negative wealth effect on consumption. In this case, private consumption increases in response to an expansion in government spending.

5. Calibration and Functional Forms

The period utility function and the aggregator functions are assumed to be of the forms:

$$U(x, h) = \frac{\left[x_t^\phi (1 - h_t)^{1-\phi} \right]^{1-\sigma} - 1}{1 - \sigma}, \quad (47)$$

$$\chi(x_a, x_b) = \left[\omega x_a^{1-1/\xi} + (1 - \omega) x_b^{1-1/\xi} \right]^{1/(1-1/\xi)}, \quad (48)$$

436 and

$$\chi^*(x_a^*, x_b^*) = \left[(1 - \omega) x_a^{*1-1/\xi} + \omega x_b^{*1-1/\xi} \right]^{1/(1-1/\xi)}. \quad (49)$$

437

[Table 1 about here.]

438 Table 1 displays the values assigned to the structural parameters in the baseline calibration of the model.
 439 The time unit is meant to be one quarter. The discount factor β is set at a value consistent with an interest
 440 rate of 4 percent per year. The curvature of the period utility function, σ , is set at 1, which implies that
 441 preferences are separable in leisure and consumption. The case of separable preferences in consumption
 442 and leisure is of particular interest because it highlights the fact that the pricing-to-habits mechanism does
 443 not depend on the assumption of nonseparabilities between leisure and consumption to deliver empirically
 444 realistic dynamics for consumption and the real exchange rate in response to public consumption shocks.
 445 The parameter ϕ of the utility function is chosen so that households devote about one fourth of their time
 446 to paid work in the deterministic steady state. The parameter ω of the aggregator function of domestic and
 447 foreign goods is set to 0.5. This value allows us to abstract from home-bias effects in the transmission of
 448 government spending shocks. It implies a relatively high share of imports in GDP of 50 percent. In our
 449 sample, the average share of imports in GDP is 22 percent, which would correspond to a value of ω of 0.7.
 450 Later in section 8 the robustness of our findings to increasing the value of ω is discussed. The elasticity
 451 of substitution between home and foreign goods, ξ , is set to 1.5, a value commonly used in business-cycle
 452 analysis. The elasticity of substitution across habit-adjusted consumption of individual varieties, η , is set
 453 to 5. The steady-state level of government consumption is assumed to represent 20 percent of value added,
 454 which is the mean value of the observed government share in our sample. The implied steady-state level of
 455 government spending, $g = g^*$, is 0.0487. The feedback rule for government spending given in equation (24)
 456 is calibrated using the econometric estimates obtained in section 2. Specifically, the following values are
 457 assigned

$$\begin{bmatrix} B_0^1 \\ B_1^1 \\ B_2^1 \\ B_3^1 \end{bmatrix} = \begin{bmatrix} 0.656 & -0.234 & 0.0878 & 0.0198 & 0.0138 \\ 0.156 & 0.263 & -0.18 & -0.144 & -0.0632 \\ 0.134 & -0.0348 & 0.0671 & 0.189 & 0.0421 \\ -0.0385 & 0.0349 & 0.0494 & -0.0632 & -0.0451 \end{bmatrix}. \quad (50)$$

458 6. Estimation of the Deep-Habit Parameters

459 There exists no readily available evidence on the parameters defining the deep-habit mechanism. For
 460 this reason, we proceed to estimate them. The parameter structure is simplified by assuming that the
 461 degree of habit formation is common across types of goods and countries. That is, it is imposed that
 462 $\theta_a^c = \theta_b^c = \theta_a^{c*} = \theta_b^{c*} = \theta^c$ and $\theta_a^g = \theta_b^g = \theta_a^{g*} = \theta_b^{g*} = \theta^g$. The parameter θ^c is not constrained to be equal to
 463 θ^g . In this way, the data determines the degrees of private and public deep-habit formation separately. In
 464 addition, the parameter ρ measuring the persistence in the stock of habits is also econometrically estimated.

465 Our estimation procedure consists in assigning values for θ^c , θ^g , and ρ to minimize the distance between
 466 the empirical impulse response functions shown with solid lines in figure 1 and the corresponding theoretical
 467 impulse response functions implied by the deep-habit model. The theoretical impulse response functions
 468 up to first order are computed using the log-linearization procedure described in Schmitt-Grohé and Uribe
 469 (2004). The first 9 quarters of the impulse response functions of 5 variables (government spending, output,
 470 consumption, the trade balance-to-GDP ratio, and the real exchange rate) to a unit innovation in government
 471 spending are considered. Specifically, let $\Theta \equiv [\theta^c \ \theta^g \ \rho]'$ denote the 3×1 vector of parameters to be estimated,
 472 IR^e the 44×1 vector of empirical impulse response functions, and $IR^m(\Theta)$ the corresponding vector of

473 impulse responses implied by the theoretical model, which is a function of the three parameters that we wish
 474 to estimate. Then, the estimate of Θ , denoted $\hat{\Theta}$, is given by

$$\hat{\Theta} = \underset{\Theta}{\operatorname{argmin}} [IR^e - IR^m(\Theta)]' \Sigma_{IR^e}^{-1} [IR^e - IR^m(\Theta)], \quad (51)$$

475 where Σ_{IR^e} is the 44×44 variance covariance matrix of IR^e computed using the delta method. This ma-
 476 trix penalizes those elements of the estimated impulse response functions associated with large confidence
 477 intervals.¹²

478 An estimate of the variance-covariance matrix of $\hat{\Theta}$, denoted $\Sigma_{\hat{\Theta}}$, is given by

$$\Sigma_{\hat{\Theta}} = \left[J_{IR^m}(\hat{\Theta})' \Sigma_{IR^e}^{-1} J_{IR^m}(\hat{\Theta}) \right]^{-1}, \quad (52)$$

479 where $J_{IR^m}(\Theta) \equiv \partial IR^m(\Theta) / \partial \Theta$ denotes the 44×3 Jacobian matrix of the theoretical impulse response
 480 function with respect to the vector Θ .

481 The estimation results are shown in table 2.

482 [Table 2 about here.]

483 The estimated degree of deep habit formation in private consumption is 0.52, which lies well within the
 484 range of values estimated on the basis of models featuring superficial habit formation. The estimated degree
 485 of deep habit persistence in public consumption is slightly higher than its private counterpart at 0.57. The
 486 estimated value of ρ is 0.9876, which implies that the stock of habits depreciates rather slowly over time.
 487 This finding is not uncommon in the related literature on superficial habits. For example, consumption-
 488 based models of stock returns typically require a high degree of persistence in the habit stock to fit the data
 489 (Campbell and Cochrane, 1999). Section 8 studies the sensitivity of our results to lowering the value of ρ .
 490 All parameters are estimated to be significantly different from zero. Of particular interest is the fact that
 491 the data identifies a nonnegligible amount of deep-habit persistence in public consumption.

492 7. Comparing Predicted and Observed Impulse Responses

493 Figure 1 plots with crossed lines the impulse responses to a one-percent increase in government spending
 494 predicted by the deep-habit model. The deep-habit model predicts an expansion in output and private
 495 consumption, a deterioration in the trade balance, and a depreciation of the real exchange rate. The model
 496 does a relatively good job at explaining the observed transmission of government spending shocks. All
 497 predicted responses fall within the estimated error bands, except for the late transition dynamics of the real
 498 exchange rate. As is well known, real exchange rate movements are highly persistent, a fact that in our
 499 regressions is reflected in a peak response occurring only 10 quarters after the innovation. Explaining such a
 500 high level of persistence in the real exchange rate is a challenge for many macroeconomic models including
 501 ours.

502 7.1. Markups

503 An important prediction of the deep habit model is that markups move countercyclically in equilibrium.
 504 An increase in domestic government spending induces a decline in markups in all domestically sold goods,
 505 regardless of whether they are imported or domestically produced.

506 At the same time, in the foreign economy markups increase as a consequence of a contraction in foreign
 507 aggregate demand brought about by the negative wealth effect associated with the increase in domestic
 508 government spending (and transmitted via complete international asset markets). The impulse responses
 509 of the domestic and foreign markups are shown in figure 2(a).¹³ In response to a one-percent increase in

¹²The impulse response functions implied by the estimated theoretical model shown below are little changed when the weighing matrix is defined as the diagonal of Σ_{IR^e} rather than as Σ_{IR^e} itself.

¹³Because of our maintained assumption of no home bias ($\omega = 1/2$), the impulse response functions of the domestic markups on imported and domestically produced goods are identical. For the same reason, the impulse response functions of foreign markups on goods produced in the domestic and the foreign countries are also identical.

510 domestic government spending, markups in domestic markets fall by 26 basis points on impact and markups
 511 in foreign markets rise by 7 basis points.

512 [Figure 2 about here.]

513 Firms selling in domestic markets find it optimal to reduce markups because the increase in aggregate
 514 demand stemming from the local public sector renders the demand for individual goods more price elastic.
 515 Recall that in the deep habit model, the price elasticity is an increasing function of the importance of
 516 current demand relative to habitual demand. The increase in government spending increases the importance
 517 of current demand causing a rise in the price elasticity and a corresponding decline in markups. At the
 518 same time, the decline in aggregate demand in the foreign country causes a decline in the price elasticity of
 519 demand across all markets inducing sellers to increase their margins.

520 The generalized fall in markups that takes place in the domestic economy following a positive innovation
 521 in government spending acts much like a positive technology shock, shifting the demand for labor out and
 522 to the right. This increase in the demand for labor tends to push real wages upward. Figure 2(b.) shows
 523 that the real wage increases by 0.26 percent in response to a one-percent government spending shock. This
 524 prediction of the deep-habit model is consistent with SVAR evidence employing the Blanchard and Perotti
 525 (2002) identification assumption. See, for example, Perotti (2008) for evidence from the United States, the
 526 United Kingdom, and Canada, three of the four countries included in our panel.

527 A natural question is whether in the data markups of prices over marginal cost indeed fall in response to
 528 a positive innovation in government spending, as required for our theoretical model to capture the observed
 529 increase in consumption and real depreciation of the exchange rate. Monacelli and Perotti (2008) provide
 530 empirical evidence for the United States supporting the countercyclicality of markups in response to govern-
 531 ment spending shocks. These authors identify movements in markups with movements in the inverse of the
 532 labor share. We note that this identification approach is valid in the context of our theoretical framework.
 533 For in our model, the domestic markup equals the inverse of the domestic real product wage, which, in turn,
 534 given our assumption of a linear production technology, equals the inverse of the labor share.

535 The implied countercyclicality of markups is crucial in allowing the deep-habit model to capture the
 536 observed expansion in private consumption and the observed initial depreciation of the real exchange rate. In
 537 effect, the combination of lower domestic markups and higher foreign markups makes the domestic economy
 538 cheaper relative to the foreign economy. That is, the domestic real exchange rate depreciates. In fact, the
 539 real depreciation of about one third of one percent on impact predicted by the model is equal to the sum of
 540 the decline in markups in domestic markets (26 basis points) and the increase in markups in foreign markets
 541 (7 basis points).

542 7.2. The real exchange rate

543 As discussed in the introduction, accounting for the observed depreciation of the domestic real exchange
 544 rate in response to a positive innovation in government spending poses a major challenge for the neoclassical
 545 growth model. Figure 2 (c.) substantiates this claim. It displays the response of the real exchange rate under
 546 deep and superficial habits. In the economy with superficial habits, habits form at the level of each composite
 547 good (domestic and imported), as opposed to at the level of each individual variety. The figure shows that
 548 the deep habit model captures well the observed initial real exchange rate depreciation. By contrast, the
 549 superficial habits model counterfactually predicts that the real exchange rate is completely unaffected by
 550 the government spending shock. The same mute response in the real exchange rate would obtain under the
 551 assumption of no habits at all.

552 To understand why the real exchange rate is unresponsive in the absence of deep habits, note that in the
 553 economy with superficial or no habits, the monopolists producing individual varieties of goods face a static
 554 demand function with a constant price elasticity. Therefore, equilibrium markups are constant over time
 555 and across countries. Furthermore, because the marginal costs of producing a given variety is independent
 556 of destination market, the monopolistic producer will charge the same price in the domestic and the foreign
 557 markets. Thus, in the absence of deep habits we have that $P_{i,a,t} = P_{i,a,t}^*$ and $P_{i,b,t} = P_{i,b,t}^*$ for all $i \in [0, 1]$. So
 558 that, under the maintained assumption of no home bias ($\omega = 0.5$), the domestic and foreign consumer price
 559 indices are identical, or, equivalently, the real exchange rate is constant over time. We note that if in the
 560 economies with superficial or no habits one were to allow for home bias, by setting $\omega > 0.5$, then an increase

561 in government purchases would increase the price of good a relative to good b causing a counterfactual
 562 appreciation of the real exchange rate.

563 7.3. Consumption

564 A second major difficulty of the neoclassical growth model is its inability to explain the observed expansion
 565 in private consumption following an increase in public spending. Figure 2(d.) illustrates this problem
 566 by depicting the impulse response function of consumption to an innovation in government spending in
 567 the economy with superficial habits. The counterfactual predicted decline in consumption is driven by a
 568 negative wealth effect brought about by the elevated absorption of resources in the public sector.¹⁴ A
 569 central contribution of the deep-habit mechanism is to enable an otherwise standard model to overcome
 570 this difficulty. In effect, figure 2(d.) shows that the deep-habit model predicts not only an expansion in
 571 consumption but also one that is similar in magnitude and persistence to the one estimated using actual
 572 data. As in the model with superficial habits, in the model with deep habits an increase in government
 573 spending creates a negative wealth effect, which tends to depress private consumption spending. However,
 574 the deep-habit mechanism generates, at the same time, an increase in wages, driven by a generalized decline in
 575 markups, which induces households to substitute away from leisure and into consumption. This substitution
 576 effect more than offsets the negative wealth effect, resulting in an equilibrium increase in consumption.

577 8. Sensitivity Analysis

578 This section reports results of a number of robustness checks regarding the ability of the deep-habit model
 579 to explain the response of consumption, the real exchange rate, and net exports to government spending
 580 shocks. These tests include allowing for home bias, reducing the persistence of the stock of habit, considering
 581 an alternative method—the HP filter—for extracting the cyclical component of time series in the empirical
 582 analysis, introducing capital accumulation into the theoretical model, and estimating the SVAR system using
 583 artificial time series generated by the theoretical model.

584 8.1. Home Bias

585 In our baseline model, no home bias in consumption is assumed. That is, the parameter ω in the
 586 aggregator function of domestic and foreign goods (equation (3)) takes the value 0.5. As indicated earlier,
 587 this value of ω implies an import share of 50 percent of GDP, which is large relative to the average import
 588 share of 22 percent observed in our panel. When ω is exactly 0.5, an increase in domestic aggregate demand
 589 does not lead to an increase in the relative price of domestically produced goods. That is, the relative price of
 590 imported goods in terms of domestically produced goods, $P_{b,t}/P_{a,t}$, is unchanged. It follows that movements
 591 in the real exchange rate are entirely due to variations in the deviations from the law of one price, via the
 592 deep-habit mechanism, and not due to variations in the relative price of imported goods.

593 When ω is set to 0.7, the implied steady-state import share is more in line with its empirical counterpart
 594 observed in our panel. For this value of ω , agents in both countries have a bias toward goods produced
 595 in their own country. In the presence of home bias, an increase in domestic government spending causes
 596 an increase in the domestic price of domestically produced goods relative to the domestic price of foreign-
 597 produced goods. That is $P_{a,t}/P_{b,t}$ goes up. Because goods of type a have a larger share in the domestic CPI
 598 index than in the foreign CPI index, the increase in the relative price of domestically produced goods tends,
 599 all other things equal, to appreciate the real exchange rate. The response of the real exchange rate to an
 600 increase in aggregate demand is then determined by two (opposing) effects, the domestic-relative-price effect,
 601 which tends to appreciate the real exchange rate and the pricing-to-habits effect, which tends to depreciate
 602 it. Figure 2(e.) compares the response of the real exchange rate to a positive government spending shock in
 603 economies with and without home bias. In the economy with home bias, all parameters other than ω take
 604 the values shown in tables 1 and 2. Overall, the two theoretical impulse responses for the real exchange
 605 rate are fairly similar. In line with the intuition developed above, when home bias is present, the impulse
 606 response function of the real exchange rate lies below the one corresponding to the baseline case without
 607 home bias.

¹⁴Government spending shocks also have contractionary effects on consumption in the case of no habits at all.

608 Figure 2(f.) compares the impulse response of consumption in an economy with and without home bias.
 609 The deep-habit model with home bias continues to predict a persistent rise in consumption that tracks the
 610 actual response fairly well.

611 8.2. Persistence of Habit Stocks

612 Our second robustness check concerns the persistence of the habit stocks. Our estimation of the pricing-
 613 to-habits model yields a value of ρ of 0.9876, which induces highly persistent stocks of habit in equilibrium.
 614 To gauge the sensitivity of our results to a less persistent stock of habits, consider the case that $\rho = 0.85$.
 615 This value is more than four standard deviations below its point estimate. All other parameters take the
 616 values shown in tables 1 and 2. Figures 2(e.) and (f.) display with diamonds the impulse responses of the
 617 real exchange rate and consumption for this value of ρ . As one would expect, the impulse responses of the
 618 real exchange rate and consumption are less persistent when the stock of habits itself is less persistent.

619 8.3. HP Filtering

620 Our third sensitivity experiment focuses on the detrending method used to compute empirical impulse
 621 responses to a government spending shock. In the baseline case all variables are detrended using a quadratic
 622 trend. Here this detrending method is replaced with the Hodrick-Prescott filter.

623 [Figure 3 about here.]

624 Figure 3 shows the empirical impulse response functions obtained after HP filtering the data with a
 625 smoothing parameter of 1,600. Comparing this figure with figure 1, one can see that the empirical impulse
 626 responses obtained from HP filtered data are quite similar to those obtained after removing a quadratic trend
 627 from the raw data. In particular, a positive innovation in government spending causes an increase in output
 628 and consumption, a depreciation of the real exchange rate, and a deterioration of the trade-balance-to-output
 629 ratio. Figure 3 also depicts the impulse responses predicted by the theoretical model, where the structural
 630 parameters of the deep-habit mechanism were reestimated to match the impulse responses associated with
 631 the HP-filtered data.¹⁵ Inspection of the figure suggests, that the fit of the theoretical model does not
 632 appear to be sensitive to whether the empirical impulse responses are estimated from HP filtered or from
 633 quadratically detrended data.

634 8.4. Capital Accumulation

635 A further sensitivity experiment consists in allowing for capital accumulation in the domestic and foreign
 636 economies. To this end, assume that domestic output of variety i of type a , $y_{i,a,t}$, is produced according to
 637 the technological relationship

$$638 \quad y_{i,a,t} = k_{i,a,t}^\alpha h_{i,a,t}^{1-\alpha}, \quad (53)$$

639 where $k_{i,a,t}$ and $h_{i,a,t}$ denote, respectively, capital and labor services used in the production of variety i of
 640 goods of type a . Set the parameter α to 0.25. Capital is accumulated by households and evolves according
 641 to the law of motion

$$642 \quad k_{t+1} = (1 - \delta)k_t + x_t^I \left[1 - \frac{\kappa}{2} \left(\frac{x_t^I}{x_{t-1}^I} - 1 \right)^2 \right], \quad (54)$$

643 where k_t denotes the aggregate level of physical capital and x_t^I denotes gross investment. Set the parameters
 644 δ and κ governing the rate of depreciation and the degree of investment adjustment costs at 0.025 and 15,
 645 respectively. The investment good is a composite of domestic and foreign goods of the type

$$646 \quad x_t^I = \left[\omega(x_{a,t}^I)^{1-1/\xi} + (1 - \omega)(x_{b,t}^I)^{1-1/\xi} \right]^{1/(1-1/\xi)}, \quad (55)$$

¹⁵The resulting point estimates of θ^c , θ^g , and ρ are, respectively, 0.56, 0.48, and 0.99.

644 where $x_{a,t}^I$ and $x_{b,t}^I$ denote investment goods of type a and b , respectively. In turn, these investment goods
 645 are composites of a continuum of intermediate varieties produced as follows

$$x_{a,t}^I = \left[\int_0^1 I_{i,a,t}^{1-1/\eta} di \right]^{1/(1-1/\eta)} \quad (56)$$

646 and

$$x_{b,t}^I = \left[\int_0^1 I_{i,b,t}^{1-1/\eta} di \right]^{1/(1-1/\eta)}, \quad (57)$$

647 where $I_{i,a,t}$ ($I_{i,b,t}$) denotes inputs of variety i and type a (b) in the production of investment good a (b). The
 648 resource constraint for capital requires that $k_t = \int_0^1 k_{i,a,t} di$. The production and accumulation of physical
 649 capital in the foreign economy is symmetric.

650 In the empirical SVAR, investment is measured as the sum of residential and nonresidential investment.
 651 Following Monacelli and Perotti (2006), the investment equation is estimated by replacing consumption with
 652 investment in the panel VAR system.

653 [Figure 4 about here.]

654 Figure 4 shows that the estimated response of investment to a one-percent increase in government spending
 655 is negative but insignificant. The two-standard-deviation confidence band includes zero at all horizons. This
 656 weak response of investment is in line with the findings of existing empirical studies. See, for instance,
 657 Perotti (2008), figure 3.14.¹⁶ As in previous sections, the structural parameters θ^c , θ^g , and ρ defining the
 658 degree of deep habit formation are estimated by minimizing a weighted difference between the theoretical
 659 and empirical impulse responses. The point estimates are $\theta^c = 0.53$, $\theta^g = 0.68$, and $\rho = 0.95$. These values
 660 are similar in magnitude to those estimated under the assumption of no capital accumulation. The model
 661 predictions regarding the responses of consumption and the real exchange rate to a government spending
 662 shock, which are the focus of our study, continue to be as successful in matching the observed responses
 663 as in the model without capital. The same is true for output and the trade-balance-to-output ratio. The
 664 predicted impulse response for investment lies within the two-standard-error band. These findings indicate
 665 that the ability of the deep-habit model to explain the response of consumption, the real exchange rate, and
 666 the trade balance to government spending shocks is robust to the introduction of capital accumulation.

667 8.5. Estimating the SVAR on Simulated Data

668 Our final sensitivity test sheds light on whether the theoretical impulse responses are comparable to the
 669 ones implied by the empirical VAR system. The reason why this question is of interest is that the theoretical
 670 model, driven by a single government spending shock, does not have a VAR representation of the type
 671 proposed in the empirical analysis. Even after adding structural shocks to equalize the number of disturbances
 672 and observables, a VAR representation may not exist. Furthermore, if a VAR representation did exist, the
 673 theoretical VAR system will in general contain an infinite lag structure, while its empirical counterpart
 674 must necessarily feature a finite lag length. To address this issue, exogenous structural disturbances are
 675 added to the deep habit model with capital accumulation and then impulse response functions are derived
 676 from SVARs estimated on artificial time series generated by the deep habit model. Specifically, a foreign
 677 government spending shock, domestic and foreign productivity shocks, and domestic and foreign preference
 678 shocks are added. All of these additional disturbances are assumed to follow AR(1) processes. The persistence
 679 and contemporaneous correlation of productivity shocks are set as in Backus et al. (1992), the persistence
 680 of the foreign government spending shock is set at 0.87, which is the observed serial correlation of public
 681 consumption in the postwar United States, and the persistence of the preference shocks is set at 0.9. Finally,
 682 the volatilities of the exogenous driving forces are calibrated to ensure that government spending shocks,
 683 preference shocks, and productivity shocks explain, respectively, 20 percent, 20 percent, and 60 percent of
 684 the unconditional variance of domestic output. It is assumed that shock volatilities are of equal size across

¹⁶Perotti uses a 68 percent confidence interval based on 500 Monte Carlo simulations.

685 countries. Then 10,000 time series for government spending, output, consumption, the trade-balance-to-
 686 output ratio, the real exchange rate, and investment are simulated from the theoretical model. The size of
 687 each of the 10,000 artificial samples is set at 512 observations, which matches the length of our panel data
 688 set (4 countries and 128 quarters per country). Finally, for each of the 10,000 samples a SVAR system is
 689 estimated using the same lag structure and identification assumptions as in the empirical analysis. Figure 4
 690 displays with circled lines the mean of the 10,000 impulse responses. The impulse responses obtained by this
 691 Monte Carlo experiment are almost identical to the true theoretical impulse responses. The main insight of
 692 this exercise is that in the context of our model and under our identification assumptions, an SVAR model
 693 uncovers the true impulse response functions to government spending shocks.

694 9. Conclusion

695 Using quarterly data from a panel of four industrialized countries from 1975 to 2005, we identify the effects
 696 of government spending shocks on output, consumption, the real exchange rate, and the trade balance.
 697 An increase in government spending produces an expansion in output, an expansion in consumption, a
 698 depreciation of the real exchange rate, and a deterioration of the trade balance.

699 A central contribution is to propose and test the hypothesis that deep habits generates a transmission
 700 mechanism for government purchases shocks that is consistent with this empirical evidence. The key feature
 701 of the transmission channel invoked by deep habits is countercyclical movements in equilibrium markups
 702 of prices over marginal costs. In our model, an increase in government spending generates a generalized
 703 decline in markups in domestic markets and an increase in markups in foreign markets. Thus, the domestic
 704 economy becomes inexpensive relative to the foreign economy, or the real exchange rate depreciates. At the
 705 same time, the decline in domestic markups shifts the demand for labor outward pushing real wages up. In
 706 turn, the increase in labor remunerations induces households to sacrifice leisure in favor of consumption. In
 707 the estimated deep-habit model, this substitution effect dominates the negative wealth effect stemming from
 708 the increase in public absorption of resources. As a result private consumption increases in equilibrium.

709 Estimation of the structural parameters defining the deep-habit mechanism provide strong evidence in
 710 favor of habit formation at a good-by-good level both in private and public consumption. The predictions of
 711 the deep-habit model replicate well the estimated impulse responses of output, consumption, and the trade
 712 balance, and the initial response of the real exchange rate. These results represent, in our opinion, a step
 713 forward in the understanding of the effects of fiscal policy.

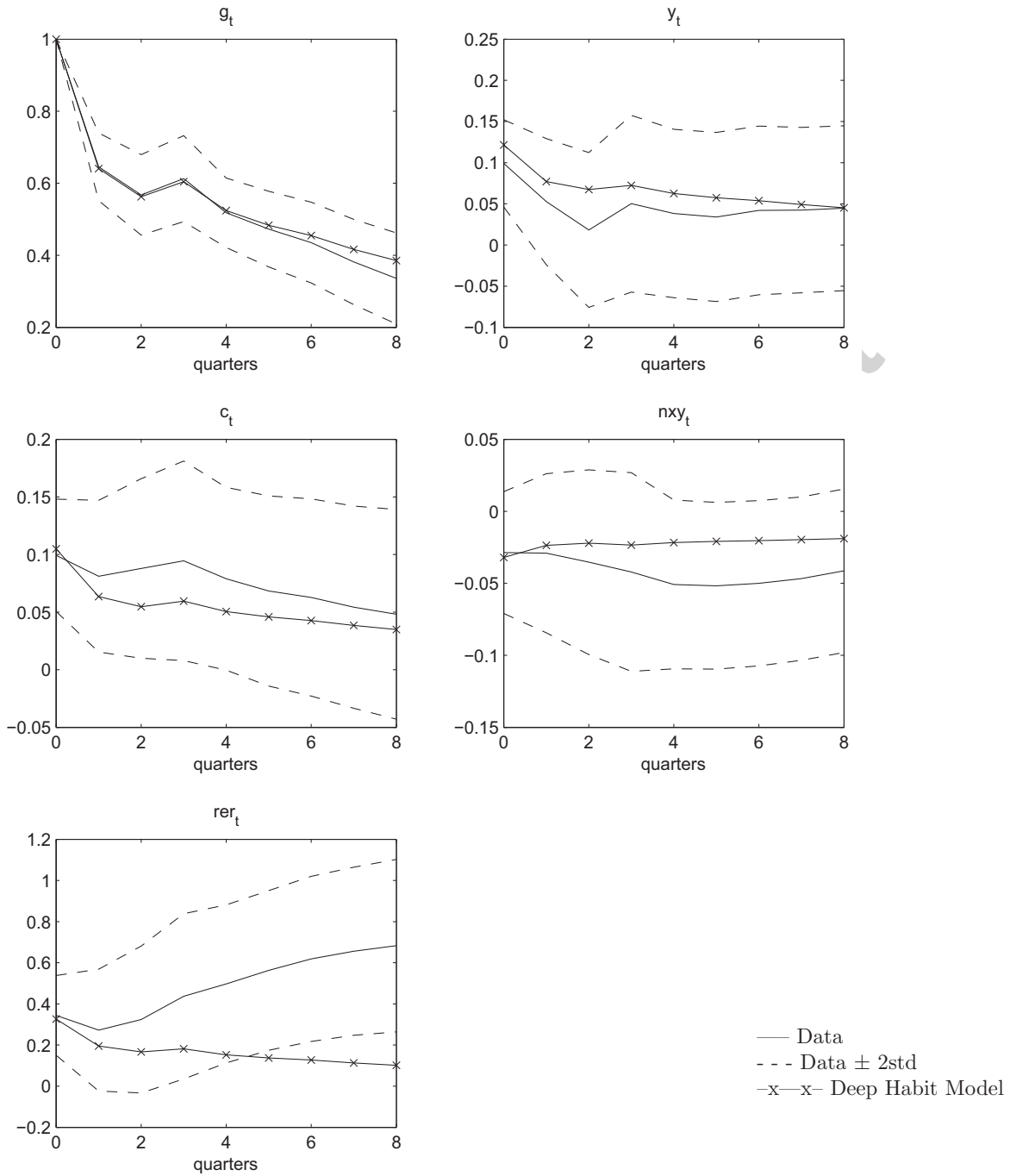
714 This paper focuses on explaining the effects of unanticipated changes in government spending identified
 715 using the SVAR methodology proposed in Blanchard and Perotti (2002). A natural next step in this research
 716 agenda is to understand the observed effects of anticipated increases in government spending, such as news
 717 about future expected military build-ups triggered by war, as identified by the narrative approach. In the
 718 working-paper version of this paper (Ravn, Schmitt-Grohé and Uribe, 2007, section 8), it is shown that in
 719 the context of a deep habit model, consumption and wages fail to increase upon the release of news about
 720 future expansions in public spending. This prediction of the deep habit model is consistent with the empirical
 721 evidence emerging from the narrative approach to identifying government spending shocks.

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Figure 1: Estimated and Predicted Impulse Responses To A One-Percent Innovation in Government Spending



Note. All responses are expressed in percent deviations from trend with the exception of the net exports-to-GDP ratio, which is in level deviations from trend and expressed in percentage points of GDP.

Figure 2: Robustness

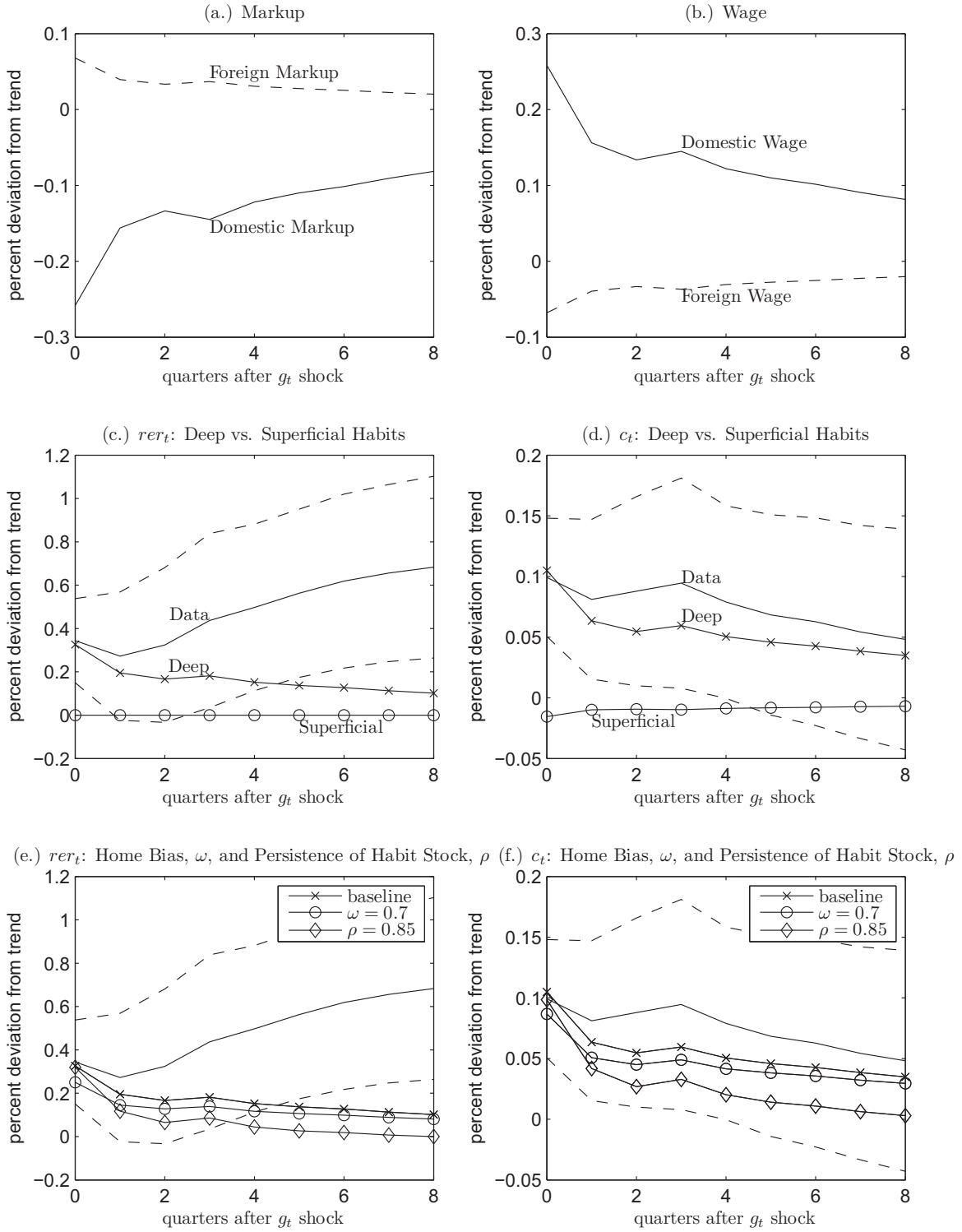
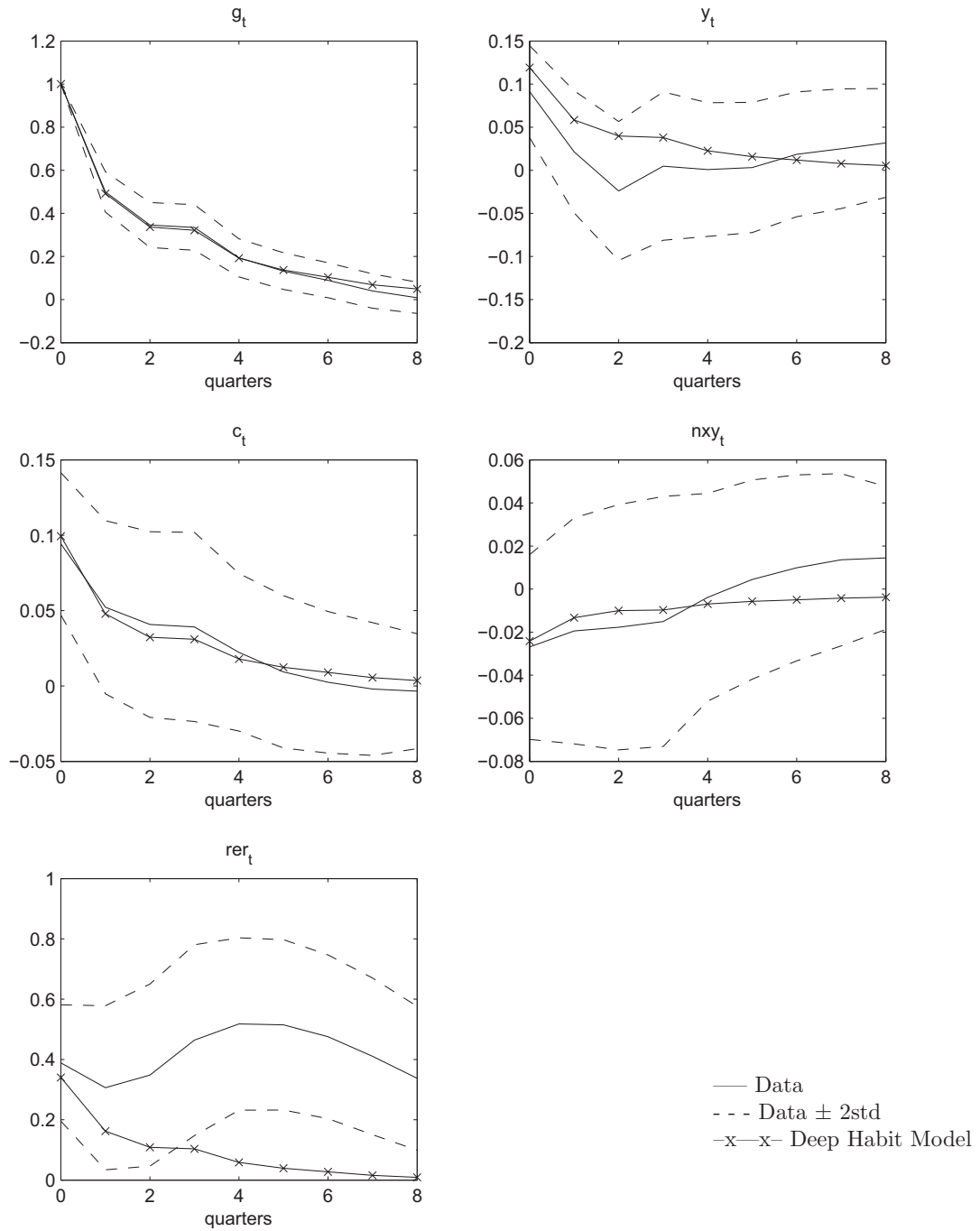
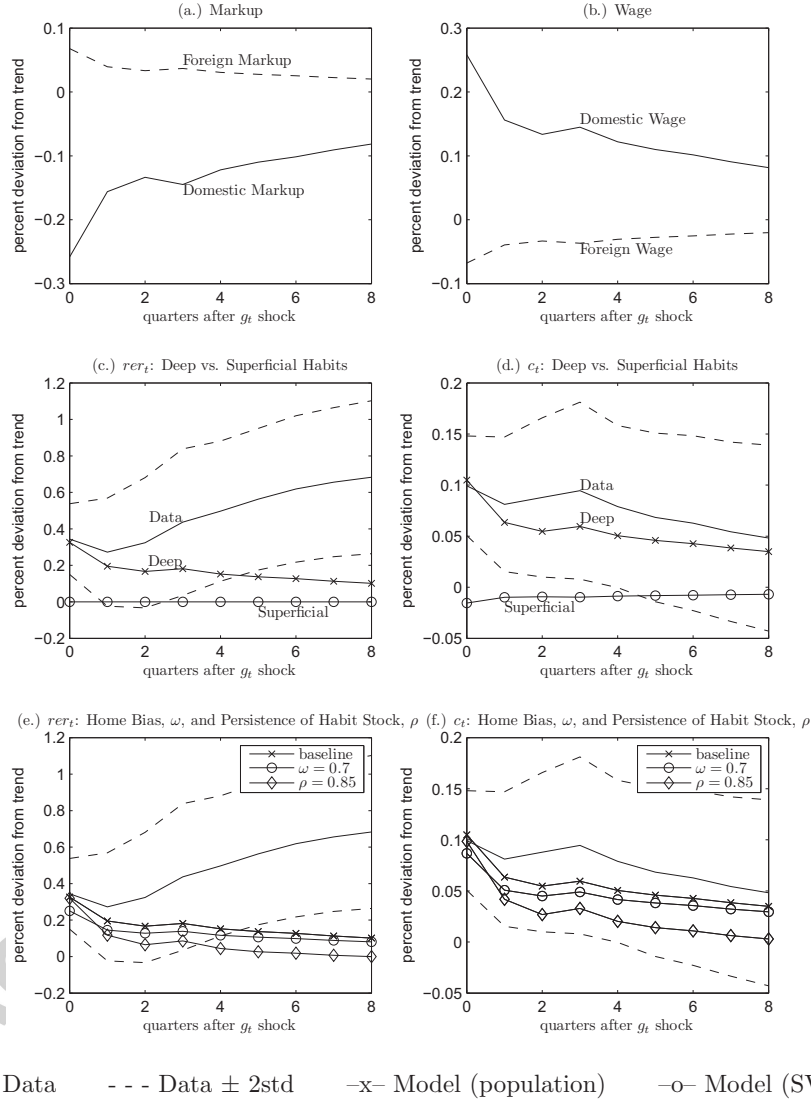


Figure 3: Sensitivity Analysis: HP Filtering



Note. All responses are expressed in percent deviations from trend with the exception of the net exports-to-GDP ratio, which is expressed in level deviations from trend.

Figure 4: The Model With Capital Accumulation: Predicted and Estimated Impulse Responses To A One-Percent Innovation in Government Spending



Note. All responses are expressed in percent deviations from trend with the exception of the net exports-to-GDP ratio, which is in level deviations from trend and expressed in percentage points of GDP.

Table 1: Calibrated Parameters

Parameter	Value	Description
β	0.99	Subjective discount factor (quarterly)
σ	1	Intertemporal elasticity of substitution
ϕ	0.15	Preference parameter
ω	0.5	Preference parameter
ξ	1.5	Elasticity of substitution between home and foreign goods
η	5	Elasticity of substitution among varieties of habit-adjusted consumption
s_g, s_g^*	0.2	Steady-state share of government consumption in GDP

Table 2: Estimated Parameters

Parameter	Point Estimate	Standard Deviation	Description
θ^c	0.52	0.08	Degree of deep-habit formation in private consumption
θ^g	0.57	0.15	Degree of deep-habit formation in public consumption
ρ	0.9876	0.03	Persistence of deep-habit stock

Research Highlights

- Cross-country panel VAR estimation of effects of governments spending shocks
- Government spending increases raise output and private consumption
- Government spending increases depreciate the real exchange rate
- A deep-habit model for the international transmission of government spending shocks
- Model explains the rise in consumption and depreciation of the real exchange rate

Accepted manuscript