

Partitioning uncertainty in climate predictions using data from undesigned climate experiments

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Human-induced climate change



Greenhouse gases (warming)

CO₂ (fossil fuels, deforestation) methane (livestock), N₂O (fertilizers) **Industrial air pollution (cooling)**

sulphates, soot



Increase in global temperature

Arctic shrinkage, sea level rise change in disease patterns, species extinctions



Changes in climate (long-term weather) change in rainfall patterns, extreme weather? floods? drought?







Global warming and climate change



Question: What will the climate be like over the next 100

years?

Answer: It will depend on

what the world is like in the future - guesses (scenarios);

how the atmosphere/oceans react - climate models.

IPCC Fourth Assessment Report (AR4) 2007

- IPCC : Intergovernmental panel on climate change.
- Provides an objective assessment of the latest literature on climate change.
- Provides climate predictions for 2000-2100 from many climate models under different socio-economic scenarios.

Socio-economic scenarios



(Educated) guesses at what the world will be like over the next 100 years.

B1: low emissions, clean and efficient technologies, global sustainability, population peaks in 2050.

A2: medium-high emissions, economic growth on regional scales, increasing population.

A1B: high emissions (a balance across all fuel sources), very rapid economic growth, market forces dominate, population peaks in 2050.

... and many others.

General Circulation Models (GCMs)



- mathematical models of atmosphere/oceans based on the laws of physics/chemistry;
- require large amounts of computing power and time;
- produce predictions of climate variables.

Comments

- Different scientists produce different GCMs.
- Predictions depend on scenario.
- Small changes in the input conditions can produce big changes in the predictions, i.e. different runs of the model produce different predictions.

IPCC AR4 data



A2 1 5 0 1	B1 1 5 1 1
•	
5 0 1	5 1 1
0 1 1	1
1	1
1	4
	- 1
1	1
1	1
1	1
0	2
0	0
1	1
0	3
1	0
1	1
1	1
0	1
3	3
3	3 3
3	3
5	5
5	8
4	4
1	1
1	0
40	48
	1 0 1 1 1 0 3 3 5 5 4 1 1

No design. Not the best use of a lot of computational effort!

Sources of climate uncertainty



Question: Is variability in predicted climate variables due mainly to choice of

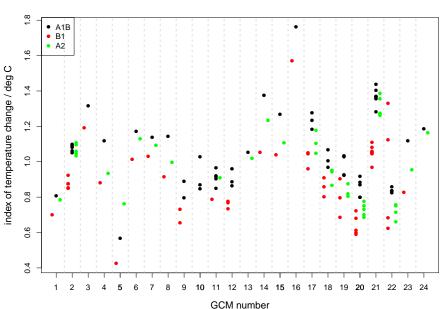
- GCM.
- socio-economic scenario, or
- GCM run?
- ... or a mixture of these?
- ...does it matter how far into the future we want to look?
- ... does the climate variable matter?
- ...does the region of the world matter?

Simple measures of climate change, e.g. global temperature

- 1. average change in 2020–2049 (relative to 1980–1999)
- 2. average change in 2069–2098 (relative to 1980–1999)

Global temperature change 2020–2049





A 2-way random effects ANOVA



 Y_{ijk} = measure of change for **GCM** i, **scenario** j and **run** k.

$$Y_{ijk} = \mu + \alpha_i + \beta_j + \gamma_{ij} + \epsilon_{ijk},$$

 $\begin{array}{lll} \mu & \text{overall mean change} \\ \alpha_i & \text{adjustment for GCM } i & \alpha_i \stackrel{\textit{iid}}{\sim} \textit{N}\left(0,\sigma_{\!_{G}}\right) \\ \beta_j & \text{adjustment for scenario } j & \beta_j \stackrel{\textit{iid}}{\sim} \textit{N}\left(0,\sigma_{\!_{S}}\right) \\ \gamma_{ij} & \text{scenario-specific adjustment for GCM } i & \gamma_{ij} \stackrel{\textit{iid}}{\sim} \textit{N}\left(0,\sigma_{\!_{GS}}\right) \\ \epsilon_{ijk} & \text{residual effect of variability over runs} & \epsilon_{ijk} \stackrel{\textit{iid}}{\sim} \textit{N}\left(0,\sigma_{\!_{B}}\right) \end{array}$

- $\alpha_i \stackrel{\textit{iid}}{\sim} N(0, \sigma_G)$ means $\alpha_1, \alpha_2, \ldots$ are independent and normally distributed with mean 0 and st. dev. σ_G .
- Imagine a population of GCMs,each producing a separate effect on Y_{iik}.
- We assume that all random variables are independent.

Interpretation of parameters



- μ overall temperature change (headline value in newspaper)
- σ_G variability over GCMs
- $\sigma_{\mathcal{S}}$ variability over scenarios
- σ_{GS} variability of scenario-specific adjustment for GCM
- σ_R variability over runs
 - Large value of σ ⇒ variable makes a big difference to predictions of global temperature:
 e.g. if σ_G is large then the choice of GCM really matters.
 - Large variability ⇒ large uncertainty.

Statistical inference



Issues

- 1. Scenario has only 3 levels. Little information about variability over scenarios σ_S .
- 2. Lack of balance.
- 3. No runs for some GCM-scenario combinations.
 - REML (cf. posterior mode). Gilmour & Goos (2009) argue against REML : σ_S tends to be underestimated.
 - Bayesian inference with weakly-informative priors.

Weakly-informative priors



Use a prior distribution that is

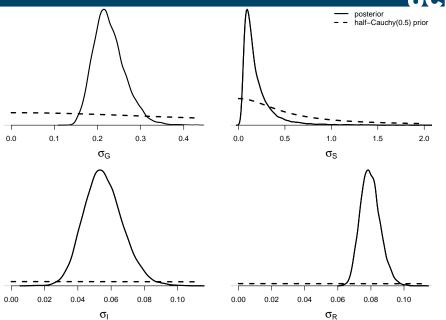
- weakly-informative for σ_S , and
- uninformative for σ_G , σ_{GS} , σ_R (and μ).

Idea

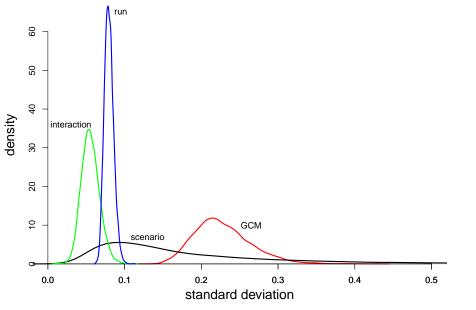
- downweight unrealistic values of σ_S because the data aren't informative enough to discount these values;
- otherwise let the data speak for themselves;
- Gelman (2006) argues against improper uniform priors and the inverse-gamma family (improper posteriors can result and/or undue sensitivity to parameters of priors)
- ... and for a half-Cauchy prior ...

Global temperature 2020–2049

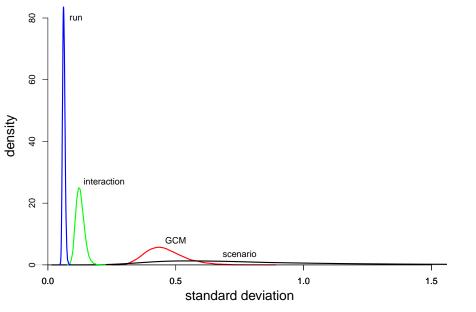




Global temp. 2020–2049: posterior distns_≜UCL

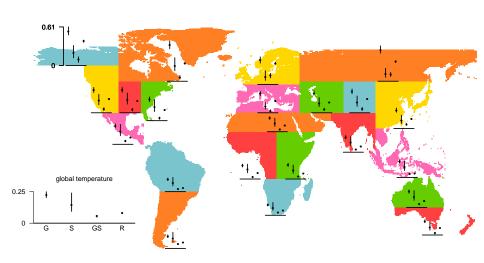


Global temp. 2069–2098: posterior distns LUCL



Regional temperature: 2020–2049

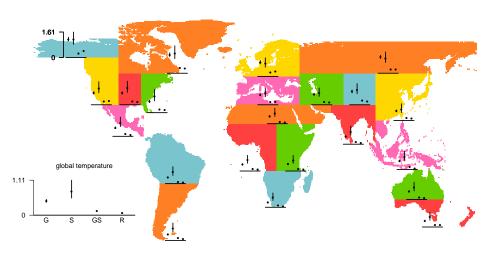




median (•) and line between quartiles

Regional temperature: 2069–2098





median (•) and line between quartiles

Summary for temperature



2020-2049

- Global: variability over GCMs > scenario > runs
- Regional: runs matters more than scenario in some areas,
 e.g. In the north

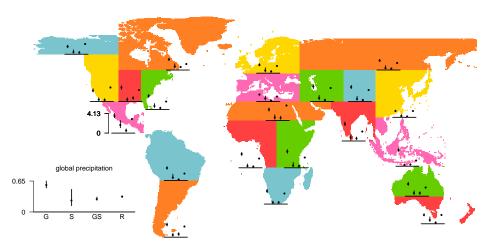
2069-2098

- Scenario matters more as we move through the 21st century (obviously!)
- Scenario is at least as important as GCM in most regions

Regional rainfall: 2020-2049



Percentage change in mean from 1980–1999

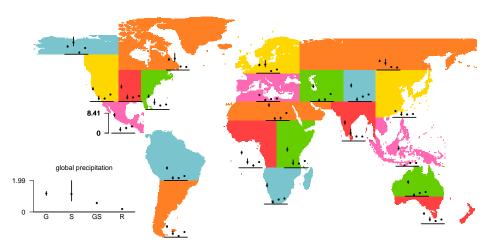


median (•) and line between quartiles

Regional rainfall: 2069-2098



Percentage change in mean from 1980–1999



median (•) and line between quartiles

Summary for rainfall



2020-2049

- Global: variability over GCMs largest, but relatively high variability over different runs from the same GCM
- Regional: a similar picture. In some areas (e.g. Alaska)
 var. over runs > var. over GCMs

2069-2098

- Global : choice of scenario becoming more important as century progresses
- In many regions scenario is relatively unimportant

Concluding remarks



- 1. Climate uncertainty depends on
 - the variable of interest;
 - the region of the world;
 - the time horizon.
- 2. Simple statistical models are useful.
- 3. Scope to improve design of climate experiments.

References

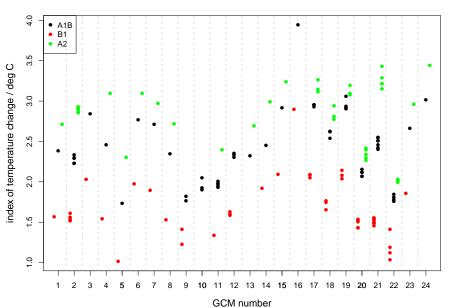


- Gelman, A. (2006) Bayesian Analysis, 1(3), 515-533
- Gilmour, S.G. and Goos, P. (2009) Appl. Statist. 58(4), 467–484
- WCRP CMIP3 Multi-Model Dataset Archive at PCMDI https://esgcet.llnl.gov: 8443/home/publicHomePage.do
- KNMI Climate Explorer http://climexp.knmi.nl

Thank you for your attention

Global temperature change 2069–2098





Experimental design (2-way RE ANOVA)

ŮCL

- Review of design for variance components estimation: Khuri, A.I. (2000) Inst. Statist. Rev., 68(3),311–322
- Optimal design depends on σ_G, σ_S, σ_R (prior information; adaptive designs?)
- 1. Fixed number of GCMs and scenarios
 - Balanced design is optimal
- 2. Can choose numbers of GCMs and scenarios
 - If R is dominant balanced design is optimal
 - If not, there are more efficient unbalanced designs
 - If $\sigma_S >> \sigma_R$ we need large number of scenarios and small number of runs per scenario.