1. * Find a maximum flow and a minimum cut for the following networks. Explain the steps you take. Explain why the flow and the cut you found are optimal.

2. (Hard) Show that any basic feasible solution to the dual of the maximal flow problem corresponds to a certain cut with the dual objective value equal to the capacity of the cut. Explain why this gives another (not easier) proof of the maximal flow–minimal cut theorem.